

# Computer algebra independent integration tests

Summer 2022 edition

1-Algebraic-functions/1.1-Binomial-products/1.1.3-General/28-

1.1.3.6-g-x<sup>m</sup>-a+b-x<sup>n</sup>-<sup>p</sup>-c+d-x<sup>n</sup>-<sup>q</sup>-e+f-x<sup>n</sup>-<sup>r</sup>

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# Chapter 1

## Introduction

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This report gives the result of running the computer algebra independent integration test. The download section in the appendix contains links to download the problems in plain text format used for all CAS systems.

The number of integrals in this report is [ 46 ]. This is test number [ 28 ].

## 1.1 Listing of CAS systems tested

The following are the CAS systems tested:

1. Mathematica 13.1 (June 29, 2022) on windows 10.
2. Rubi 4.16.1 (Dec 19, 2018) on Mathematica 13.0.1 on windows 10.
3. Maple 2022.1 (June 1, 2022) on windows 10.
4. Maxima 5.46 (April 13, 2022) using Lisp SBCL 2.1.11.debian on Linux via sagemath 9.6.
5. Fricas 1.3.8 (June 21, 2022) based on sbcl 2.1.11.debian on Linux via sagemath 9.6.
6. Giac/Xcas 1.9.0-13 (July 3, 2022) on Linux via sagemath 9.6.
7. Sympy 1.10.1 (March 20, 2022) Using Python 3.10.4 on Linux.
8. Mupad using Matlab 2021a with Symbolic Math Toolbox Version 8.7 on windows 10.

Maxima and Fricas and Giac are called using Sagemath. This was done using Sagemath `integrate` command by changing the name of the algorithm to use the different CAS systems.

Sympy was called directly from Python.

## 1.2 Results

Important note: A number of problems in this test suite have no antiderivative in closed form. This means the antiderivative of these integrals can not be expressed in terms of elementary, special functions or `Hypergeometric2F1` functions. `RootSum` and `RootOf` are not allowed.

If a CAS returns the above integral unevaluated within the time limit, then the result is counted as passed and assigned an A grade.

However, if CAS times out, then it is assigned an F grade even if the integral is not integrable, as this implies CAS could not determine that the integral is not integrable in the time limit.

If a CAS returns an antiderivative to such an integral, it is assigned an A grade automatically and this special result is listed in the introduction section of each individual test report to make it easy to identify as this can be important result to investigate.

The results given in in the table below reflects the above.

System	% solved	% Failed
Rubi	100.00 ( 46 )	0.00 ( 0 )
Mathematica	100.00 ( 46 )	0.00 ( 0 )
Sympy	43.48 ( 20 )	56.52 ( 26 )
Fricas	26.09 ( 12 )	73.91 ( 34 )
Maple	26.09 ( 12 )	73.91 ( 34 )
Mupad	26.09 ( 12 )	73.91 ( 34 )
Giac	26.09 ( 12 )	73.91 ( 34 )
Maxima	26.09 ( 12 )	73.91 ( 34 )

Table 1.1: Percentage solved for each CAS

The table below gives additional break down of the grading of quality of the antiderivatives generated by each CAS. The grading is given using the letters A,B,C and F with A being the best quality. The grading is accomplished by comparing the antiderivative generated with the optimal antiderivatives included in the test suite. The following table describes the meaning of these grades.

grade	description
A	Integral was solved and antiderivative is optimal in quality and leaf size.
B	Integral was solved and antiderivative is optimal in quality but leaf size is larger than twice the optimal antiderivatives leaf size.
C	Integral was solved and antiderivative is non-optimal in quality. This can be due to one or more of the following reasons <ol style="list-style-type: none"> <li>1. antiderivative contains a hypergeometric function and the optimal antiderivative does not.</li> <li>2. antiderivative contains a special function and the optimal antiderivative does not.</li> <li>3. antiderivative contains the imaginary unit and the optimal antiderivative does not.</li> </ol>
F	Integral was not solved. Either the integral was returned unevaluated within the time limit, or it timed out, or CAS hanged or crashed or an exception was raised.

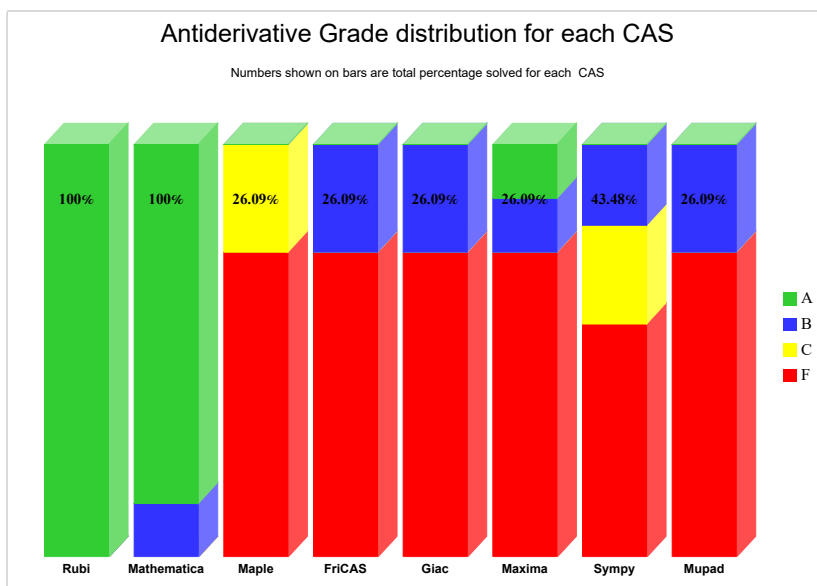
Table 1.2: Description of grading applied to integration result

Grading is implemented for all CAS systems. Based on the above, the following table summarizes the grading for this test suite.

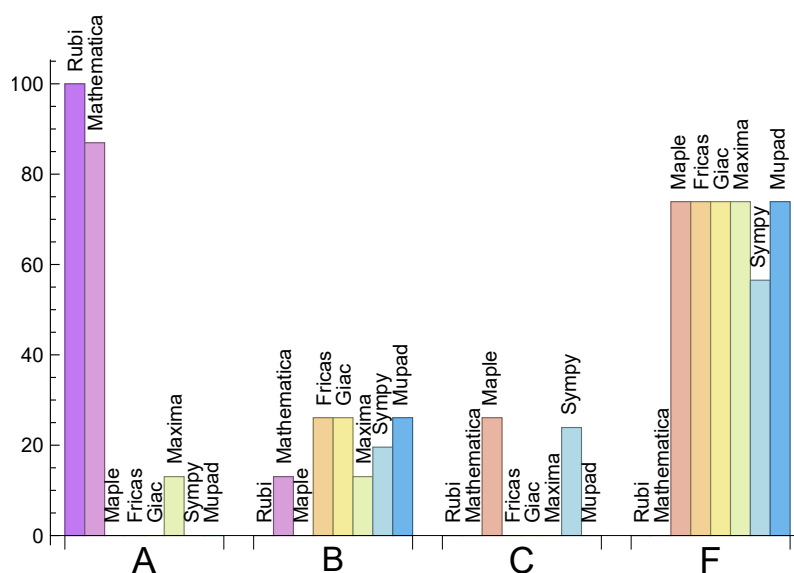
System	% A grade	% B grade	% C grade	% F grade
Rubi	100.00	0.00	0.00	0.00
Mathematica	86.96	13.04	0.00	0.00
Maxima	13.04	13.04	0.00	73.91
Fricas	0.00	26.09	0.00	73.91
Maple	0.00	0.00	26.09	73.91
Mupad	N/A	26.09	0.00	73.91
Giac	0.00	26.09	0.00	73.91
Sympy	0.00	19.57	23.91	56.52

Table 1.3: Antiderivative Grade distribution of each CAS

The following is a Bar chart illustration of the data in the above table.



The figure below compares the CAS systems for each grade level.



The following table shows the distribution of the different types of failure for each CAS. There are 3 types of reasons why it can fail. The first is when CAS returns back the input within the time limit, which means it could not solve it. This is the typical normal failure **F**.

The second is due to time out. CAS could not solve the integral within the 3 minutes time limit which is assigned **F(-1)**.

The third is due to an exception generated. Assigned **F(-2)**. This most likely indicates an interface problem between sagemath and the CAS (applicable only to FriCAS, Maxima and

Giac) or it could be an indication of an internal error in CAS. This type of error requires more investigations to determine the cause.

System	Number failed	Percentage normal failure	Percentage time-out failure	Percentage exception failure
Rubi	0	0.00 %	0.00 %	0.00 %
Mathematica	0	0.00 %	0.00 %	0.00 %
Maple	34	100.00 %	0.00 %	0.00 %
Fricas	34	100.00 %	0.00 %	0.00 %
Giac	34	100.00 %	0.00 %	0.00 %
Maxima	34	100.00 %	0.00 %	0.00 %
Sympy	26	7.69 %	50.00 %	42.31 %
Mupad	34	100.00 %	0.00 %	0.00 %

Table 1.4: Failure statistics for each CAS



## 1.3 Time and leaf size Performance

The table below summarizes the performance of each CAS system in terms of time used and leaf size of results.

Mean size is the average leaf size produced by the CAS (before any normalization). The Normalized mean is relative to the mean size of the optimal anti-derivative given in the input files.

For example, if CAS has **Normalized mean** of 3, then the mean size of its leaf size is 3 times as large as the mean size of the optimal leaf size.

Median size is value of leaf size where half the values are larger than this and half are smaller (before any normalization). i.e. The Middle value.

Similarly the **Normalized median** is relative to the median leaf size of the optimal.

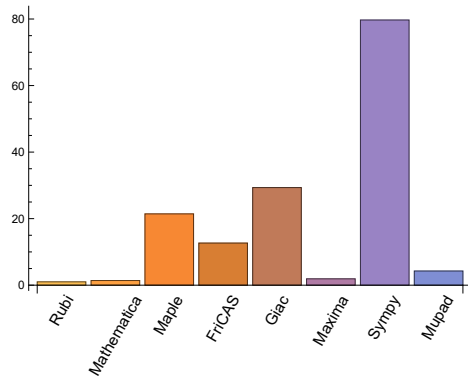
For example, if a CAS has Normalized median of 1.2, then its median is 1.2 as large as the median leaf size of the optimal.

System	Mean time (sec)	Mean size	Normalized mean	Median size	Normalized median
Rubi	0.31	237.96	1.00	211.50	1.00
Mathematica	0.65	389.78	1.40	177.00	0.84
Maple	0.37	5656.75	21.43	3691.00	19.37
Maxima	0.36	415.75	1.91	372.00	2.00
Fricas	1.99	3281.17	12.66	2162.00	11.42
Sympy	54.45	14915.60	79.70	3025.00	22.95
Giac	1.48	7684.42	29.34	5171.00	27.16
Mupad	5.65	993.92	4.26	838.50	4.42

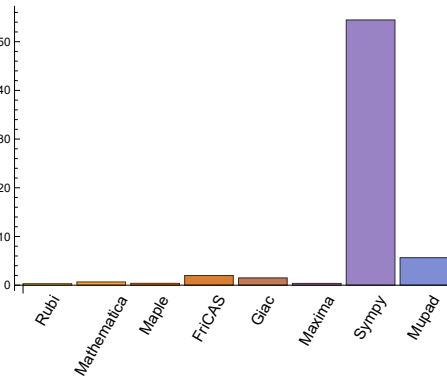
Table 1.5: Time and leaf size performance for each CAS

The following are bar charts for the normalized leafsize and time used from the above table.

**Normalized mean size of antiderivative**  
Lower is better



**Mean time used (seconds)**  
Lower is better



## 1.4 list of integrals that has no closed form antiderivative

{

## 1.5 List of integrals solved by CAS but has no known antiderivative

Rubi {}

Mathematica {}

Maple {}

Maxima {}

Fricas {}

Sympy {}

Giac {}

Mupad {}

## 1.6 list of integrals solved by CAS but failed verification

The following are integrals solved by CAS but the verification phase failed to verify the anti-derivative produced is correct. This does not mean necessarily that the anti-derivative is wrong, as additional methods of verification might be needed, or more time is needed (3 minutes time limit was used). These integrals are listed here to make it easier to do further investigation to determine why it was not possible to verify the result produced.

**Rubi** {}

**Mathematica** {}

**Maple** Verification phase not implemented yet.

**Maxima** Verification phase not implemented yet.

**Fricas** Verification phase not implemented yet.

**Sympy** Verification phase not implemented yet.

**Giac** Verification phase not implemented yet.

**Mupad** Verification phase not implemented yet.

## 1.7 Timing

The command `AbsoluteTiming[]` was used in Mathematica to obtain the elapsed time for each integrate call. In Maple, the command `Usage` was used as in the following example

```
cpu_time := Usage(assign ('result_of_int',int(expr,x)),output='realtime')
```

For all other CAS systems, the elapsed time to complete each integral was found by taking the difference between the time after the call completed from the time before the call was made. This was done using Python's `time.time()` call.

All elapsed times shown are in seconds. A time limit of 3 CPU minutes was used for each integral. If the integrate command did not complete within this time limit, the integral was aborted and considered to have failed and assigned an F grade. The time used by failed integrals due to time out was not counted in the final statistics.

## 1.8 Verification

A verification phase was applied on the result of integration for `Rubi` and `Mathematica`.

Future version of this report will implement verification for the other CAS systems. For the integrals whose result was not run through a verification phase, it is assumed that the antiderivative was correct.

Verification phase also had 3 minutes time out. An integral whose result was not verified could still be correct, but further investigation is needed on those integrals. These integrals were marked in the summary table below and also in each integral separate section so they are easy to identify and locate.

## 1.9 Important notes about some of the results

### 1.9.1 Important note about Maxima results

Since tests were run in a batch mode, and using an automated script, then any integral where Maxima needed an interactive response from the user to answer a question during the evaluation of the integral will fail.

The exception raised is `ValueError`. Therefore Maxima results is lower than what would result if Maxima was run directly and each question was answered correctly.

The percentage of such failures were not counted for each test file, but for an example, for the `Timofeev` test file, there were about 14 such integrals out of total 705, or about 2 percent. This percentage can be higher or lower depending on the specific input test file.

Such integrals can be identified by looking at the output of the integration in each section for Maxima. The exception message will indicate the cause of error.

Maxima `integrate` was run using SageMath with the following settings set by default

```
'besselexpand : true'
'display2d : false'
'domain : complex'
'keepfloat : true'
'load(to_poly_solve)'
'load(simplify_sum)'
'load(abs_integrate)' 'load(diag)'
```

SageMath automatic loading of Maxima `abs_integrate` was found to cause some problems. So the following code was added to disable this effect.

```
from sage.interfaces.maxima_lib import maxima_lib
maxima_lib.set('extra_definite_integration_methods', '[]')
```

```
maxima_lib.set('extra_integration_methods', '[]')
```

See <https://ask.sagemath.org/question/43088/integrate-results-that-are-different-from-using-maxima/> for reference.

### 1.9.2 Important note about FriCAS result

There were few integrals which failed due to SageMath interface and not because FriCAS system could not do the integration.

These will fail With error `Exception raised: NotImplementedError`.

The number of such cases seems to be very small. About 1 or 2 percent of all integrals. These can be identified by looking at the exception message given in the result.

### 1.9.3 Important note about finding leaf size of antiderivative

For Mathematica, Rubi, and Maple, the builtin system function `LeafSize` was used to find the leaf size of each antiderivative.

The other CAS systems (SageMath and Sympy) do not have special builtin function for this purpose at this time. Therefore the leaf size for Fricas and Sympy antiderivative was determined using the following function, thanks to user `slelievre` at [https://ask.sagemath.org/question/57123/could-we-have-a-leaf\\_count-function-in-base-sagemath/](https://ask.sagemath.org/question/57123/could-we-have-a-leaf_count-function-in-base-sagemath/)

```
def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)
```

For Sympy, which was called directly from Python, the following code was used to obtain the leafsize of its result

```
try:
    # 1.7 is a fudge factor since it is low side from actual leaf count
    leafCount = round(1.7*count_ops(anti))

except Exception as ee:
    leafCount =1
```

### 1.9.4 Important note about Mupad results

Matlab's symbolic toolbox does not have a leaf count function to measure the size of the antiderivative. Maple was used to determine the leaf size of Mupad output by post processing Mupad result.

Currently no grading of the antiderivative for Mupad is implemented. If it can integrate the problem, it was assigned a B grade automatically as a placeholder. In the future, when grading function is implemented for Mupad, the tests will be rerun again.

The following is an example of using Matlab's symbolic toolbox (Mupad) to solve an integral

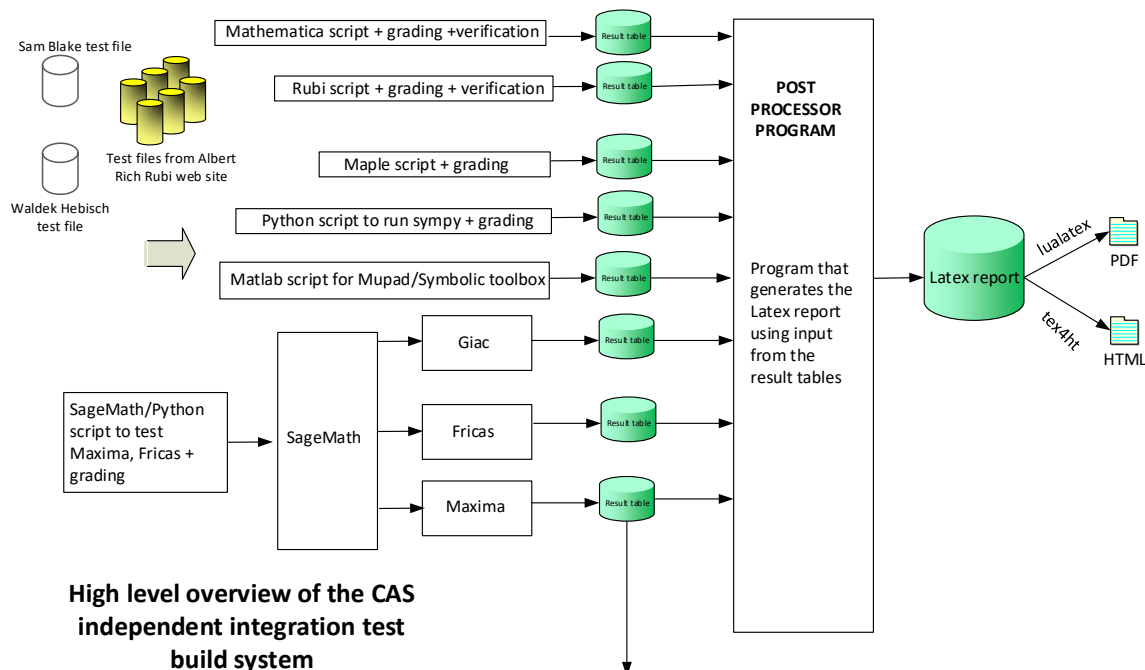
```
integrand = evalin(symengine, 'cos(x)*sin(x)')
the_variable = evalin(symengine, 'x')
anti = int(integrand,the_variable)
```

Which gives  $\sin(x)^2/2$



## 1.10 Design of the test system

The following diagram gives a high level view of the current test build system.



One record (line) per one integral result. The line is CSV comma separated. This is description of each record

1. integer, the problem number.
2. integer. 0 for failed, 1 for passed, -1 for timeout, -2 for CAS specific exception. (this is not the grade field)
3. integer. Leaf size of result.
4. integer. Leaf size of the optimal antiderivative.
5. number. CPU time used to solve this integral. 0 if failed.
6. string. The integral in Latex format
7. string. The input used in CAS own syntax.
8. string. The result (antiderivative) produced by CAS in Latex format
9. string. The optimal antiderivative in Latex format.
10. integer. 0 or 1. Indicates if problem has known antiderivative or not
11. String. The result (antiderivative) in CAS own syntax.
12. String. The grade of the antiderivative. Can be "A", "B", "C", or "F"
13. String. Small string description of why the grade was given.
14. integer. 1 if result was verified or 0 if not verified.

*The following fields are present only in Rubi Table file*

15. integer. Number of steps used.
16. integer. Number of rules used.
17. integer. Integrand leaf size.
18. real number. Ratio. Field 16 over field 17
19. String of form "{n,n,..}" which is list of the rules used by Rubi
20. String. The optimal antiderivative in Mathematica syntax



# Chapter 2

## detailed summary tables of results

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## 2.1 List of integrals sorted by grade for each CAS

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### 2.1.1 Rubi

A grade: { 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46 }

B grade: { }

C grade: { }

F grade: { }

### 2.1.2 Mathematica

A grade: { 1, 2, 3, 4, 5, 6, 8, 9, 10, 11, 12, 13, 15, 16, 17, 18, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 38, 39, 41, 42, 43, 44, 45, 46 }

B grade: { 7, 14, 35, 36, 37, 40 }

C grade: { }

F grade: { }

### 2.1.3 Maple

A grade: { }

B grade: { }

C grade: { 1, 2, 3, 4, 8, 9, 10, 11, 15, 16, 17, 18 }

F grade: { 5, 6, 7, 12, 13, 14, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46 }

### 2.1.4 Maxima

A grade: { 2, 3, 4, 10, 11, 18 }

B grade: { 1, 8, 9, 15, 16, 17 }

C grade: { }

F grade: { 5, 6, 7, 12, 13, 14, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46 }

### 2.1.5 FriCAS

A grade: { }

B grade: { 1, 2, 3, 4, 8, 9, 10, 11, 15, 16, 17, 18 }

C grade: { }

F grade: { 5, 6, 7, 12, 13, 14, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46 }

### 2.1.6 Sympy

A grade: { }

B grade: { 1, 2, 3, 4, 9, 10, 11, 17, 18 }

C grade: { 5, 6, 12, 19, 21, 22, 23, 24, 25, 31, 32 }

F grade: { 7, 8, 13, 14, 15, 16, 20, 26, 27, 28, 29, 30, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46 }

### 2.1.7 Giac

A grade: { }

B grade: { 1, 2, 3, 4, 8, 9, 10, 11, 15, 16, 17, 18 }

C grade: { }

F grade: { 5, 6, 7, 12, 13, 14, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46 }

### 2.1.8 Mupad

A grade: { }

B grade: { 1, 2, 3, 4, 8, 9, 10, 11, 15, 16, 17, 18 }

C grade: { }

F grade: { 5, 6, 7, 12, 13, 14, 19, 20, 21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37, 38, 39, 40, 41, 42, 43, 44, 45, 46 }

## 2.2 Detailed conclusion table per each integral for all CAS systems

Detailed conclusion table per each integral is given by table below. The elapsed time is in seconds. For failed result it is given as F(-1) if the failure was due to timeout. It is given as F(-2) if the failure was due to an exception being raised, which could indicate a bug in the system. If the failure was due to integral not being evaluated within the time limit, then it is given just an F.

In this table, the column N.S. in the table below, which stands for **normalized size** is defined as  $\frac{\text{antiderivative leaf size}}{\text{optimal antiderivative leaf size}}$ . To help make the table fit, **Mathematica** was abbrevi-

	Problem 1	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
viated to <b>MMA</b> .	grade	A	A	A	C	B	B	B	B	B
	verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
	size	210	210	172	4972	434	3055	63250	6927	1089
	N.S.	1	1.00	0.82	23.68	2.07	14.55	301.19	32.99	5.19
	time (sec)	N/A	0.182	0.685	0.399	0.343	3.748	175.912	0.677	5.644

Problem 2	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	160	160	129	2410	310	1509	24932	3415	588
N.S.	1	1.00	0.81	15.06	1.94	9.43	155.82	21.34	3.68
time (sec)	N/A	0.111	0.322	0.379	0.337	2.331	88.119	1.351	5.231

Problem 3	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	108	108	84	891	186	550	7686	1290	271
N.S.	1	1.00	0.78	8.25	1.72	5.09	71.17	11.94	2.51
time (sec)	N/A	0.056	0.137	0.081	0.322	2.002	39.423	0.802	4.958

Problem 4	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	66	66	49	262	85	176	1499	327	91
N.S.	1	1.00	0.74	3.97	1.29	2.67	22.71	4.95	1.38
time (sec)	N/A	0.027	0.062	0.057	0.310	1.209	13.538	2.278	4.830

Problem 5	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	120	120	115	0	0	0	666	0	-1
N.S.	1	1.00	0.96	0.00	0.00	0.00	5.55	0.00	-0.01
time (sec)	N/A	0.077	0.175	0.065	0.000	0.000	5.669	0.000	0.000

Problem 6	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	177	177	195	0	0	0	4129	0	-1
N.S.	1	1.00	1.10	0.00	0.00	0.00	23.33	0.00	-0.01
time (sec)	N/A	0.161	0.255	0.066	0.000	0.000	31.570	0.000	0.000

Problem 7	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	228	227	1153	0	0	0	0	0	-1
N.S.	1	1.00	5.06	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.190	0.568	0.068	0.000	0.000	0.000	0.000	0.000

Problem 8	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	318	318	273	11389	702	6617	0	15358	1882
N.S.	1	1.00	0.86	35.81	2.21	20.81	0.00	48.30	5.92
time (sec)	N/A	0.277	1.340	0.499	0.378	1.171	0.000	1.723	6.348



Problem 9	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	237	237	199	5908	506	3497	71580	8103	1119
N.S.	1	1.00	0.84	24.93	2.14	14.76	302.03	34.19	4.72
time (sec)	N/A	0.204	0.599	0.428	0.355	2.392	189.292	1.976	5.591

Problem 10	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	160	160	129	2410	310	1411	24932	3415	588
N.S.	1	1.00	0.81	15.06	1.94	8.82	155.82	21.34	3.68
time (sec)	N/A	0.116	0.337	0.379	0.375	1.806	88.963	0.901	5.196

Problem 11	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	102	102	78	732	145	515	5794	1023	265
N.S.	1	1.00	0.76	7.18	1.42	5.05	56.80	10.03	2.60
time (sec)	N/A	0.052	0.111	0.356	0.321	3.532	35.264	1.448	5.113

Problem 12	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	185	185	156	0	0	0	1085	0	-1
N.S.	1	1.00	0.84	0.00	0.00	0.00	5.86	0.00	-0.01
time (sec)	N/A	0.152	0.315	0.079	0.000	0.000	11.794	0.000	0.000

Problem 13	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	268	268	227	0	0	0	0	0	-1
N.S.	1	1.00	0.85	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.445	0.874	0.081	0.000	0.000	0.000	0.000	0.000

Problem 14	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	322	322	1924	0	0	0	0	0	-1
N.S.	1	1.00	5.98	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.357	1.055	0.079	0.000	0.000	0.000	0.000	0.000

Problem 15	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	410	410	358	20937	970	11604	0	27792	2500
N.S.	1	1.00	0.87	51.07	2.37	28.30	0.00	67.79	6.10
time (sec)	N/A	0.414	1.531	0.587	0.458	1.452	0.000	1.925	7.495

Problem 16	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	B	B	F(-1)	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	310	310	265	11389	702	6536	0	15358	1882
N.S.	1	1.00	0.85	36.74	2.26	21.08	0.00	49.54	6.07
time (sec)	N/A	0.281	1.360	0.505	0.430	1.843	0.000	1.810	6.414

Problem 17	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	B	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	210	210	172	4972	434	2815	63250	6927	1089
N.S.	1	1.00	0.82	23.68	2.07	13.40	301.19	32.99	5.19
time (sec)	N/A	0.172	0.612	0.415	0.356	1.332	180.149	0.989	5.653

Problem 18	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	C	A	B	B	B	B
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	137	137	106	1609	205	1089	16521	2278	563
N.S.	1	1.00	0.77	11.74	1.50	7.95	120.59	16.63	4.11
time (sec)	N/A	0.078	0.147	0.356	0.351	1.004	76.544	1.886	5.307

Problem 19	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	270	270	212	0	0	0	1503	0	-1
N.S.	1	1.00	0.79	0.00	0.00	0.00	5.57	0.00	-0.00
time (sec)	N/A	0.258	0.587	0.102	0.000	0.000	23.381	0.000	0.000

Problem 20	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	394	389	345	0	0	0	0	0	-1
N.S.	1	0.99	0.88	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.657	2.184	0.079	0.000	0.000	0.000	0.000	0.000

Problem 21	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	380	380	290	0	0	0	1921	0	-1
N.S.	1	1.00	0.76	0.00	0.00	0.00	5.06	0.00	-0.00
time (sec)	N/A	0.415	1.104	0.082	0.000	0.000	44.642	0.000	0.000

Problem 22	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	272	272	213	0	0	0	1503	0	-1
N.S.	1	1.00	0.78	0.00	0.00	0.00	5.53	0.00	-0.00
time (sec)	N/A	0.268	0.624	0.075	0.000	0.000	23.443	0.000	0.000

Problem 23	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	187	187	156	0	0	0	1085	0	-1
N.S.	1	1.00	0.83	0.00	0.00	0.00	5.80	0.00	-0.01
time (sec)	N/A	0.172	0.334	0.079	0.000	0.000	12.162	0.000	0.000

Problem 24	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	122	122	115	0	0	0	666	0	-1
N.S.	1	1.00	0.94	0.00	0.00	0.00	5.46	0.00	-0.01
time (sec)	N/A	0.087	0.182	0.068	0.000	0.000	6.245	0.000	0.000

Problem 25	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	78	78	59	0	0	0	284	0	-1
N.S.	1	1.00	0.76	0.00	0.00	0.00	3.64	0.00	-0.01
time (sec)	N/A	0.027	0.086	0.094	0.000	0.000	1.998	0.000	0.000

Problem 26	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	127	127	102	0	0	0	0	0	-1
N.S.	1	1.00	0.80	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.092	0.190	0.122	0.000	0.000	0.000	0.000	0.000

Problem 27	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	212	212	177	0	0	0	0	0	-1
N.S.	1	1.00	0.83	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.354	0.361	0.112	0.000	0.000	0.000	0.000	0.000

Problem 28	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	407	407	402	0	0	0	0	0	-1
N.S.	1	1.00	0.99	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.812	1.215	0.115	0.000	0.000	0.000	0.000	0.000

Problem 29	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	386	381	365	0	0	0	0	0	-1
N.S.	1	0.99	0.95	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.737	1.956	0.085	0.000	0.000	0.000	0.000	0.000

Problem 30	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	267	267	249	0	0	0	0	0	-1
N.S.	1	1.00	0.93	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.448	0.823	0.079	0.000	0.000	0.000	0.000	0.000

Problem 31	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	178	178	193	0	0	0	4129	0	-1
N.S.	1	1.00	1.08	0.00	0.00	0.00	23.20	0.00	-0.01
time (sec)	N/A	0.169	0.289	0.061	0.000	0.000	31.125	0.000	0.000

Problem 32	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	C	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	107	107	84	0	0	0	1897	0	-1
N.S.	1	1.00	0.79	0.00	0.00	0.00	17.73	0.00	-0.01
time (sec)	N/A	0.038	0.136	0.061	0.000	0.000	9.761	0.000	0.000

Problem 33	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	211	211	177	0	0	0	0	0	-1
N.S.	1	1.00	0.84	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.349	0.357	0.117	0.000	0.000	0.000	0.000	0.000

Problem 34	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	315	315	242	0	0	0	0	0	-1
N.S.	1	1.00	0.77	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.717	0.736	0.146	0.000	0.000	0.000	0.000	0.000

Problem 35	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	567	567	2176	0	0	0	0	0	-1
N.S.	1	1.00	3.84	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.561	1.875	0.113	0.000	0.000	0.000	0.000	0.000

Problem 36	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	322	322	1924	0	0	0	0	0	-1
N.S.	1	1.00	5.98	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.367	1.138	0.080	0.000	0.000	0.000	0.000	0.000

Problem 37	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	228	227	1153	0	0	0	0	0	-1
N.S.	1	1.00	5.06	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.189	0.591	0.069	0.000	0.000	0.000	0.000	0.000

Problem 38	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	112	112	127	0	0	0	0	0	-1
N.S.	1	1.00	1.13	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.036	0.178	0.063	0.000	0.000	0.000	0.000	0.000

Problem 39	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	366	366	357	0	0	0	0	0	-1
N.S.	1	1.00	0.98	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.801	1.245	0.111	0.000	0.000	0.000	0.000	0.000

Problem 40	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	B	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	482	482	2178	0	0	0	0	0	-1
N.S.	1	1.00	4.52	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	1.356	1.850	0.115	0.000	0.000	0.000	0.000	0.000

Problem 41	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	211	211	162	0	0	0	0	0	-1
N.S.	1	1.00	0.77	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.163	0.312	0.329	0.000	0.000	0.000	0.000	0.000

Problem 42	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	271	255	164	0	0	0	0	0	-1
N.S.	1	0.94	0.61	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.414	0.397	0.089	0.000	0.000	0.000	0.000	0.000

Problem 43	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	164	164	138	0	0	0	0	0	-1
N.S.	1	1.00	0.84	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.117	0.196	0.147	0.000	0.000	0.000	0.000	0.000

Problem 44	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-2)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	304	304	138	0	0	0	0	0	-1
N.S.	1	1.00	0.45	0.00	0.00	0.00	0.00	0.00	-0.00
time (sec)	N/A	0.353	0.269	0.136	0.000	0.000	0.000	0.000	0.000

Problem 45	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	139	139	124	0	0	0	0	0	-1
N.S.	1	1.00	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.073	0.328	0.157	0.000	0.000	0.000	0.000	0.000

Problem 46	Optimal	Rubi	MMA	Maple	Maxima	Fricas	Sympy	Giac	Mupad
grade	A	A	A	F	F	F	F(-1)	F	F
verified	N/A	Yes	Yes	TBD	TBD	TBD	TBD	TBD	TBD
size	139	167	124	0	0	0	0	0	-1
N.S.	1	1.20	0.89	0.00	0.00	0.00	0.00	0.00	-0.01
time (sec)	N/A	0.078	0.070	0.147	0.000	0.000	0.000	0.000	0.000



## 2.3 Detailed conclusion table specific for Rubi results

The following table is specific to Rubi. It gives additional statistics for each integral. the column **steps** is the number of steps used by Rubi to obtain the antiderivative. The **rules** column is the number of unique rules used. The **integrand size** column is the leaf size of the integrand. Finally the ratio  $\frac{\text{number of rules}}{\text{integrand size}}$  is given. The larger this ratio is, the harder the integral was to solve. In this test, problem number [46] had the largest ratio of [55]

Table 2.1: Rubi specific breakdown of results for each integral

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
1	A	12	3	1.00	29	0.103
2	A	10	3	1.00	29	0.103
3	A	8	3	1.00	27	0.111
4	A	6	3	1.00	20	0.150
5	A	5	4	1.00	29	0.138
6	A	3	3	1.00	29	0.103
7	A	3	3	1.00	29	0.103
8	A	14	3	1.00	31	0.097
9	A	12	3	1.00	31	0.097
10	A	10	3	1.00	29	0.103
11	A	8	3	1.00	22	0.136
12	A	7	4	1.00	31	0.129
13	A	6	5	1.00	31	0.161
14	A	4	3	1.00	31	0.097
15	A	16	3	1.00	31	0.097
16	A	14	3	1.00	31	0.097
17	A	12	3	1.00	29	0.103
18	A	10	3	1.00	22	0.136
19	A	9	4	1.00	31	0.129
20	A	8	5	0.99	31	0.161
21	A	11	4	1.00	31	0.129
22	A	9	4	1.00	31	0.129
23	A	7	4	1.00	31	0.129
24	A	5	4	1.00	29	0.138
25	A	2	2	1.00	22	0.091

Continued on next page

Table 2.1 – continued from previous page

#	grade	number of steps used	number of unique rules	normalized antiderivative leaf size	integrand leaf size	$\frac{\text{number of rules}}{\text{integrand leaf size}}$
26	A	4	2	1.00	31	0.065
27	A	5	3	1.00	31	0.097
28	A	6	3	1.00	31	0.097
29	A	8	5	0.99	31	0.161
30	A	6	5	1.00	31	0.161
31	A	3	3	1.00	29	0.103
32	A	2	2	1.00	22	0.091
33	A	5	3	1.00	31	0.097
34	A	6	3	1.00	31	0.097
35	A	7	3	1.00	31	0.097
36	A	4	3	1.00	31	0.097
37	A	3	3	1.00	29	0.103
38	A	2	2	1.00	22	0.091
39	A	6	3	1.00	31	0.097
40	A	7	3	1.00	31	0.097
41	A	7	3	1.00	31	0.097
42	A	4	4	0.94	29	0.138
43	A	6	5	1.00	31	0.161
44	A	7	6	1.00	31	0.194
45	A	4	4	1.00	47	0.085
46	A	4	4	1.20	55	0.073

# Chapter 3

## Listing of integrals

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### 3.1 $\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=210

$$\frac{a^2(3Abc + aBc + aAd)x^{1+n}(ex)^m}{1 + m + n} + \frac{a(3Ab(bc + ad) + aB(3bc + ad))x^{1+2n}(ex)^m}{1 + m + 2n} + \frac{b(3aB(bc + ad) + Ab(bc + ad))x^{1+3n}(ex)^m}{1 + m + 3n} + \frac{b^2(3aB^2(bc + ad) + Ab^2(3bc + ad))x^{1+4n}(ex)^m}{1 + m + 4n} + \frac{b^3(3aB^3(bc + ad) + Ab^3(3bc + ad))x^{1+5n}(ex)^m}{1 + m + 5n} + \frac{a^3A^2c^2(ex)^{m+1}}{e(m+1)}$$

[Out]  $a^2*(A*a*d+3*A*b*c+B*a*c)*x^{(1+n)}*(e*x)^m/(1+m+n)+a*(3*A*b*(a*d+b*c)+a*B*(a*d+3*b*c))*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+b*(3*a*B*(a*d+b*c)+A*b*(3*a*d+b*c))*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+b^2*(A*b*d+3*B*a*d+B*b*c)*x^{(1+4*n)}*(e*x)^m/(1+m+4*n)+b^3*B*d*x^{(1+5*n)}*(e*x)^m/(1+m+5*n)+a^3*A*c*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.18, antiderivative size = 210, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ ,

Rules used = {584, 20, 30}

$$\frac{a^3Ac(ex)^{m+1}}{e(m+1)} + \frac{a^2x^{n+1}(ex)^m(aAd+aBc+3Abc)}{m+n+1} + \frac{b^2x^{4n+1}(ex)^m(3aBd+Abd+bBc)}{m+4n+1} + \frac{ax^{2n+1}(ex)^m(3Ab(ad+bc)+aB(ad+3bc))}{m+2n+1} + \frac{bx^{3n+1}(ex)^m(Ab(3ad+bc)+3aB(ad+bc))}{m+3n+1} + \frac{b^3Bdx^{5n+1}(ex)^m}{m+5n+1}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(a + b*x^n)^3*(A + B*x^n)*(c + d*x^n), x]$

[Out]  $(a^2*(3*A*b*c + a*B*c + a*A*d)*x^{(1 + n)}*(e*x)^m/(1 + m + n) + (a*(3*A*b*(b*c + a*d) + a*B*(3*b*c + a*d))*x^{(1 + 2*n)}*(e*x)^m/(1 + m + 2*n) + (b*(3*a*B*(b*c + a*d) + A*b*(b*c + 3*a*d))*x^{(1 + 3*n)}*(e*x)^m/(1 + m + 3*n) + (b^2*(b*B*c + A*b*d + 3*a*B*d)*x^{(1 + 4*n)}*(e*x)^m/(1 + m + 4*n) + (b^3*B*d*x^{(1 + 5*n)}*(e*x)^m/(1 + m + 5*n) + (a^3*A*c*(e*x)^{(1 + m)})/(e*(1 + m)))$

**Rule 20**

$\text{Int}[(u_.)*((a_.)*(v_))^{(m_.)}*((b_.)*(v_))^{(n_.)}, x\_Symbol] := \text{Dist}[b^{\text{IntPart}[n]}*((b*v)^{\text{FracPart}[n]}/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]})), \text{Int}[u*(a*v)^{(m+n)}, x], x] /;$  FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

**Rule 30**

$\text{Int}[(x_)^{(m_.)}, x\_Symbol] := \text{Simp}[x^{(m+1)}/(m+1), x] /;$  FreeQ[m, x] && N eQ[m, -1]

**Rule 584**

$\text{Int}[((g_.)*(x_))^{(m_.)}*((a_.) + (b_.)*(x_)^{(n_.)})^{(p_.)}*((c_.) + (d_.)*(x_)^{(n_.)})^{(q_.)}*((e_.) + (f_.)*(x_)^{(n_.)})^{(r_.)}, x\_Symbol] := \text{Int}[\text{ExpandIntegrand}[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /;$  FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

Rubi steps

$$\begin{aligned}
\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n) dx &= \int (a^3 Ac(ex)^m + a^2(3Abc + aBc + aAd)x^n(ex)^m + a(3Ab(bc + ad) + aB(3b^2c + Abd + 3aBd))x^{2n} \\
&= \frac{a^3 Ac(ex)^{1+m}}{e(1+m)} + (b^3 Bd) \int x^{5n}(ex)^m dx + (a^2(3Abc + aBc + aAd)x^n(ex)^m) \int x^{m+5n} dx + (a(3Ab(bc + ad) + aB(3b^2c + Abd + 3aBd))x^{2n}(ex)^m) \int x^{m+5n} dx \\
&= \frac{a^3 Ac(ex)^{1+m}}{e(1+m)} + (b^3 Bdx^{-m}(ex)^m) \int x^{m+5n} dx + (a^2(3Abc + aBc + aAd)x^{1+n}(ex)^m) \int x^{m+5n} dx + (a(3Ab(bc + ad) + aB(3b^2c + Abd + 3aBd))x^{1+n}(ex)^m) \int x^{m+5n} dx \\
&= \frac{a^3 Ac(ex)^{1+m}}{e(1+m)} + \frac{a^2(3Abc + aBc + aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{a(3Ab(bc + ad) + aB(3b^2c + Abd + 3aBd))x^{1+n}(ex)^m}{1+m+n}
\end{aligned}$$

Mathematica [A]

time = 0.69, size = 172, normalized size = 0.82

$$x(ex)^m \left( \frac{a^3 Ac}{1+m} + \frac{a^2(3Abc + aBc + aAd)x^n}{1+m+n} + \frac{a(3Ab(bc + ad) + aB(3b^2c + Abd + 3aBd))x^{2n}}{1+m+2n} + \frac{b(3aB(bc + ad) + Ab(bc + 3ad))x^{3n}}{1+m+3n} + \frac{b^2(bBc + Abd + 3aBd)x^{4n}}{1+m+4n} + \frac{b^3 Bdx^{5n}}{1+m+5n} \right)$$

Antiderivative was successfully verified.

`[In] Integrate[(e*x)^m*(a + b*x^n)^3*(A + B*x^n)*(c + d*x^n), x]`

```
[Out] x*(e*x)^m*((a^3*A*c)/(1 + m) + (a^2*(3*A*b*c + a*B*c + a*A*d)*x^n)/(1 + m + n) + (a*(3*A*b*(b*c + a*d) + a*B*(3*b*c + a*d))*x^(2*n))/(1 + m + 2*n) + (b*(3*a*B*(b*c + a*d) + A*b*(b*c + 3*a*d))*x^(3*n))/(1 + m + 3*n) + (b^2*(b*B*c + A*b*d + 3*a*B*d)*x^(4*n))/(1 + m + 4*n) + (b^3*B*d*x^(5*n))/(1 + m + 5*n))
```

Maple [C] Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.40, size = 4972, normalized size = 23.68

method	result	size
risch	Expression too large to display	4972

Verification of antiderivative is not currently implemented for this CAS.

`[In] int((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n), x, method=_RETURNVERBOSE)`

```
[Out] x*(147*A*a*b^2*d*n^2*(x^n)^3+48*A*b^3*c*m*n*(x^n)^3+56*B*a^3*c*m^3*n*x^n+3*(x^n)^3*B*a*b^2*c+3*(x^n)^2*d*A*a^2*b+B*a^3*c*x^n+105*B*b^3*d*m^2*n^2*(x^n)^5+100*B*b^3*d*m*n^3*(x^n)^5+60*B*a^3*d*m*n^4*(x^n)^2+3*B*a^2*b*c*m^5*(x^n)^2+13*B*a^3*d*m^4*n*(x^n)^2+59*B*a^3*d*m^3*n^2*(x^n)^2+39*A*a*b^2*c*(x^n)^2*n+56*B*a^3*c*m*n*x^n+15*B*a^2*b*c*(x^n)^2+m+30*B*a*b^2*c*m^3*(x^n)^3+234*B*a*b^2*c*n^3*(x^n)^3+30*B*a*b^2*d*m^2*(x^n)^4+234*A*a*b^2*d*m^2*n^3*(x^n)^3+120*A*a*b^2*d*m*n^4*(x^n)^3+36*B*a^2*b*d*m^4*n*(x^n)^3+147*B*a^2*b*d*m^3*n^2*(x^n)^3+234*B*a^2*b*d*m^2*n^3*(x^n)^3+A*a^3*c*m^5+36*B*a*b^2*c*(x^n)^3*n
```

$$\begin{aligned}
& +56*A*a^3*d*m*n*x^n+30*A*a^2*b*c*m^2*x^n+213*A*a^2*b*c*n^2*x^n+15*A*a^2*b*d \\
& *(x^n)^2+m+123*B*a*b^2*d*n^2*(x^n)^4+44*B*b^3*c*m*n*(x^n)^4+56*A*a^3*d*m^3* \\
& n*x^n+213*A*a^3*d*m^2*n^2*x^n+308*A*a^3*d*m*n^3*x^n+A*a^3*c+90*B*a*b^2*d*m* \\
& n^4*(x^n)^4+36*A*a*b^2*d*m^4*n*(x^n)^3+B*a^3*d*(x^n)^2+A*a^3*d*x^n+321*A*a* \\
& b^2*c*n^3*(x^n)^2+30*A*a*b^2*d*m^2*(x^n)^3+120*B*a^2*b*d*m*n^4*(x^n)^3+36*B \\
& *a*b^2*c*m^4*n*(x^n)^3+147*B*a*b^2*c*m^3*n^2*(x^n)^3+10*B*b^3*d*m^4*n*(x^n) \\
& ^5+39*A*a^2*b*d*(x^n)^2+n+30*A*a*b^2*c*m^2*(x^n)^2+15*A*a*b^2*c*(x^n)^2*m+5 \\
& *A*a^3*c*m^4+274*A*a^3*c*n^4+10*A*a^3*c*m^3+225*A*a^3*c*n^3+10*A*a^3*c*m^2+ \\
& 85*A*a^3*c*n^2+B*b^3*c*(x^n)^4+A*b^3*c*(x^n)^3+122*A*b^3*d*m*n^3*(x^n)^4+14 \\
& 7*B*a*b^2*c*n^2*(x^n)^3+15*B*a*b^2*d*(x^n)^4*m+33*B*a*b^2*d*(x^n)^4*n+84*A* \\
& a^3*d*m^2*n*x^n+213*A*a^3*d*m*n^2*x^n+321*A*a^2*b*d*n^3*(x^n)^2+30*A*a*b^2*c \\
& *m^3*(x^n)^2+33*B*a*b^2*d*m^4*n*(x^n)^4+123*B*a*b^2*d*m^3*n^2*(x^n)^4+183* \\
& B*a*b^2*d*m^2*n^3*(x^n)^4+107*B*a^3*d*m^2*n^3*(x^n)^2+120*A*a^3*c*n^5+5*A*a \\
& ^3*c*m+15*A*a^3*c*n+213*B*a^3*c*m^2*n^2*x^n+308*B*a^3*c*m*n^3*x^n+78*B*a^3* \\
& d*m^2*n*(x^n)^2+177*B*a^3*d*m*n^2*(x^n)^2+30*B*a^2*b*c*m^3*(x^n)^2+15*B*a*b \\
& ^2*c*(x^n)^3*m+180*B*a^2*b*c*m*n^4*(x^n)^2+144*B*a^2*b*d*m^3*n*(x^n)^3+441* \\
& B*a^2*b*d*m^2*n^2*(x^n)^3+5*A*b^3*d*(x^n)^4*m+11*A*b^3*d*(x^n)^4*n+5*B*a^3* \\
& c*m^4*x^n+120*B*a^3*c*n^4*x^n+10*B*a^3*d*m^3*(x^n)^2+107*B*a^3*d*n^3*(x^n)^ \\
& 2+5*B*b^3*c*(x^n)^4*m+11*B*b^3*c*(x^n)^4*n+35*B*b^3*d*n^2*(x^n)^5+A*a^3*d*m \\
& ^5*x^n+10*A*b^3*c*m^3*(x^n)^3+78*A*b^3*c*n^3*(x^n)^3+10*A*b^3*d*m^2*(x^n)^4 \\
& +41*A*b^3*d*n^2*(x^n)^4+10*A*a^3*d*m^2*x^n+71*A*a^3*d*n^2*x^n+5*A*b^3*d*m^4 \\
& *(x^n)^4+30*A*b^3*d*n^4*(x^n)^4+5*B*a^3*d*(x^n)^2*m+13*B*a^3*d*(x^n)^2*n+5* \\
& A*a^3*d*x^n*m+14*A*a^3*d*x^n*n+3*(x^n)^2*c*B*a^2*b+3*x^n*c*A*a^2*b+5*B*a^3* \\
& c*x^n*m+B*a^3*c*m^5*x^n+5*B*a^3*d*m^4*(x^n)^2+60*B*a^3*d*n^4*(x^n)^2+10*B*b \\
& ^3*c*m^2*(x^n)^4+41*B*b^3*c*n^2*(x^n)^4+5*m*b^3*B*d*(x^n)^5+3*(x^n)^3*B*a^2 \\
& *b*d+3*(x^n)^2*c*A*a*b^2+B*a^3*d*m^5*(x^n)^2+10*B*b^3*c*m^3*(x^n)^4+61*B*b^ \\
& 3*c*n^3*(x^n)^4+5*B*b^3*c*m^4*(x^n)^4+10*B*a^3*c*m^2*x^n+71*B*a^3*c*n^2*x^n \\
& +10*b^3*B*d*(x^n)^5+n+5*A*a^3*d*m^4*x^n+120*A*a^3*d*n^4*x^n+10*A*b^3*c*m^2* \\
& (x^n)^3+49*A*b^3*c*n^2*(x^n)^3+14*B*a^3*c*x^n*n+154*B*a^3*c*m^2*n^3*x^n+120 \\
& *B*a^3*c*m*n^4*x^n+52*B*a^3*d*m^3*n*(x^n)^2+177*B*a^3*d*m^2*n^2*(x^n)^2+214 \\
& *B*a^3*d*m*n^3*(x^n)^2+321*B*a^2*b*c*n^3*(x^n)^2+30*B*a^2*b*d*m^2*(x^n)^3+1 \\
& 47*B*a^2*b*d*n^2*(x^n)^3+30*B*a*b^2*c*m^2*(x^n)^3+90*B*a*b^2*d*n^4*(x^n)^4+ \\
& 44*B*b^3*c*m^3*n*(x^n)^4+123*B*b^3*c*m^2*n^2*(x^n)^4+122*B*b^3*c*m*n^3*(x^n) \\
& )^4+11*B*b^3*c*m^4*n*(x^n)^4+15*B*a^2*b*c*m^4*(x^n)^2+180*B*a^2*b*c*n^4*(x^n) \\
& ^2+30*B*a^2*b*d*m^3*(x^n)^3+234*B*a^2*b*d*n^3*(x^n)^3+78*A*b^3*c*m^2*n^3* \\
& (x^n)^3+40*A*b^3*c*m*n^4*(x^n)^3+44*A*b^3*d*m^3*n*(x^n)^4+123*A*b^3*d*m^2*n \\
& ^2*(x^n)^4+42*A*a^2*b*c*x^n*n+168*A*a^2*b*c*m^3*n*x^n+639*A*a^2*b*c*m^2*n^2 \\
& *x^n+b^3*B*d*(x^n)^5+A*b^3*d*(x^n)^4+3*B*a^2*b*d*m^5*(x^n)^3+3*B*a*b^2*c*m^ \\
& 5*(x^n)^3+15*B*a*b^2*d*m^4*(x^n)^4+642*A*a^2*b*d*m*n^3*(x^n)^2+156*A*a*b^2* \\
& c*m^3*n*(x^n)^2+531*A*a*b^2*c*m^2*n^2*(x^n)^2+642*A*a*b^2*c*m*n^3*(x^n)^2+6 \\
& 0*A*a^3*c*m^3*n+255*A*a^3*c*m^2*n^2+450*A*a^3*c*m*n^3+90*A*a^3*c*m^2*n+255* \\
& A*a^3*c*m*n^2+156*A*b^3*c*m*n^3*(x^n)^3+66*A*b^3*d*m^2*n*(x^n)^4+123*A*b^3* \\
& d*m*n^2*(x^n)^4+15*B*a^2*b*d*m^4*(x^n)^3+120*B*a^2*b*d*n^4*(x^n)^3+15*B*a*b \\
& ^2*c*m^4*(x^n)^3+120*B*a*b^2*c*n^4*(x^n)^3+24*B*b^3*d*n^4*(x^n)^5+A*b^3*c*m \\
& ^5*(x^n)^3+3*B*a*b^2*d*m^5*(x^n)^4+15*A*a^3*c*m^4*n+85*A*a^3*c*m^3*n^2+225*
\end{aligned}$$

$$A^3c^2m^2n^3 + 274A^3c^2m^2n^4 + 144B^2c^2m^2n^3(x^n)^3 + 252A^2b^2c^2m^2n^2x^n + 120A^2b^2d^2m^2n^4(x^n)^3 + 48A^2b^3c^2m^2n^3(x^n)^3 + 147A^2b^3c^2m^2n^2(x^n)^3 + 105B^2b^3d^2m^2n^2(x^n)^5 + 3A^2b^2d^2m^5(x^n)^2 + 3A^2b^2c^2m^5(x^n)^2 + 15A^2b^2d^2m^4(x^n)^3 + 30B^2b^2c^2m^2(x^n)^2 + 177B^2b^2c^2m^2n^2(x^n)^2 + 15B^2b^2d^2m^2(x^n)^3 + 36B^2b^2d^2m^2(x^n)^3 + 60B^2b^3d^2m^2n(x^n)^5 + 36A^2b^2d^2m^2(x^n)^3 + 84B^2b^3c^2m^2n^2x^n + 213B^2b^3c^2m^2n^2x^n + 52B^2b^3d^2m^2n^2(x^n)^2 + 14A^3d^2m^4n^2x^n + 71A^3d^2m^3n^2x^n + 154A^3d^2m^2n^3x^n + 177A^2b^2c^2n^2(x^n)^2 + 15A^2b^2d^2m^2(x^n)^3 + 15A^2b^2c^2x^nm + 183B^2b^2d^2m^3(x^n)^4 + 66B^2b^3c^2m^2n^2(x^n)^4 + 123B^2b^3c^2m^2n^2(x^n)^4 + 40B^2b^3d^2m^2n^2(x^n)^5 + 30A^2b^3d^2m^2n^4(x^n)^4 + 39B^2b^2c^2(x^n)^2 + 11A^2b^3d^2m^4n^2(x^n)^4 + 41A^2b^3d^2m^3n^2(x^n)^4 + 61A^2b^3d^2m^2n^3(x^n)^4 + 180A^2b^2d^2m^4(x^n)^2 + 15A^2b^2c^2m^4(x^n)^2 + 180A^2b^2c^2n^4(x^n)^2 + 35B^2b^3d^2m^3n^2(x^n)^5 + 50B^2b^3d^2m^2n^3(x^n)^5 + 24B^2b^3d^2m^2n^4(x^n)^5 + 120A^3d^2m^2n^4x^n + 3A^2b^2c^2m^2n^4x^n + \dots$$

**Maxima** [B] Leaf count of result is larger than twice the leaf count of optimal. 434 vs.  $2(215) = 430$ .

time = 0.34, size = 434, normalized size = 2.07

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Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="maxima")

[Out]  $(x^m e^m)^{m+1} A^3 c^2 e^{-1} / (m+1) + B^2 b^3 d^2 x^m e^{(m \log(x) + 5n \log(x) + m) / (m+5n+1)} + B^2 b^3 c^2 x^m e^{(m \log(x) + 4n \log(x) + m) / (m+4n+1)} + 3B^2 a^2 b^2 d^2 x^m e^{(m \log(x) + 4n \log(x) + m) / (m+4n+1)} + A^2 b^3 d^2 x^m e^{(m \log(x) + 4n \log(x) + m) / (m+4n+1)} + 3B^2 a^2 b^2 c^2 x^m e^{(m \log(x) + 3n \log(x) + m) / (m+3n+1)} + A^2 b^3 c^2 x^m e^{(m \log(x) + 3n \log(x) + m) / (m+3n+1)} + 3B^2 a^2 b^2 d^2 x^m e^{(m \log(x) + 3n \log(x) + m) / (m+3n+1)} + 3A^2 a^2 b^2 d^2 x^m e^{(m \log(x) + 3n \log(x) + m) / (m+3n+1)} + 3B^2 a^2 b^2 c^2 x^m e^{(m \log(x) + 2n \log(x) + m) / (m+2n+1)} + 3A^2 a^2 b^2 c^2 x^m e^{(m \log(x) + 2n \log(x) + m) / (m+2n+1)} + B^2 a^3 d^2 x^m e^{(m \log(x) + 2n \log(x) + m) / (m+2n+1)} + 3A^2 a^2 b^2 d^2 x^m e^{(m \log(x) + 2n \log(x) + m) / (m+2n+1)} + B^2 a^3 c^2 x^m e^{(m \log(x) + n \log(x) + m) / (m+n+1)} + 3A^2 a^2 b^2 c^2 x^m e^{(m \log(x) + n \log(x) + m) / (m+n+1)} + A^2 a^3 d^2 x^m e^{(m \log(x) + n \log(x) + m) / (m+n+1)}$

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 3055 vs.  $2(215) = 430$ .

time = 3.75, size = 3055, normalized size = 14.55

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="fricas")



[Out]  $((B*b^3*d*m^5 + 5*B*b^3*d*m^4 + 10*B*b^3*d*m^3 + 10*B*b^3*d*m^2 + 5*B*b^3*d*m + B*b^3*d + 24*(B*b^3*d*m + B*b^3*d)*n^4 + 50*(B*b^3*d*m^2 + 2*B*b^3*d*m + B*b^3*d)*n^3 + 35*(B*b^3*d*m^3 + 3*B*b^3*d*m^2 + 3*B*b^3*d*m + B*b^3*d)*n^2 + 10*(B*b^3*d*m^4 + 4*B*b^3*d*m^3 + 6*B*b^3*d*m^2 + 4*B*b^3*d*m + B*b^3*d)*n)*x*x^(5*n)*e^(m*log(x) + m) + ((B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^5 + B*b^3*c + 5*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^4 + 30*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n^4 + 10*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^3 + 61*(B*b^3*c + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + (3*B*a*b^2 + A*b^3)*d + 2*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n^3 + 10*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + 41*(B*b^3*c + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^3 + 3*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + (3*B*a*b^2 + A*b^3)*d + 3*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n^2 + (3*B*a*b^2 + A*b^3)*d + 5*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m + 11*(B*b^3*c + (B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^4 + 4*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^3 + 6*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m^2 + (3*B*a*b^2 + A*b^3)*d + 4*(B*b^3*c + (3*B*a*b^2 + A*b^3)*d)*m)*n)*x*x^(4*n)*e^(m*log(x) + m) + (((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^5 + 5*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^4 + 40*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + ((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m)*n^4 + 10*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^3 + 78*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + (3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + 2*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m)*n^3 + 10*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + 49*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^3 + 3*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + (3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + 3*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m)*n^2 + (3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + 5*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m + 12*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^4 + 4*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^3 + 6*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m^2 + (3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d + 4*((3*B*a*b^2 + A*b^3)*c + 3*(B*a^2*b + A*a*b^2)*d)*m)*n)*x*x^(3*n)*e^(m*log(x) + m) + ((3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^5 + 5*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^4 + 60*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + (3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m)*n^4 + 10*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^3 + 107*((3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^2 + 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + 2*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m)*n^3 + 10*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^2 + 59*((3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^3 + 3*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^2 + 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + 3*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m)*n^2 + 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + 5*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m + 13*((3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^4 + 4*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^3 + 6*(3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d)*m^2 +$

$$\begin{aligned}
& 3*(B*a^2*b + A*a*b^2)*c + (B*a^3 + 3*A*a^2*b)*d + 4*(3*(B*a^2*b + A*a*b^2)* \\
& c + (B*a^3 + 3*A*a^2*b)*d)*m)*n)*x^{(2*n)}*e^{(m*\log(x) + m)} + ((A*a^3*d + ( \\
& B*a^3 + 3*A*a^2*b)*c)*m^5 + A*a^3*d + 5*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m \\
& ^4 + 120*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c + (A*a^3*d + (B*a^3 + 3*A*a^2*b)* \\
& c)*m)*n^4 + 10*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^3 + 154*(A*a^3*d + (A*a^ \\
& 3*d + (B*a^3 + 3*A*a^2*b)*c)*m^2 + (B*a^3 + 3*A*a^2*b)*c + 2*(A*a^3*d + (B* \\
& a^3 + 3*A*a^2*b)*c)*m)*n^3 + 10*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^2 + 71* \\
& (A*a^3*d + (A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^3 + 3*(A*a^3*d + (B*a^3 + 3* \\
& A*a^2*b)*c)*m^2 + (B*a^3 + 3*A*a^2*b)*c + 3*(A*a^3*d + (B*a^3 + 3*A*a^2*b)* \\
& c)*m)*n^2 + (B*a^3 + 3*A*a^2*b)*c + 5*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m + \\
& 14*(A*a^3*d + (A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^4 + 4*(A*a^3*d + (B*a^3 \\
& + 3*A*a^2*b)*c)*m^3 + 6*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m^2 + (B*a^3 + 3* \\
& A*a^2*b)*c + 4*(A*a^3*d + (B*a^3 + 3*A*a^2*b)*c)*m)*n)*x^n*e^{(m*\log(x) + \\
& m)} + (A*a^3*c*m^5 + 120*A*a^3*c*n^5 + 5*A*a^3*c*m^4 + 10*A*a^3*c*m^3 + 10*A \\
& *a^3*c*m^2 + 5*A*a^3*c*m + A*a^3*c + 274*(A*a^3*c*m + A*a^3*c)*n^4 + 225*(A \\
& *a^3*c*m^2 + 2*A*a^3*c*m + A*a^3*c)*n^3 + 85*(A*a^3*c*m^3 + 3*A*a^3*c*m^2 + \\
& 3*A*a^3*c*m + A*a^3*c)*n^2 + 15*(A*a^3*c*m^4 + 4*A*a^3*c*m^3 + 6*A*a^3*c*m \\
& ^2 + 4*A*a^3*c*m + A*a^3*c)*n)*x*e^{(m*\log(x) + m)}/(m^6 + 120*(m + 1)*n^5 + \\
& 6*m^5 + 274*(m^2 + 2*m + 1)*n^4 + 15*m^4 + 225*(m^3 + 3*m^2 + 3*m + 1)*n^3 \\
& + 20*m^3 + 85*(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n^2 + 15*m^2 + 15*(m^5 + 5*m \\
& ^4 + 10*m^3 + 10*m^2 + 5*m + 1)*n + 6*m + 1)
\end{aligned}$$

**Sympy [B]** Leaf count of result is larger than twice the leaf count of optimal. 63250 vs.  $2(206) = 412$ .

time = 175.91, size = 63250, normalized size = 301.19

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*3\*(A+B\*x\*\*n)\*(c+d\*x\*\*n),x)

[Out] Piecewise(((A + B)\*(a + b)\*\*3\*(c + d)\*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A\*a\*\*3\*c\*log(x) + A\*a\*\*3\*d\*x\*\*n/n + 3\*A\*a\*\*2\*b\*c\*x\*\*n/n + 3\*A\*a\*\*2\*b\*d\*x\*\*(2\*n)/(2\*n) + 3\*A\*a\*b\*\*2\*c\*x\*\*(2\*n)/(2\*n) + A\*a\*b\*\*2\*d\*x\*\*(3\*n)/n + A\*b\*\*3\*c\*x\*\*(3\*n)/(3\*n) + A\*b\*\*3\*d\*x\*\*(4\*n)/(4\*n) + B\*a\*\*3\*c\*x\*\*n/n + B\*a\*\*3\*d\*x\*\*(2\*n)/(2\*n) + 3\*B\*a\*\*2\*b\*c\*x\*\*(2\*n)/(2\*n) + B\*a\*\*2\*b\*d\*x\*\*(3\*n)/n + B\*a\*b\*\*2\*c\*x\*\*(3\*n)/n + 3\*B\*a\*b\*\*2\*d\*x\*\*(4\*n)/(4\*n) + B\*b\*\*3\*c\*x\*\*(4\*n)/(4\*n) + B\*b\*\*3\*d\*x\*\*(5\*n)/(5\*n))/e, Eq(m, -1)), (A\*a\*\*3\*c\*Piecewise((-1/(5\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + A\*a\*\*3\*d\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*a\*\*2\*b\*c\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*a\*\*2\*b\*d\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*a\*b\*\*2\*c\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*a\*b\*\*2\*d\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + A\*b\*\*3\*c\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/

$e + A*b**3*d*Piecewise((-x**(4*n)/(n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + B*a**3*c*Piecewise((-x**n/(4*n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + B*a**3*d*Piecewise((-x**(2*n)/(3*n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a**2*b*c*Piecewise((-x**(2*n)/(3*n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a**2*b*d*Piecewise((-x**(3*n)/(2*n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a*b**2*c*Piecewise((-x**(3*n)/(2*n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a*b**2*d*Piecewise((-x**(4*n)/(n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + B*b**3*c*Piecewise((-x**(4*n)/(n*(e*x)**(5*n))), Ne(n, 0)), (\log(x), True))/e + B*b**3*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (\log(x)/e**(5*n), Abs(x) < 1), (-log(1/x)/e**(5*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(5*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(5*n), True))/e, Eq(m, -5*n - 1)), (A*a**3*c*Piecewise((-1/(4*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + A*a**3*d*Piecewise((-x**n/(3*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a**2*b*c*Piecewise((-x**n/(3*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a**2*b*d*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a*b**2*c*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a*b**2*d*Piecewise((-x**(3*n)/(n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + A*b**3*c*Piecewise((-x**(3*n)/(n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + A*b**3*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (\log(x)/e**(4*n), Abs(x) < 1), (-log(1/x)/e**(4*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), True))/e + B*a**3*c*Piecewise((-x**n/(3*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + B*a**3*d*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a**2*b*c*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a**2*b*d*Piecewise((-x**(3*n)/(n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a*b**2*c*Piecewise((-x**(3*n)/(n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e + 3*B*a*b**2*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (\log(x)/e**(4*n), Abs(x) < 1), (-log(1/x)/e**(4*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), True))/e + B*b**3*c*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (\log(x)/e**(4*n), Abs(x) < 1), (-log(1/x)/e**(4*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), True))/e + B*b**3*d*Piecewise((x**(5*n)/(n*(e*x)**(4*n))), Ne(n, 0)), (\log(x), True))/e, Eq(m, -4*n - 1)), (A*a**3*c*Piecewise((-1/(3*n*(e*x)**(3*n))), Ne(n, 0)), (\log(x), True))/e + A*a**3*d*Piecewise((-x**n/(2*n*(e*x)**(3*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a**2*b*c*Piecewise((-x**n/(2*n*(e*x)**(3*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a**2*b*d*Piecewise((-x**(2*n)/(n*(e*x)**(3*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a*b**2*c*Piecewise((-x**(2*n)/(n*(e*x)**(3*n))), Ne(n, 0)), (\log(x), True))/e + 3*A*a*b**2*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (\log(x)/e**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(3*n), True))/e + A*b**3*c*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)),$

$(\log(x)/e^{3n}, \text{Abs}(x) < 1), (-\log(1/x)/e^{3n}, 1/\text{Abs}(x) < 1), (-\text{meijerg}(((), (1, 1)), ((0, 0), ()), x)/e^{3n} + \text{meijerg}(((1, 1), ()), ((), (0, 0)), x)/e^{3n}, \text{True})/e + A*b^{3*d}\text{Piecewise}((x^{4n}/(n*(e^x)^{3n}), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + B*a^{3*c}\text{Piecewise}((-x^{2n}/(2*n*(e^x)^{3n}), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + B*a^{3*d}\text{Piecewise}((-x^{2n}/(n*(e^x)^{3n}), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*B*a^{2*b*c}\text{Piecewise}((-x^{2n}/(n*(e^x)^{3n}), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*B*a^{2*b*d}\text{Piecewise}((0, (\text{Abs}(x) < 1) \& (1/\text{Abs}(x) < 1)), (\log(x)/e^{3n})...$

**Giac [B]** Leaf count of result is larger than twice the leaf count of optimal. 6927 vs.  $2(215) = 430$ .

time = 0.68, size = 6927, normalized size = 32.99

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n),x, algorithm="giac")`

[Out]  $(B*b^3*d^m^5*x*x^m*x^{(5*n)}*e^m + 10*B*b^3*d^m^4*n*x*x^m*x^{(5*n)}*e^m + 35*B*b^3*d^m^3*n^2*x*x^m*x^{(5*n)}*e^m + 50*B*b^3*d^m^2*n^3*x*x^m*x^{(5*n)}*e^m + 24*B*b^3*d^m*n^4*x*x^m*x^{(5*n)}*e^m + B*b^3*c^m^5*x*x^m*x^{(4*n)}*e^m + 3*B*a*b^2*d^m^5*x*x^m*x^{(4*n)}*e^m + A*b^3*d^m^5*x*x^m*x^{(4*n)}*e^m + 11*B*b^3*c^m^4*n*x*x^m*x^{(4*n)}*e^m + 33*B*a*b^2*d^m^4*n*x*x^m*x^{(4*n)}*e^m + 11*A*b^3*d^m^4*n*x*x^m*x^{(4*n)}*e^m + 41*B*b^3*c^m^3*n^2*x*x^m*x^{(4*n)}*e^m + 123*B*a*b^2*d^m^3*n^2*x*x^m*x^{(4*n)}*e^m + 41*A*b^3*d^m^3*n^2*x*x^m*x^{(4*n)}*e^m + 61*B*b^3*c^m^2*n^3*x*x^m*x^{(4*n)}*e^m + 183*B*a*b^2*d^m^2*n^3*x*x^m*x^{(4*n)}*e^m + 61*A*b^3*d^m^2*n^3*x*x^m*x^{(4*n)}*e^m + 30*B*b^3*c^m*n^4*x*x^m*x^{(4*n)}*e^m + 90*B*a*b^2*d^m*n^4*x*x^m*x^{(4*n)}*e^m + 30*A*b^3*d^m*n^4*x*x^m*x^{(4*n)}*e^m + 3*B*a*b^2*c^m^5*x*x^m*x^{(3*n)}*e^m + A*b^3*c^m^5*x*x^m*x^{(3*n)}*e^m + 3*B*a^2*b*d^m^5*x*x^m*x^{(3*n)}*e^m + 3*A*a*b^2*d^m^5*x*x^m*x^{(3*n)}*e^m + 36*B*a*b^2*c^m^4*n*x*x^m*x^{(3*n)}*e^m + 12*A*b^3*c^m^4*n*x*x^m*x^{(3*n)}*e^m + 36*B*a^2*b*d^m^4*n*x*x^m*x^{(3*n)}*e^m + 36*A*a*b^2*d^m^4*n*x*x^m*x^{(3*n)}*e^m + 147*B*a*b^2*c^m^3*n^2*x*x^m*x^{(3*n)}*e^m + 49*A*b^3*c^m^3*n^2*x*x^m*x^{(3*n)}*e^m + 147*B*a^2*b*d^m^3*n^2*x*x^m*x^{(3*n)}*e^m + 147*A*a*b^2*d^m^3*n^2*x*x^m*x^{(3*n)}*e^m + 234*B*a*b^2*c^m^2*n^3*x*x^m*x^{(3*n)}*e^m + 78*A*b^3*c^m^2*n^3*x*x^m*x^{(3*n)}*e^m + 234*B*a^2*b*d^m^2*n^3*x*x^m*x^{(3*n)}*e^m + 234*A*a*b^2*d^m^2*n^3*x*x^m*x^{(3*n)}*e^m + 120*B*a*b^2*c^m*n^4*x*x^m*x^{(3*n)}*e^m + 40*A*b^3*c^m*n^4*x*x^m*x^{(3*n)}*e^m + 120*B*a^2*b*d^m*n^4*x*x^m*x^{(3*n)}*e^m + 3*B*a^2*b*c^m^5*x*x^m*x^{(2*n)}*e^m + 3*A*a*b^2*c^m^5*x*x^m*x^{(2*n)}*e^m + B*a^3*d^m^5*x*x^m*x^{(2*n)}*e^m + 3*A*a^2*b*d^m^5*x*x^m*x^{(2*n)}*e^m + 39*B*a^2*b*c^m^4*n*x*x^m*x^{(2*n)}*e^m + 39*A*a*b^2*c^m^4*n*x*x^m*x^{(2*n)}*e^m + 13*B*a^3*d^m^4*n*x*x^m*x^{(2*n)}*e^m + 39*A*a^2*b*d^m^4*n*x*x^m*x^{(2*n)}*e^m + 177*B*a^2*b*c^m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*a*b^2*c^m^3*n^2*x*x^m*x^{(2*n)}*e^m + 59*B*a^3*d^m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*a^2*b*d^m^3*n^2*x*x^m*x^{(2*n)}*e^m + 321*B*a^2*b*c^m^2*n^3*x*x^m*x^{(2*n)}$

$$\begin{aligned}
& )e^m + 321A^2a^2b^2c^2m^2n^3xxx^m x^{(2n)}e^m + 107B^3a^3d^2m^2n^3xxx^m \\
& x^{(2n)}e^m + 321A^2a^2b^2d^2m^2n^3xxx^m x^{(2n)}e^m + 180B^2a^2b^2c^2m^2n^4 \\
& xxx^m x^{(2n)}e^m + 180A^2a^2b^2c^2m^2n^4xxx^m x^{(2n)}e^m + 60B^3a^3d^2m^2n^4 \\
& xxx^m x^{(2n)}e^m + 180A^2a^2b^2d^2m^2n^4xxx^m x^{(2n)}e^m + B^3a^3c^2m^5 \\
& xxx^m x^n e^m + 3A^2a^2b^2c^2m^5xxx^m x^n e^m + A^3a^3d^2m^5xxx^m x^n e^m \\
& + 14B^3a^3c^2m^4n^2xxx^m x^n e^m + 42A^2a^2b^2c^2m^4n^2xxx^m x^n e^m + 14A^3 \\
& a^3d^2m^4n^2xxx^m x^n e^m + 71B^3a^3c^2m^3n^2xxx^m x^n e^m + 213A^2a^2b^2c^2m^3 \\
& n^2xxx^m x^n e^m + 71A^3a^3d^2m^3n^2xxx^m x^n e^m + 154B^3a^3c^2m^2n^3 \\
& xxx^m x^n e^m + 462A^2a^2b^2c^2m^2n^3xxx^m x^n e^m + 154A^3a^3d^2m^2n^3 \\
& xxx^m x^n e^m + 120B^3a^3c^2m^2n^4xxx^m x^n e^m + 360A^2a^2b^2c^2m^2n^4 \\
& xxx^m x^n e^m + 120A^3a^3d^2m^2n^4xxx^m x^n e^m + A^3a^3c^2m^5xxx^m e^m + 1 \\
& 5A^2a^2b^2c^2m^4n^2xxx^m e^m + 85A^3a^3c^2m^3n^2xxx^m e^m + 225A^2a^2b^2c^2m^2n^3 \\
& xxx^m e^m + 274A^3a^3c^2m^2n^4xxx^m e^m + 120A^3a^3c^2m^2n^5xxx^m e^m + 5 \\
& B^3b^3d^2m^4xxx^m x^{(5n)}e^m + 40B^3b^3d^2m^3n^2xxx^m x^{(5n)}e^m + 105B^3 \\
& b^3d^2m^2n^2xxx^m x^{(5n)}e^m + 100B^3b^3d^2m^2n^3xxx^m x^{(5n)}e^m + 24 \\
& B^3b^3d^2n^4xxx^m x^{(5n)}e^m + 5B^3b^3c^2m^4xxx^m x^{(4n)}e^m + 15B^2a^2b^2 \\
& d^2m^4xxx^m x^{(4n)}e^m + 5A^2b^2c^2m^4xxx^m x^{(4n)}e^m + 44B^3b^3c^2m^3n^2 \\
& xxx^m x^{(4n)}e^m + 132B^2a^2b^2d^2m^3n^2xxx^m x^{(4n)}e^m + 44A^2b^2c^2d^2 \\
& m^3n^2xxx^m x^{(4n)}e^m + 123B^3b^3c^2m^2n^2xxx^m x^{(4n)}e^m + 369B^2a^2b^2 \\
& d^2m^2n^2xxx^m x^{(4n)}e^m + 123A^2b^2c^2d^2m^2n^2xxx^m x^{(4n)}e^m + 1 \\
& 22B^3b^3c^2m^2n^3xxx^m x^{(4n)}e^m + 366B^2a^2b^2d^2m^2n^3xxx^m x^{(4n)}e^m \\
& + 122A^2b^2c^2d^2m^2n^3xxx^m x^{(4n)}e^m + 30B^3b^3c^2n^4xxx^m x^{(4n)}e^m + \\
& 90B^2a^2b^2d^2n^4xxx^m x^{(4n)}e^m + 30A^2b^2c^2d^2n^4xxx^m x^{(4n)}e^m + 15 \\
& B^2a^2b^2c^2m^4xxx^m x^{(3n)}e^m + 5A^2b^2c^2m^4xxx^m x^{(3n)}e^m + 15B^2a^2 \\
& b^2d^2m^4xxx^m x^{(3n)}e^m + 15A^2a^2b^2d^2m^4xxx^m x^{(3n)}e^m + 144B^2a^2b^2 \\
& c^2m^3n^2xxx^m x^{(3n)}e^m + 48A^2b^2c^2m^3n^2xxx^m x^{(3n)}e^m + 144B^2a^2b^2 \\
& d^2m^3n^2xxx^m x^{(3n)}e^m + 144A^2a^2b^2d^2m^3n^2xxx^m x^{(3n)}e^m + 4 \\
& 41B^2a^2b^2c^2m^2n^2xxx^m x^{(3n)}e^m + 147A^2b^2c^2m^2n^2xxx^m x^{(3n)}e^m \\
& + 441B^2a^2b^2d^2m^2n^2xxx^m x^{(3n)}e^m + 441A^2a^2b^2d^2m^2n^2xxx^m \\
& x^{(3n)}e^m + 468B^2a^2b^2c^2m^2n^3xxx^m x^{(3n)}e^m + 156A^2b^2c^2m^2n^3xxx^m \\
& x^{(3n)}e^m + 468B^2a^2b^2d^2m^2n^3xxx^m x^{(3n)}e^m + 468A^2a^2b^2d^2m^2n^3 \\
& xxx^m x^{(3n)}e^m + 120B^2a^2b^2c^2n^4xxx^m x^{(3n)}e^m + 40A^2b^2c^2n^4 \\
& xxx^m x^{(3n)}e^m + 120B^2a^2b^2d^2n^4xxx^m x^{(3n)}e^m + 120A^2a^2b^2d^2n^4 \\
& xxx^m x^{(3n)}e^m + 15B^2a^2b^2c^2m^4xxx^m x^{(2n)}e^m + 15A^2a^2b^2c^2m^4 \\
& xxx^m x^{(2n)}e^m + 5B^2a^3d^2m^4xxx^m x^{(2n)}e^m + 15A^2a^2b^2d^2m^4xxx^m \\
& x^{(2n)}e^m + 156B^2a^2b^2c^2m^3n^2xxx^m x^{(2n)}e^m + 156A^2a^2b^2c^2m^3n^2 \\
& xxx^m x^{(2n)}e^m + 52B^2a^3d^2m^3n^2xxx^m x^{(2n)}e^m + 156A^2a^2b^2d^2m^3 \\
& n^2xxx^m x^{(2n)}e^m + 531B^2a^2b^2c^2m^2n^2xxx^m x^{(2n)}e^m + 531A^2a^2b^2 \\
& c^2m^2n^2xxx^m x^{(2n)}e^m + 177B^2a^3d^2m^2n^2xxx^m x^{(2n)}e^m + 53 \\
& 1A^2a^2b^2d^2m^2n^2xxx^m x^{(2n)}e^m + 642B^2a^2b^2c^2m^2n^2xxx^m x^{(2n)}e^m + \dots
\end{aligned}$$

Mupad [B]

time = 5.64, size = 1089, normalized size = 5.19

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)^3*(c + d*x^n), x)$

[Out]  $(A*a^3*c*x*(e*x)^m)/(m + 1) + (b^2*x*x^{(4*n)}*(e*x)^m*(A*b*d + 3*B*a*d + B*b*c)*(4*m + 11*n + 33*m*n + 82*m*n^2 + 33*m^2*n + 61*m*n^3 + 11*m^3*n + 6*m^2 + 4*m^3 + m^4 + 41*n^2 + 61*n^3 + 30*n^4 + 41*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (a*x*x^{(2*n)}*(e*x)^m*(3*A*b^2*c + B*a^2*d + 3*A*a*b*d + 3*B*a*b*c)*(4*m + 13*n + 39*m*n + 118*m*n^2 + 39*m^2*n + 107*m*n^3 + 13*m^3*n + 6*m^2 + 4*m^3 + m^4 + 59*n^2 + 107*n^3 + 60*n^4 + 59*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (b*x*x^{(3*n)}*(e*x)^m*(A*b^2*c + 3*B*a^2*d + 3*A*a*b*d + 3*B*a*b*c)*(4*m + 12*n + 36*m*n + 98*m*n^2 + 36*m^2*n + 78*m*n^3 + 12*m^3*n + 6*m^2 + 4*m^3 + m^4 + 49*n^2 + 78*n^3 + 40*n^4 + 49*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (a^2*x*x^n*(e*x)^m*(A*a*d + 3*A*b*c + B*a*c)*(4*m + 14*n + 42*m*n + 142*m*n^2 + 42*m^2*n + 154*m*n^3 + 14*m^3*n + 6*m^2 + 4*m^3 + m^4 + 71*n^2 + 154*n^3 + 120*n^4 + 71*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (B*b^3*d*x*x^{(5*n)}*(e*x)^m*(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1)$

### 3.2 $\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=160

$$\frac{a(2Abc + aBc + aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(aB(2bc + ad) + Ab(bc + 2ad))x^{1+2n}(ex)^m}{1+m+2n} + \frac{b(bBc + Abd + 2aBd)x^{1+3n}(ex)^m}{1+m+3n}$$

[Out]  $a*(A*a*d+2*A*b*c+B*a*c)*x^{(1+n)}*(e*x)^m/(1+m+n)+(a*B*(a*d+2*b*c)+A*b*(2*a*d+b*c))*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+b*(A*b*d+2*B*a*d+B*b*c)*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+b^2*B*d*x^{(1+4*n)}*(e*x)^m/(1+m+4*n)+a^2*A*c*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.11, antiderivative size = 160, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ ,

Rules used = {584, 20, 30}

$$\frac{a^2 Ac(ex)^{m+1}}{e(m+1)} + \frac{ax^{n+1}(ex)^m(aAd + aBc + 2Abc)}{m+n+1} + \frac{x^{2n+1}(ex)^m(Ab(2ad + bc) + aB(ad + 2bc))}{m+2n+1} + \frac{bx^{3n+1}(ex)^m(2aBd + Abd + bBc)}{m+3n+1} + \frac{b^2 Bdx^{4n+1}(ex)^m}{m+4n+1}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(a + b*x^n)^2*(A + B*x^n)*(c + d*x^n), x]$

[Out]  $(a*(2*A*b*c + a*B*c + a*A*d)*x^{(1+n)}*(e*x)^m)/(1+m+n) + ((a*B*(2*b*c + a*d) + A*b*(b*c + 2*a*d))*x^{(1+2*n)}*(e*x)^m)/(1+m+2*n) + (b*(b*B*c + A*b*d + 2*a*B*d)*x^{(1+3*n)}*(e*x)^m)/(1+m+3*n) + (b^2*B*d*x^{(1+4*n)}*(e*x)^m)/(1+m+4*n) + (a^2*A*c*(e*x)^{(1+m)})/(e*(1+m))$

**Rule 20**

$\text{Int}[(u_*)*((a_*)*(v_))^{(m_*)}*((b_*)*(v_))^{(n_*)}, x\_Symbol] \rightarrow \text{Dist}[b^{\text{IntPart}[n]}*(b*v)^{\text{FracPart}[n]}/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]})], \text{Int}[u*(a*v)^{(m+n)}, x], x] /;$  FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

**Rule 30**

$\text{Int}[(x_*)^{(m_*)}, x\_Symbol] \rightarrow \text{Simp}[x^{(m+1)}/(m+1), x] /;$  FreeQ[m, x] && NeQ[m, -1]

**Rule 584**

$\text{Int}[(g_*)*(x_*)^{(m_*)}*((a_*) + (b_*)*(x_*)^{(n_*)})^{(p_*)}*((c_*) + (d_*)*(x_*)^{(n_*)})^{(q_*)}*((e_*) + (f_*)*(x_*)^{(n_*)})^{(r_*)}, x\_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /;$  FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

Rubi steps

$$\begin{aligned}
\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n) dx &= \int (a^2 Ac(ex)^m + a(2Abc + aBc + aAd)x^n(ex)^m + (aB(2bc + \\
&= \frac{a^2 Ac(ex)^{1+m}}{e(1+m)} + (b^2 Bd) \int x^{4n}(ex)^m dx + (a(2Abc + aBc + aAd)x^n(ex)^m) \int x^{m+4n} dx + (aB(2bc + ad) + Ab(bc + ad)) \int x^{m+n} dx \\
&= \frac{a^2 Ac(ex)^{1+m}}{e(1+m)} + (b^2 Bdx^{-m}(ex)^m) \int x^{m+4n} dx + (a(2Abc + aBc + aAd)x^n(ex)^m) \int x^{m+n} dx + (aB(2bc + ad) + Ab(bc + ad)) \int x^{m+n} dx \\
&= \frac{a(2Abc + aBc + aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(aB(2bc + ad) + Ab(bc + ad))x^{m+n}}{1+m+n}
\end{aligned}$$

**Mathematica [A]**

time = 0.32, size = 129, normalized size = 0.81

$$x(ex)^m \left( \frac{a^2 Ac}{1+m} + \frac{a(2Abc + aBc + aAd)x^n}{1+m+n} + \frac{(aB(2bc + ad) + Ab(bc + 2ad))x^{2n}}{1+m+2n} + \frac{b(bBc + Abd + 2aBd)x^{3n}}{1+m+3n} + \frac{b^2 Bdx^{4n}}{1+m+4n} \right)$$

Antiderivative was successfully verified.

`[In] Integrate[(e*x)^m*(a + b*x^n)^2*(A + B*x^n)*(c + d*x^n), x]`

```
[Out] x*(e*x)^m*((a^2*A*c)/(1+m) + (a*(2*A*b*c + a*B*c + a*A*d)*x^n)/(1+m+n) + ((a*B*(2*b*c + a*d) + A*b*(b*c + 2*a*d))*x^(2*n))/(1+m+2*n) + (b*(b*B*c + A*b*d + 2*a*B*d)*x^(3*n))/(1+m+3*n) + (b^2*B*d*x^(4*n))/(1+m+4*n))
```

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.38, size = 2410, normalized size = 15.06

method	result	size
risch	Expression too large to display	2410

Verification of antiderivative is not currently implemented for this CAS.

`[In] int((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n), x, method=_RETURNVERBOSE)`

```
[Out] x*(38*B*a^2*d*m*n^2*(x^n)^2+8*B*a*b*c*m^3*(x^n)^2+24*A*b^2*c*m*n*(x^n)^2+27*B*a^2*c*m^2*n*x^n+52*B*a^2*c*m*n^2*x^n+24*B*a^2*d*m*n*(x^n)^2+19*B*a^2*d*m^2*n^2*(x^n)^2+12*A*a*b*d*m^2*(x^n)^2+38*A*a*b*d*n^2*(x^n)^2+2*x^n*c*a*b*A+8*B*a^2*d*m^3*n*(x^n)^2+A*a^2*d*x^n+B*a^2*c*x^n+30*A*a^2*c*m^2*n+70*A*a^2*c*m*n^2+30*A*a^2*c*m*n+21*B*b^2*c*m^2*n*(x^n)^3+28*B*b^2*c*m*n^2*(x^n)^3+18*B*b^2*d*m*n*(x^n)^4+9*A*a^2*d*m^3*n*x^n+26*A*a^2*d*m^2*n^2*x^n+24*A*a*b*d*m*n^3*(x^n)^2+16*B*a*b*c*m^3*n*(x^n)^2+38*B*a*b*c*m^2*n^2*(x^n)^2+a^2*A*c+48*B*a*b*c*m*n*(x^n)^2+54*A*a*b*c*m*n*x^n+16*A*a*b*d*m^3*n*(x^n)^2+48*A*a*b*d*m*n*(x^n)^2+(x^n)^2*A*b^2*c+(x^n)^2*B*a^2*d+24*B*a^2*c*m*n^3*x^n+24*B*a^2*d*m^2*n*(x^n)^2+24*A*a^2*d*n^3*x^n+6*A*b^2*c*m^2*(x^n)^2+19*A*b^2*c*n^2*(x^n)^2
```



$$\begin{aligned}
& n)^2+4*A*b^2*d*(x^n)^3+m+7*A*b^2*d*(x^n)^3+n+4*B*a^2*c*m^3*x^n+56*B*a*b*d*m \\
& *n^2*(x^n)^3+18*A*a*b*c*m^3*n*x^n+24*B*a*b*c*m^3*(x^n)^2+42*B*a*b*d*m^2*n \\
& *(x^n)^3+(x^n)^3*b^2*B*c+6*A*a^2*c*m^2+14*B*a*b*d*m^3*n*(x^n)^3+28*B*a*b*d* \\
& m^2*n^2*(x^n)^3+16*B*a*b*d*m*n^3*(x^n)^3+b^2*B*d*(x^n)^4+52*A*a*b*c*m^2*n^2 \\
& *x^n+26*B*a^2*c*n^2*x^n+4*B*a^2*d*(x^n)^2+m+8*B*a^2*d*(x^n)^2+n+B*b^2*d*m^4 \\
& *(x^n)^4+38*A*a*b*d*m^2*n^2*(x^n)^2+A*a^2*c*m^4+4*A*a^2*c*m^3+50*A*a^2*c*n^ \\
& 3+35*A*a^2*c*n^2+11*B*b^2*d*m^2*n^2*(x^n)^4+B*a^2*d*m^4*(x^n)^2+4*B*b^2*c*m \\
& ^3*(x^n)^3+8*B*b^2*c*n^3*(x^n)^3+6*B*b^2*d*m^2*(x^n)^4+11*B*b^2*d*n^2*(x^n) \\
& ^4+A*a^2*d*m^4*x^n+27*A*a^2*d*m*n*x^n+12*A*a*b*c*m^2*x^n+26*B*a^2*c*m^2*n^2 \\
& *x^n+104*A*a*b*c*m*n^2*x^n+4*a^2*A*c*m+10*a^2*A*c*n+(x^n)^3*A*b^2*d+54*A*a* \\
& b*c*m^2*n*x^n+24*A*a^2*c*n^4+24*B*a*b*c*n^3*(x^n)^2+12*B*a*b*d*m^2*(x^n)^3+ \\
& 28*B*a*b*d*n^2*(x^n)^3+16*B*a*b*d*n^3*(x^n)^3+12*B*a*b*c*m^2*(x^n)^2+38*B*a \\
& *b*c*n^2*(x^n)^2+8*B*a*b*d*(x^n)^3+m+6*B*b^2*d*m^3*n*(x^n)^4+14*B*a*b*d*(x \\
& ^n)^3+n+16*A*a*b*d*(x^n)^2+n+27*B*a^2*c*m*n*x^n+8*B*a*b*c*(x^n)^2+m+16*B*a*b \\
& *c*(x^n)^2+n+6*B*b^2*d*m*n^3*(x^n)^4+7*A*b^2*d*m^3*n*(x^n)^3+14*A*b^2*d*m^2 \\
& *n^2*(x^n)^3+8*A*b^2*d*m*n^3*(x^n)^3+48*A*a*b*c*m*n^3*x^n+52*A*a*b*c*n^2*x \\
& ^n+8*A*a*b*d*(x^n)^2+m+28*A*b^2*d*m*n^2*(x^n)^3+4*B*a^2*d*m^3*(x^n)^2+12*B*a \\
& ^2*d*n^3*(x^n)^2+6*B*b^2*c*m^2*(x^n)^3+14*B*b^2*c*n^2*(x^n)^3+4*m*b^2*B*d*( \\
& x^n)^4+6*b^2*B*d*(x^n)^4*n+4*A*a^2*d*m^3*x^n+4*A*a^2*d*x^n*m+9*A*a^2*d*x^n* \\
& n+4*B*a^2*c*x^n*m+48*A*a*b*c*n^3*x^n+7*B*b^2*c*m^3*n*(x^n)^3+14*B*b^2*c*m^2 \\
& *n^2*(x^n)^3+8*B*b^2*c*m*n^3*(x^n)^3+8*A*a*b*c*x^n*m+18*A*a*b*c*x^n*n+2*B*a \\
& *b*d*m^4*(x^n)^3+38*A*b^2*c*m*n^2*(x^n)^2+21*A*b^2*d*m*n*(x^n)^3+9*B*a^2*c* \\
& m^3*n*x^n+2*B*a*b*c*m^4*(x^n)^2+8*B*a*b*d*m^3*(x^n)^3+24*A*a*b*d*n^3*(x^n)^ \\
& 2+24*A*b^2*c*m^2*n*(x^n)^2+2*A*a*b*d*m^4*(x^n)^2+12*B*a^2*d*m*n^3*(x^n)^2+1 \\
& 9*A*b^2*c*m^2*n^2*(x^n)^2+12*A*b^2*c*m*n^3*(x^n)^2+21*A*b^2*d*m^2*n*(x^n)^3 \\
& +18*B*b^2*d*m^2*n*(x^n)^4+22*B*b^2*d*m*n^2*(x^n)^4+24*A*a^2*d*m*n^3*x^n+2*A \\
& *a*b*c*m^4*x^n+8*A*a*b*d*m^3*(x^n)^2+8*A*b^2*c*m^3*n*(x^n)^2+76*B*a*b*c*m*n \\
& ^2*(x^n)^2+42*B*a*b*d*m*n*(x^n)^3+76*A*a*b*d*m*n^2*(x^n)^2+48*B*a*b*c*m^2*n \\
& *(x^n)^2+48*A*a*b*d*m^2*n*(x^n)^2+21*B*b^2*c*m*n*(x^n)^3+27*A*a^2*d*m^2*n*x \\
& ^n+52*A*a^2*d*m*n^2*x^n+8*A*a*b*c*m^3*x^n+10*A*a^2*c*m^3*n+35*A*a^2*c*m^2*n \\
& ^2+50*A*a^2*c*m*n^3+9*B*a^2*c*x^n*n+24*B*a^2*c*n^3*x^n+6*B*a^2*d*m^2*(x^n)^ \\
& 2+19*B*a^2*d*n^2*(x^n)^2+A*b^2*d*m^4*(x^n)^3+B*b^2*c*m^4*(x^n)^3+4*B*b^2*d* \\
& m^3*(x^n)^4+6*B*b^2*d*n^3*(x^n)^4+A*b^2*c*m^4*(x^n)^2+4*A*b^2*d*m^3*(x^n)^3 \\
& +8*A*b^2*d*n^3*(x^n)^3+2*(x^n)^2*A*a*b*d+2*(x^n)^2*B*a*b*c+2*(x^n)^3*B*a*b* \\
& d+4*A*b^2*c*m^3*(x^n)^2+12*A*b^2*c*n^3*(x^n)^2+6*A*b^2*d*m^2*(x^n)^3+14*A*b \\
& ^2*d*n^2*(x^n)^3+B*a^2*c*m^4*x^n+4*B*b^2*c*(x^n)^3+m+7*B*b^2*c*(x^n)^3+n+6* \\
& A*a^2*d*m^2*x^n+26*A*a^2*d*n^2*x^n+4*A*b^2*c*(x^n)^2+m+8*A*b^2*c*(x^n)^2+n+ \\
& 6*B*a^2*c*m^2*x^n)/(1+m)/(1+m+n)/(1+m+2*n)/(1+m+3*n)/(1+m+4*n)*exp(1/2*m*(- \\
& I*Pi*csgn(I*e*x)^3+I*Pi*csgn(I*e*x)^2*csgn(I*e)+I*Pi*csgn(I*e*x)^2*csgn(I*x \\
& )-I*Pi*csgn(I*e*x)*csgn(I*e)*csgn(I*x)+2*ln(e)+2*ln(x))
\end{aligned}$$

**Maxima** [A]

time = 0.34, size = 310, normalized size = 1.94

$$\frac{(x^n)^{m+1} A^n e^{c x^{-n}}}{m+1} + \frac{B^2 d x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+4n+1} + \frac{B^2 c x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+3n+1} + \frac{2 B d d x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+3n+1} + \frac{A^2 d x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+3n+1} + \frac{2 B d c x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+2n+1} + \frac{A^2 c x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+2n+1} + \frac{B^2 d x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+2n+1} + \frac{2 A b d x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+2n+1} + \frac{B^2 c x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+n+1} + \frac{2 A b c x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+n+1} + \frac{A^2 d x^{2n} (m^2 b^2 d^2 + 4 b^2 d^2 c + c^2)}{m+n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="maxima")

[Out] (x\*e)^(m + 1)\*A\*a^2\*c\*e^(-1)/(m + 1) + B\*b^2\*d\*x\*e^(m\*log(x) + 4\*n\*log(x) + m)/(m + 4\*n + 1) + B\*b^2\*c\*x\*e^(m\*log(x) + 3\*n\*log(x) + m)/(m + 3\*n + 1) + 2\*B\*a\*b\*d\*x\*e^(m\*log(x) + 3\*n\*log(x) + m)/(m + 3\*n + 1) + A\*b^2\*d\*x\*e^(m\*log(x) + 3\*n\*log(x) + m)/(m + 3\*n + 1) + 2\*B\*a\*b\*c\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + A\*b^2\*c\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + B\*a^2\*d\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + 2\*A\*a\*b\*d\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + B\*a^2\*c\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1) + 2\*A\*a\*b\*c\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1) + A\*a^2\*d\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1)

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 1509 vs. 2(164) = 328.

time = 2.33, size = 1509, normalized size = 9.43

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="fricas")

[Out] ((B\*b^2\*d\*m^4 + 4\*B\*b^2\*d\*m^3 + 6\*B\*b^2\*d\*m^2 + 4\*B\*b^2\*d\*m + B\*b^2\*d + 6\*(B\*b^2\*d\*m + B\*b^2\*d)\*n^3 + 11\*(B\*b^2\*d\*m^2 + 2\*B\*b^2\*d\*m + B\*b^2\*d)\*n^2 + 6\*(B\*b^2\*d\*m^3 + 3\*B\*b^2\*d\*m^2 + 3\*B\*b^2\*d\*m + B\*b^2\*d)\*n)\*x\*x^(4\*n)\*e^(m\*log(x) + m) + ((B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^4 + B\*b^2\*c + 4\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^3 + 8\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d) + (B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m)\*n^3 + 6\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^2 + 14\*(B\*b^2\*c + (B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^2 + (2\*B\*a\*b + A\*b^2)\*d + 2\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m)\*n^2 + (2\*B\*a\*b + A\*b^2)\*d + 4\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m + 7\*(B\*b^2\*c + (B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^3 + 3\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m^2 + (2\*B\*a\*b + A\*b^2)\*d + 3\*(B\*b^2\*c + (2\*B\*a\*b + A\*b^2)\*d)\*m)\*n)\*x\*x^(3\*n)\*e^(m\*log(x) + m) + (((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^4 + 4\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^3 + 12\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d) + ((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m)\*n^3 + 6\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^2 + 19\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^2 + (2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d + 2\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m)\*n^2 + (2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d + 4\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m + 8\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^3 + 3\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m^2 + (2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d + 3\*((2\*B\*a\*b + A\*b^2)\*c + (B\*a^2 + 2\*A\*a\*b)\*d)\*m)\*n)\*x\*x^(2\*n)\*e^(m\*log(x) + m) + ((A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^4 + A\*a^2\*d + 4\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m^3 + 24\*(A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c + (A\*a^2\*d + (B\*a^2 + 2\*A\*a\*b)\*c)\*m)\*n^3 + 6\*(A\*a^2\*d + (B\*a^2 + 2\*A

$$\begin{aligned}
& *a*b)*c)*m^2 + 26*(A*a^2*d + (A*a^2*d + (B*a^2 + 2*A*a*b)*c)*m^2 + (B*a^2 + \\
& 2*A*a*b)*c + 2*(A*a^2*d + (B*a^2 + 2*A*a*b)*c)*m)*n^2 + (B*a^2 + 2*A*a*b)* \\
& c + 4*(A*a^2*d + (B*a^2 + 2*A*a*b)*c)*m + 9*(A*a^2*d + (A*a^2*d + (B*a^2 + \\
& 2*A*a*b)*c)*m^3 + 3*(A*a^2*d + (B*a^2 + 2*A*a*b)*c)*m^2 + (B*a^2 + 2*A*a*b) \\
& *c + 3*(A*a^2*d + (B*a^2 + 2*A*a*b)*c)*m)*n)*x*x^n*e^{(m*\log(x) + m) + (A*a^ \\
& 2*c*m^4 + 24*A*a^2*c*n^4 + 4*A*a^2*c*m^3 + 6*A*a^2*c*m^2 + 4*A*a^2*c*m + A* \\
& a^2*c + 50*(A*a^2*c*m + A*a^2*c)*n^3 + 35*(A*a^2*c*m^2 + 2*A*a^2*c*m + A*a^ \\
& 2*c)*n^2 + 10*(A*a^2*c*m^3 + 3*A*a^2*c*m^2 + 3*A*a^2*c*m + A*a^2*c)*n)*x*e^ \\
& (m*\log(x) + m))/(m^5 + 24*(m + 1)*n^4 + 5*m^4 + 50*(m^2 + 2*m + 1)*n^3 + 10 \\
& *m^3 + 35*(m^3 + 3*m^2 + 3*m + 1)*n^2 + 10*m^2 + 10*(m^4 + 4*m^3 + 6*m^2 + \\
& 4*m + 1)*n + 5*m + 1)
\end{aligned}$$

**Sympy [B]** Leaf count of result is larger than twice the leaf count of optimal. 24932 vs.  $2(156) = 312$ .

time = 88.12, size = 24932, normalized size = 155.82

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)**m*(a+b*x**n)**2*(A+B*x**n)*(c+d*x**n),x)`

[Out] `Piecewise(((A + B)*(a + b)**2*(c + d)*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A*a**2*c*log(x) + A*a**2*d*x**n/n + 2*A*a*b*c*x**n/n + A*a*b*d*x**(2*n)/n + A*b**2*c*x**(2*n)/(2*n) + A*b**2*d*x**(3*n)/(3*n) + B*a**2*c*x**n/n + B*a**2*d*x**(2*n)/(2*n) + B*a*b*c*x**(2*n)/n + 2*B*a*b*d*x**(3*n)/(3*n) + B*b**2*c*x**(3*n)/(3*n) + B*b**2*d*x**(4*n)/(4*n))/e, Eq(m, -1)), (A*a**2*c*Piecewise((-1/(4*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + A*a**2*d*Piecewise((-x**n/(3*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + 2*A*a*b*c*Piecewise((-x**n/(3*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + 2*A*a*b*d*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + A*b**2*c*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + A*b**2*d*Piecewise((-x**(3*n)/(n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + B*a**2*c*Piecewise((-x**n/(3*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + B*a**2*d*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + 2*B*a*b*c*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + 2*B*a*b*d*Piecewise((-x**(3*n)/(n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + B*b**2*c*Piecewise((-x**(3*n)/(n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + B*b**2*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(4*n), Abs(x) < 1), (-log(1/x)/e**(4*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), True))/e, Eq(m, -4*n - 1)), (A*a**2*c*Piecewise((-1/(3*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))/e + A*a**2*d*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))/e + 2*A*a*b*c*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))/e + 2*A*a*b*d*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))/e + A*b**2*c*`

```

Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))/e + A*b**
2*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(3*n), Abs(x)
< 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0),
()), x)/e**(3*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(3*n), True))/
e + B*a**2*c*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True)
)/e + B*a**2*d*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)), (log(x), T
rue))/e + 2*B*a*b*c*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)), (log(
x), True))/e + 2*B*a*b*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log
(x)/e**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-meijerg((
), (1, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), ()), (((), (0, 0)),
x)/e**(3*n), True))/e + B*b**2*c*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) <
1)), (log(x)/e**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-m
eijerg(((), (1, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), ()), (((),
(0, 0)), x)/e**(3*n), True))/e + B*b**2*d*Piecewise((x**(4*n)/(n*(e*x)**(3
*n)), Ne(n, 0)), (log(x), True))/e, Eq(m, -3*n - 1)), (A*a**2*c*Piecewise((
-1/(2*n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + A*a**2*d*Piecewise((-
x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + 2*A*a*b*c*Piecewise((
-x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + 2*A*a*b*d*Piecewise(
(0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n), Abs(x) < 1), (-log(1/
x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(2*
n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n), True))/e + A*b**2*c*P
iecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n), Abs(x) < 1),
(-log(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()),
x)/e**(2*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n), True))/e + A
*b**2*d*Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e
+ B*a**2*c*Piecewise((-x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e
+ B*a**2*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n),
Abs(x) < 1), (-log(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((
0, 0), ()), x)/e**(2*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n),
True))/e + 2*B*a*b*c*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/
e**(2*n), Abs(x) < 1), (-log(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (
1, 1)), ((0, 0), ()), x)/e**(2*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/
e**(2*n), True))/e + 2*B*a*b*d*Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(n,
0)), (log(x), True))/e + B*b**2*c*Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(
n, 0)), (log(x), True))/e + B*b**2*d*Piecewise((x**(4*n)/(2*n*(e*x)**(2*n))
, Ne(n, 0)), (log(x), True))/e, Eq(m, -2*n - 1)), (A*a**2*c*Piecewise((-1/(
n*(e*x)**n), Ne(n, 0)), (log(x), True))/e + A*a**2*d*Piecewise((0, (Abs(x)
< 1) & (1/Abs(x) < 1)), (log(x)/e**n, Abs(x) < 1), (-log(1/x)/e**n, 1/Abs(x)
< 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**n + meijerg(((1, 1), (
)), (((), (0, 0)), x)/e**n, True))/e + 2*A*a*b*c*Piecewise((0, (Abs(x) < 1) &
(1/Abs(x) < 1)), (log(x)/e**n, Abs(x) < 1), (-log(1/x)/e**n, 1/Abs(x) < 1)
, (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**n + meijerg(((1, 1), ()), ((
, (0, 0)), x)/e**n, True))/e + 2*A*a*b*d*Piec...

```

**Giac [B]** Leaf count of result is larger than twice the leaf count of optimal. 3415 vs.

2(164) = 328.

time = 1.35, size = 3415, normalized size = 21.34

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="giac")

[Out]  $(B*b^2*d*m^4*x*x^m*x^{(4*n)}*e^m + 6*B*b^2*d*m^3*n*x*x^m*x^{(4*n)}*e^m + 11*B*b^2*d*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 6*B*b^2*d*m*n^3*x*x^m*x^{(4*n)}*e^m + B*b^2*c*m^4*x*x^m*x^{(3*n)}*e^m + 2*B*a*b*d*m^4*x*x^m*x^{(3*n)}*e^m + A*b^2*d*m^4*x*x^m*x^{(3*n)}*e^m + 7*B*b^2*c*m^3*n*x*x^m*x^{(3*n)}*e^m + 14*B*a*b*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 7*A*b^2*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 14*B*b^2*c*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 28*B*a*b*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 14*A*b^2*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 8*B*b^2*c*m*n^3*x*x^m*x^{(3*n)}*e^m + 16*B*a*b*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 8*A*b^2*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 2*B*a*b*c*m^4*x*x^m*x^{(2*n)}*e^m + A*b^2*c*m^4*x*x^m*x^{(2*n)}*e^m + B*a^2*d*m^4*x*x^m*x^{(2*n)}*e^m + 2*A*a*b*d*m^4*x*x^m*x^{(2*n)}*e^m + 16*B*a*b*c*m^3*n*x*x^m*x^{(2*n)}*e^m + 8*A*b^2*c*m^3*n*x*x^m*x^{(2*n)}*e^m + 8*B*a^2*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 16*A*a*b*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 38*B*a*b*c*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 19*A*b^2*c*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 19*B*a^2*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 38*A*a*b*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 24*B*a*b*c*m*n^3*x*x^m*x^{(2*n)}*e^m + 12*A*b^2*c*m*n^3*x*x^m*x^{(2*n)}*e^m + 12*B*a^2*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 24*A*a*b*d*m*n^3*x*x^m*x^{(2*n)}*e^m + B*a^2*c*m^4*x*x^m*x^n*e^m + 2*A*a*b*c*m^4*x*x^m*x^n*e^m + A*a^2*d*m^4*x*x^m*x^n*e^m + 9*B*a^2*c*m^3*n*x*x^m*x^n*e^m + 18*A*a*b*c*m^3*n*x*x^m*x^n*e^m + 9*A*a^2*d*m^3*n*x*x^m*x^n*e^m + 26*B*a^2*c*m^2*n^2*x*x^m*x^n*e^m + 52*A*a*b*c*m^2*n^2*x*x^m*x^n*e^m + 26*A*a^2*d*m^2*n^2*x*x^m*x^n*e^m + 24*B*a^2*c*m*n^3*x*x^m*x^n*e^m + 48*A*a*b*c*m*n^3*x*x^m*x^n*e^m + 24*A*a^2*d*m*n^3*x*x^m*x^n*e^m + A*a^2*c*m^4*x*x^m*e^m + 10*A*a^2*c*m^3*n*x*x^m*e^m + 35*A*a^2*c*m^2*n^2*x*x^m*e^m + 50*A*a^2*c*m*n^3*x*x^m*e^m + 24*A*a^2*c*n^4*x*x^m*e^m + 4*B*b^2*d*m^3*x*x^m*x^{(4*n)}*e^m + 18*B*b^2*d*m^2*n*x*x^m*x^{(4*n)}*e^m + 22*B*b^2*d*m*n^2*x*x^m*x^{(4*n)}*e^m + 6*B*b^2*d*n^3*x*x^m*x^{(4*n)}*e^m + 4*B*b^2*c*m^3*x*x^m*x^{(3*n)}*e^m + 8*B*a*b*d*m^3*x*x^m*x^{(3*n)}*e^m + 4*A*b^2*d*m^3*x*x^m*x^{(3*n)}*e^m + 21*B*b^2*c*m^2*n*x*x^m*x^{(3*n)}*e^m + 42*B*a*b*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 21*A*b^2*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 28*B*b^2*c*m*n^2*x*x^m*x^{(3*n)}*e^m + 56*B*a*b*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 28*A*b^2*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 8*B*b^2*c*n^3*x*x^m*x^{(3*n)}*e^m + 16*B*a*b*d*n^3*x*x^m*x^{(3*n)}*e^m + 8*A*b^2*d*n^3*x*x^m*x^{(3*n)}*e^m + 8*B*a*b*c*m^3*x*x^m*x^{(2*n)}*e^m + 4*A*b^2*c*m^3*x*x^m*x^{(2*n)}*e^m + 4*B*a^2*d*m^3*x*x^m*x^{(2*n)}*e^m + 8*A*a*b*d*m^3*x*x^m*x^{(2*n)}*e^m + 48*B*a*b*c*m^2*n*x*x^m*x^{(2*n)}*e^m + 24*A*b^2*c*m^2*n*x*x^m*x^{(2*n)}*e^m + 24*B*a^2*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 48*A*a*b*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 76*B*a*b*c*m*n^2*x*x^m*x^{(2*n)}*e^m + 38*A*b^2*c*m*n^2*x*x^m*x^{(2*n)}*e^m + 38*B*a^2*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 76*A*a*b*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 24*B*a*b*c*n^3*x*x^m*x^{(2*n)}*e^m + 12*A*b^2*c*n^3*x*x^m*x^{(2*n)}*e^m + 12*B*a^2*d*n^3*x*x$

$x^{2n}e^m + 24A^2a^2b^2c^2d^2m^3x^{2n}e^m + 4B^2a^2c^2m^3x^{2n}e^m + 8A^2a^2b^2c^2m^3x^{2n}e^m + 4A^2a^2d^2m^3x^{2n}e^m + 27B^2a^2c^2m^2n^2x^{2n}e^m + 54A^2a^2b^2c^2m^2n^2x^{2n}e^m + 27A^2a^2d^2m^2n^2x^{2n}e^m + 52B^2a^2c^2m^2n^2x^{2n}e^m + 104A^2a^2b^2c^2m^2n^2x^{2n}e^m + 52A^2a^2d^2m^2n^2x^{2n}e^m + 24B^2a^2c^2n^3x^{2n}e^m + 48A^2a^2b^2c^2n^3x^{2n}e^m + 24A^2a^2d^2n^3x^{2n}e^m + 4A^2a^2c^2m^3x^{2n}e^m + 30A^2a^2c^2m^2n^2x^{2n}e^m + 70A^2a^2c^2m^2n^2x^{2n}e^m + 50A^2a^2c^2n^3x^{2n}e^m + 6B^2b^2d^2m^2x^{4n}e^m + 18B^2b^2d^2m^2n^2x^{4n}e^m + 11B^2b^2d^2n^2x^{4n}e^m + 6B^2b^2c^2m^2x^{3n}e^m + 12B^2a^2b^2d^2m^2x^{3n}e^m + 6A^2b^2d^2m^2x^{3n}e^m + 21B^2b^2c^2m^2n^2x^{3n}e^m + 42B^2a^2b^2d^2m^2n^2x^{3n}e^m + 21A^2b^2d^2m^2n^2x^{3n}e^m + 14B^2b^2c^2n^2x^{3n}e^m + 28B^2a^2b^2d^2n^2x^{3n}e^m + 14A^2b^2d^2n^2x^{3n}e^m + 12B^2a^2b^2c^2m^2x^{2n}e^m + 6A^2b^2c^2m^2x^{2n}e^m + 6B^2a^2d^2m^2x^{2n}e^m + 12A^2a^2b^2d^2m^2x^{2n}e^m + 48B^2a^2b^2c^2m^2n^2x^{2n}e^m + 24A^2b^2c^2m^2n^2x^{2n}e^m + 24B^2a^2d^2m^2n^2x^{2n}e^m + 48A^2a^2b^2d^2m^2n^2x^{2n}e^m + 38B^2a^2b^2c^2n^2x^{2n}e^m + 19A^2b^2c^2n^2x^{2n}e^m + 19B^2a^2d^2n^2x^{2n}e^m + 38A^2a^2b^2d^2n^2x^{2n}e^m + 6B^2a^2c^2m^2x^{2n}e^m + 12A^2a^2b^2c^2m^2x^{2n}e^m + 6A^2a^2d^2m^2x^{2n}e^m + 27B^2a^2c^2m^2n^2x^{2n}e^m + 54A^2a^2b^2c^2m^2n^2x^{2n}e^m + 27A^2a^2d^2m^2n^2x^{2n}e^m + 26B^2a^2c^2n^2x^{2n}e^m + 52A^2a^2b^2c^2n^2x^{2n}e^m + 26A^2a^2d^2n^2x^{2n}e^m + 6A^2a^2c^2m^2x^{2n}e^m + 30A^2a^2c^2m^2n^2x^{2n}e^m + 35A^2a^2c^2n^2x^{2n}e^m + 4B^2b^2d^2m^2x^{4n}e^m + 6B^2b^2d^2n^2x^{4n}e^m + 4B^2b^2c^2m^2x^{3n}e^m + 8B^2a^2b^2d^2m^2x^{3n}e^m + 4A^2b^2d^2m^2x^{3n}e^m + 7B^2b^2c^2n^2x^{3n}e^m + 14B^2a^2b^2d^2n^2x^{3n}e^m + 7A^2b^2d^2n^2x^{3n}e^m + 8B^2a^2b^2c^2m^2x^{2n}e^m + 4A^2b^2c^2m^2x^{2n}e^m + 4B^2a^2d^2m^2x^{2n}e^m + 8A^2a^2b^2d^2m^2x^{2n}e^m + 16B^2a^2b^2c^2n^2x^{2n}e^m + 8A^2b^2c^2n^2x^{2n}e^m + 8B^2a^2d^2n^2x^{2n}e^m + 16*...$

Mupad [B]

time = 5.23, size = 588, normalized size = 3.68

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Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)^2*(c + d*x^n), x)$

[Out]  $(x^{2n}(e*x)^m(A^2b^2c + B^2a^2d + 2A^2a^2b^2d + 2B^2a^2b^2c)(3m + 8n + 16m^2n + 19m^2n^2 + 8m^2n^2 + 3m^2 + m^3 + 19n^2 + 12n^3 + 1))/(4m + 10n + 30m^2n + 70m^2n^2 + 30m^2n^2 + 50m^2n^3 + 10m^3n + 6m^2 + 4m^3 + m^4 + 35n^2 + 50n^3 + 24n^4 + 35m^2n^2 + 1) + (A^2a^2c*x(e*x)^m)/(m + 1) + (a*x^n(e*x)^m(A^2a^2d + 2A^2a^2b^2c + B^2a^2c)(3m + 9n + 18m^2n + 26m^2n^2 + 9m^2n^2 + 3m^2 + m^3 + 26n^2 + 24n^3 + 1))/(4m + 10n + 30m^2n +$

$$\begin{aligned}
& 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + \\
& 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1) + (b*x*x^(3*n)*(e*x)^m*(A*b*d + 2*B*a*d \\
& + B*b*c)*(3*m + 7*n + 14*m*n + 14*m*n^2 + 7*m^2*n + 3*m^2 + m^3 + 14*n^2 + \\
& 8*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3* \\
& n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1) + (B*b \\
& ^2*d*x*x^(4*n)*(e*x)^m*(3*m + 6*n + 12*m*n + 11*m*n^2 + 6*m^2*n + 3*m^2 + m \\
& ^3 + 11*n^2 + 6*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m \\
& *n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n \\
& ^2 + 1)
\end{aligned}$$

### 3.3 $\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=108

$$\frac{(Abc + aBc + aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(bBc + Abd + aBd)x^{1+2n}(ex)^m}{1+m+2n} + \frac{bBdx^{1+3n}(ex)^m}{1+m+3n} + \frac{aAc(ex)^{1+m}}{e(1+m)}$$

[Out] (A\*a\*d+A\*b\*c+B\*a\*c)\*x^(1+n)\*(e\*x)^m/(1+m+n)+(A\*b\*d+B\*a\*d+B\*b\*c)\*x^(1+2\*n)\*(e\*x)^m/(1+m+2\*n)+b\*B\*d\*x^(1+3\*n)\*(e\*x)^m/(1+m+3\*n)+a\*A\*c\*(e\*x)^(1+m)/e/(1+m)

**Rubi [A]**

time = 0.06, antiderivative size = 108, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 3, integrand size = 27,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.111$ , Rules used = {584, 20, 30}

$$\frac{x^{n+1}(ex)^m(aAd + aBc + Abc)}{m+n+1} + \frac{x^{2n+1}(ex)^m(aBd + Abd + bBc)}{m+2n+1} + \frac{aAc(ex)^{m+1}}{e(m+1)} + \frac{bBdx^{3n+1}(ex)^m}{m+3n+1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] ((A\*b\*c + a\*B\*c + a\*A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + ((b\*B\*c + A\*b\*d + a\*B\*d)\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (b\*B\*d\*x^(1 + 3\*n)\*(e\*x)^m)/(1 + m + 3\*n) + (a\*A\*c\*(e\*x)^(1 + m))/(e\*(1 + m))

**Rule 20**

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_.)\*((b\_.)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

**Rule 30**

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

**Rule 584**

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_.)\*((e\_) + (f\_.)\*(x\_)^(n\_))^(r\_.), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

Rubi steps





$$a*d*m^n^2*x^n+5*A*b*c*m^2*n*x^n+5*B*a*c*m^2*n*x^n+11*A*a*c*n^2+4*B*a*d*m^2*n*(x^n)^2+6*A*a*c*n^3+A*a*c*m^3+3*A*a*c*m^2+B*b*c*(x^n)^2+8*B*b*c*m*n*(x^n)^2+10*A*a*d*m*n*x^n+6*B*b*d*m*n*(x^n)^3+3*B*a*c*m^2*x^n+6*B*a*c*n^2*x^n+B*b*d*m^3*(x^n)^3+A*b*d*m^3*(x^n)^2+B*a*d*m^3*(x^n)^2+B*b*c*m^3*(x^n)^2+3*B*b*d*m^2*(x^n)^3+3*B*b*c*n^2*(x^n)^2+3*A*a*d*m^2*x^n+6*A*a*d*n^2*x^n+3*A*b*c*m^2*x^n+6*A*b*c*n^2*x^n+12*A*a*c*m*n+2*B*b*d*n^2*(x^n)^3+A*a*d*m^3*x^n+A*b*c*m^3*x^n+3*A*b*d*m^2*(x^n)^2+3*A*b*d*n^2*(x^n)^2+B*a*c*m^3*x^n+6*A*a*c*m^2*n+11*A*a*c*m*n^2)/(1+m)/(1+m+n)/(1+m+2*n)/(1+m+3*n)*exp(1/2*m*(-I*Pi*csgn(I*e*x)^3+I*Pi*csgn(I*e*x)^2*csgn(I*e)+I*Pi*csgn(I*e*x)^2*csgn(I*x)-I*Pi*csgn(I*e*x)*csgn(I*e)*csgn(I*x)+2*ln(e)+2*ln(x)))$$

**Maxima** [A]

time = 0.32, size = 186, normalized size = 1.72

$$\frac{(xe)^{m+1} Aace^{-1}}{m+1} + \frac{Bbdze^{(m \log(x) + 3n \log(x) + m)}}{m+3n+1} + \frac{Bbcze^{(m \log(x) + 2n \log(x) + m)}}{m+2n+1} + \frac{Badze^{(m \log(x) + 2n \log(x) + m)}}{m+2n+1} + \frac{Abdze^{(m \log(x) + 2n \log(x) + m)}}{m+2n+1} + \frac{Bacze^{(m \log(x) + n \log(x) + m)}}{m+n+1} + \frac{Abcze^{(m \log(x) + n \log(x) + m)}}{m+n+1} + \frac{Aadze^{(m \log(x) + n \log(x) + m)}}{m+n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="maxima")

[Out] (x\*e)^(m + 1)\*A\*a\*c\*e^(-1)/(m + 1) + B\*b\*d\*x\*e^(m\*log(x) + 3\*n\*log(x) + m)/(m + 3\*n + 1) + B\*b\*c\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + B\*a\*d\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + A\*b\*d\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + B\*a\*c\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1) + A\*b\*c\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1) + A\*a\*d\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1)

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 550 vs. 2(111) = 222.

time = 2.00, size = 550, normalized size = 5.09

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="fricas")

[Out] ((B\*b\*d\*m^3 + 3\*B\*b\*d\*m^2 + 3\*B\*b\*d\*m + B\*b\*d + 2\*(B\*b\*d\*m + B\*b\*d)\*n^2 + 3\*(B\*b\*d\*m^2 + 2\*B\*b\*d\*m + B\*b\*d)\*n)\*x\*x^(3\*n)\*e^(m\*log(x) + m) + ((B\*b\*c + (B\*a + A\*b)\*d)\*m^3 + B\*b\*c + 3\*(B\*b\*c + (B\*a + A\*b)\*d)\*m^2 + 3\*(B\*b\*c + (B\*a + A\*b)\*d + (B\*b\*c + (B\*a + A\*b)\*d)\*m)\*n^2 + (B\*a + A\*b)\*d + 3\*(B\*b\*c + (B\*a + A\*b)\*d)\*m + 4\*(B\*b\*c + (B\*b\*c + (B\*a + A\*b)\*d)\*m^2 + (B\*a + A\*b)\*d + 2\*(B\*b\*c + (B\*a + A\*b)\*d)\*m)\*n)\*x\*x^(2\*n)\*e^(m\*log(x) + m) + ((A\*a\*d + (B\*a + A\*b)\*c)\*m^3 + A\*a\*d + 3\*(A\*a\*d + (B\*a + A\*b)\*c)\*m^2 + 6\*(A\*a\*d + (B\*a + A\*b)\*c + (A\*a\*d + (B\*a + A\*b)\*c)\*m)\*n^2 + (B\*a + A\*b)\*c + 3\*(A\*a\*d + (B\*a + A\*b)\*c)\*m + 5\*(A\*a\*d + (A\*a\*d + (B\*a + A\*b)\*c)\*m^2 + (B\*a + A\*b)\*c + 2\*(A\*a\*d + (B\*a + A\*b)\*c)\*m)\*n)\*x\*x^n\*e^(m\*log(x) + m) + (A\*a\*c\*m^3 + 6\*A\*a\*c\*n^3 + 3\*A\*a\*c\*m^2 + 3\*A\*a\*c\*m + A\*a\*c + 11\*(A\*a\*c\*m + A\*a\*c)\*n^2 + 6\*(A\*a\*c\*m^



```

ijerg((((), (1, 1)), ((0, 0), ()), x)/e**n + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**n, True))/e + A*b*d*Piecewise((x**(2*n)/(n*(e*x)**n), Ne(n, 0)), (log(x), True))/e + B*a*c*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**n, Abs(x) < 1), (-log(1/x)/e**n, 1/Abs(x) < 1), (-meijerg((((), (1, 1)), ((0, 0), ()), x)/e**n + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**n, True))/e + B*a*d*Piecewise((x**(2*n)/(n*(e*x)**n), Ne(n, 0)), (log(x), True))/e + B*b*c*Piecewise((x**(2*n)/(n*(e*x)**n), Ne(n, 0)), (log(x), True))/e + B*b*d*Piecewise((x**(3*n)/(2*n*(e*x)**n), Ne(n, 0)), (log(x), True))/e, Eq(m, -n - 1)), (A*a*c*m**3*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 6*A*a*c*m**2*n*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*a*c*m**2*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 11*A*a*c*m*n**2*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 12*A*a*c*m*n*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*a*c*m*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 6*A*a*c*n**3*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 11*A*a*c*n**2*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 6*A*a*c*n*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + A*a*c*x*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + A*a*d*m**3*x*x**n*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 5*A*a*d*m**2*n*x*x**n*(e*x)**m/(m**4 + 6*m**3*n + 4*m**3 + 11*m**2*n**2 + 18*m**2*n + 6*m**2 + 6*m*n**3 + 22*m*n**2 + 18*m*n + 4*m + 6*n**3 + 11*n**2 + 6*n + 1) + 3*A*a*d*m**2*x*x**n*(e*x)**m/(m...

```

**Giac [B]** Leaf count of result is larger than twice the leaf count of optimal. 1290 vs. 2(111) = 222.

time = 0.80, size = 1290, normalized size = 11.94

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="giac")

[Out] (B\*b\*d\*m^3\*x\*x^m\*x^(3\*n)\*e^m + 3\*B\*b\*d\*m^2\*n\*x\*x^m\*x^(3\*n)\*e^m + 2\*B\*b\*d\*m\*n^2\*x\*x^m\*x^(3\*n)\*e^m + B\*b\*c\*m^3\*x\*x^m\*x^(2\*n)\*e^m + B\*a\*d\*m^3\*x\*x^m\*x^(2\*

$$\begin{aligned}
& n) e^m + A b d m^3 x x^m x^{(2n)} e^m + 4 B b c m^2 n x x^m x^{(2n)} e^m + 4 B a d m^2 n x x^m x^{(2n)} e^m + 4 A a b d m^2 n x x^m x^{(2n)} e^m + 3 B b c m \\
& n^2 x x^m x^{(2n)} e^m + 3 B a d m n^2 x x^m x^{(2n)} e^m + 3 A a b d m n^2 x x \\
& x^m x^{(2n)} e^m + B a c m^3 x x^m x^n e^m + A b c m^3 x x^m x^n e^m + A a d \\
& m^3 x x^m x^n e^m + 5 B a c m^2 n x x^m x^n e^m + 5 A b c m^2 n x x^m x^n \\
& e^m + 5 A a d m^2 n x x^m x^n e^m + 6 B a c m n^2 x x^m x^n e^m + 6 A b c m \\
& n^2 x x^m x^n e^m + 6 A a d m n^2 x x^m x^n e^m + A a c m^3 x x^m e^m + 6 \\
& A a c m^2 n x x^m e^m + 11 A a c m n^2 x x^m e^m + 6 A a c n^3 x x^m e^m + \\
& 3 B b d m^2 x x^m x^{(3n)} e^m + 6 B b d m n x x^m x^{(3n)} e^m + 2 B b d n^2 \\
& x x^m x^{(3n)} e^m + 3 B b c m^2 x x^m x^{(2n)} e^m + 3 B a d m^2 x x^m x^{(2 \\
& n)} e^m + 3 A b d m^2 x x^m x^{(2n)} e^m + 8 B b c m n x x^m x^{(2n)} e^m + 8 \\
& B a d m n x x^m x^{(2n)} e^m + 8 A b d m n x x^m x^{(2n)} e^m + 3 B b c n^2 x \\
& x^m x^{(2n)} e^m + 3 B a d n^2 x x^m x^{(2n)} e^m + 3 A b d n^2 x x^m x^{(2n)} \\
& e^m + 3 B a c m^2 x x^m x^n e^m + 3 A b c m^2 x x^m x^n e^m + 3 A a d m^2 \\
& x x^m x^n e^m + 10 B a c m n x x^m x^n e^m + 10 A b c m n x x^m x^n e^m + \\
& 10 A a d m n x x^m x^n e^m + 6 B a c n^2 x x^m x^n e^m + 6 A b c n^2 x x^m \\
& x^n e^m + 6 A a d n^2 x x^m x^n e^m + 3 A a c m^2 x x^m e^m + 12 A a c m n \\
& x x^m e^m + 11 A a c n^2 x x^m e^m + 3 B b d m x x^m x^{(3n)} e^m + 3 B b d \\
& n x x^m x^{(3n)} e^m + 3 B b c m x x^m x^{(2n)} e^m + 3 B a d m x x^m x^{(2n)} \\
& e^m + 3 A b d m x x^m x^{(2n)} e^m + 4 B b c n x x^m x^{(2n)} e^m + 4 B a d \\
& n x x^m x^{(2n)} e^m + 4 A b d n x x^m x^{(2n)} e^m + 3 B a c m x x^m x^n e^ \\
& m + 3 A b c m x x^m x^n e^m + 3 A a d m x x^m x^n e^m + 5 B a c n x x^m x^n \\
& e^m + 5 A b c n x x^m x^n e^m + 5 A a d n x x^m x^n e^m + 3 A a c m x x^m \\
& e^m + 6 A a c n x x^m e^m + B b d x x^m x^{(3n)} e^m + B b c x x^m x^{(2n)} e \\
& m + B a d x x^m x^{(2n)} e^m + A b d x x^m x^{(2n)} e^m + B a c x x^m x^n e^ \\
& m + A b c x x^m x^n e^m + A a d x x^m x^n e^m + A a c x x^m e^m) / (m^4 + 6 m \\
& ^3 n + 11 m^2 n^2 + 6 m n^3 + 4 m^3 + 18 m^2 n + 22 m n^2 + 6 n^3 + 6 m^2 + \\
& 18 m n + 11 n^2 + 4 m + 6 n + 1)
\end{aligned}$$

**Mupad [B]**

time = 4.96, size = 271, normalized size = 2.51

$$\frac{A a c x (e x)^m}{m+1} + \frac{x x^{2n} (e x)^m (A b d + B a d + B b c) (m^2 + 4 m n + 2 m + 3 n^2 + 4 n + 1)}{m^3 + 6 m^2 n + 3 m^2 + 11 m n^2 + 12 m n + 3 m + 6 n^3 + 11 n^2 + 6 n + 1} + \frac{x x^n (e x)^m (A a d + A b c + B a c) (m^2 + 5 m n + 2 m + 6 n^2 + 5 n + 1)}{m^3 + 6 m^2 n + 3 m^2 + 11 m n^2 + 12 m n + 3 m + 6 n^3 + 11 n^2 + 6 n + 1} + \frac{B b d x x^{2n} (e x)^m (m^2 + 3 m n + 2 m + 2 n^2 + 3 n + 1)}{m^3 + 6 m^2 n + 3 m^2 + 11 m n^2 + 12 m n + 3 m + 6 n^3 + 11 n^2 + 6 n + 1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)\*(c + d\*x^n),x)

[Out] (A\*a\*c\*x\*(e\*x)^m)/(m + 1) + (x\*x^(2\*n)\*(e\*x)^m\*(A\*b\*d + B\*a\*d + B\*b\*c)\*(2\*m + 4\*n + 4\*m\*n + m^2 + 3\*n^2 + 1))/(3\*m + 6\*n + 12\*m\*n + 11\*m\*n^2 + 6\*m^2\*n + 3\*m^2 + m^3 + 11\*n^2 + 6\*n^3 + 1) + (x\*x^n\*(e\*x)^m\*(A\*a\*d + A\*b\*c + B\*a\*c)\*(2\*m + 5\*n + 5\*m\*n + m^2 + 6\*n^2 + 1))/(3\*m + 6\*n + 12\*m\*n + 11\*m\*n^2 + 6\*m^2\*n + 3\*m^2 + m^3 + 11\*n^2 + 6\*n^3 + 1) + (B\*b\*d\*x\*x^(3\*n)\*(e\*x)^m\*(2\*m + 3\*n + 3\*m\*n + m^2 + 2\*n^2 + 1))/(3\*m + 6\*n + 12\*m\*n + 11\*m\*n^2 + 6\*m^2\*n + 3\*m^2 + m^3 + 11\*n^2 + 6\*n^3 + 1)

### 3.4 $\int (ex)^m (A + Bx^n) (c + dx^n) dx$

Optimal. Leaf size=66

$$\frac{(Bc + Ad)x^{1+n}(ex)^m}{1 + m + n} + \frac{Bdx^{1+2n}(ex)^m}{1 + m + 2n} + \frac{Ac(ex)^{1+m}}{e(1 + m)}$$

[Out] (A\*d+B\*c)\*x^(1+n)\*(e\*x)^m/(1+m+n)+B\*d\*x^(1+2\*n)\*(e\*x)^m/(1+m+2\*n)+A\*c\*(e\*x)^(1+m)/e/(1+m)

Rubi [A]

time = 0.03, antiderivative size = 66, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 20,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.150$ , Rules used = {459, 20, 30}

$$\frac{x^{n+1}(ex)^m(Ad + Bc)}{m + n + 1} + \frac{Ac(ex)^{m+1}}{e(m + 1)} + \frac{Bdx^{2n+1}(ex)^m}{m + 2n + 1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n), x]

[Out] ((B\*c + A\*d)\*x^(1 + n)\*(e\*x)^m)/(1 + m + n) + (B\*d\*x^(1 + 2\*n)\*(e\*x)^m)/(1 + m + 2\*n) + (A\*c\*(e\*x)^(1 + m))/(e\*(1 + m))

Rule 20

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_.)\*((b\_.)\*(v\_))^(n\_.), x\_Symbol] := Dist[b^IntPart[n]\*(b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n]), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

Rule 30

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 459

Int[((e\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_.))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_.))^(q\_.), x\_Symbol] := Int[ExpandIntegrand[(e\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && IGtQ[p, 0] && IGtQ[q, 0]

Rubi steps

$$\begin{aligned}
\int (ex)^m (A + Bx^n) (c + dx^n) dx &= \int (Ac(ex)^m + (Bc + Ad)x^n(ex)^m + Bdx^{2n}(ex)^m) dx \\
&= \frac{Ac(ex)^{1+m}}{e(1+m)} + (Bd) \int x^{2n}(ex)^m dx + (Bc + Ad) \int x^n(ex)^m dx \\
&= \frac{Ac(ex)^{1+m}}{e(1+m)} + (Bdx^{-m}(ex)^m) \int x^{m+2n} dx + ((Bc + Ad)x^{-m}(ex)^m) \int x^n dx \\
&= \frac{(Bc + Ad)x^{1+n}(ex)^m}{1+m+n} + \frac{Bdx^{1+2n}(ex)^m}{1+m+2n} + \frac{Ac(ex)^{1+m}}{e(1+m)}
\end{aligned}$$

**Mathematica [A]**

time = 0.06, size = 49, normalized size = 0.74

$$x(ex)^m \left( \frac{Ac}{1+m} + \frac{(Bc + Ad)x^n}{1+m+n} + \frac{Bdx^{2n}}{1+m+2n} \right)$$

Antiderivative was successfully verified.

`[In] Integrate[(e*x)^m*(A + B*x^n)*(c + d*x^n), x]``[Out] x*(e*x)^m*((A*c)/(1 + m) + ((B*c + A*d)*x^n)/(1 + m + n) + (B*d*x^(2*n))/(1 + m + 2*n))`**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.06, size = 262, normalized size = 3.97

method	result
risch	$\frac{x(Bd^2m^2x^{2n} + Bdmnx^{2n} + Adm^2x^n + 2Admnx^n + Bcm^2x^n + 2Bcmnx^n + 2Bx^{2n}dm + Bx^{2n}dn + Ac m^2 + 3Ac mn + 2Ac n^2 + 2A x^n dn)}{...}$

Verification of antiderivative is not currently implemented for this CAS.

`[In] int((e*x)^m*(A+B*x^n)*(c+d*x^n), x, method=_RETURNVERBOSE)`

```
[Out] x*(B*d*m^2*(x^n)^2+B*d*m*n*(x^n)^2+A*d*m^2*x^n+2*A*d*m*n*x^n+B*c*m^2*x^n+2*B*c*m*n*x^n+2*B*(x^n)^2*d*m+B*(x^n)^2*d*n+A*c*m^2+3*A*c*m*n+2*A*c*n^2+2*A*x^n*d*m+2*A*x^n*d*n+2*B*x^n*c*m+2*B*x^n*c*n+d*(x^n)^2*B+2*A*c*m+3*A*c*n+d*x^n*A+c*B*x^n+A*c)/(1+m)/(1+m+n)/(1+m+2*n)*exp(1/2*m*(-I*Pi*csgn(I*e*x)^3+I*Pi*csgn(I*e*x)^2*csgn(I*e)+I*Pi*csgn(I*e*x)^2*csgn(I*x)-I*Pi*csgn(I*e*x)*csgn(I*e)*csgn(I*x)+2*ln(e)+2*ln(x)))
```

**Maxima [A]**

time = 0.31, size = 85, normalized size = 1.29

$$\frac{(xe)^{m+1} Ace^{(-1)}}{m+1} + \frac{Bdxe^{(m \log(x)+2n \log(x)+m)}}{m+2n+1} + \frac{Bcxe^{(m \log(x)+n \log(x)+m)}}{m+n+1} + \frac{Adxe^{(m \log(x)+n \log(x)+m)}}{m+n+1}$$





```

), (0, 0)), x)/e**n, True))/e + B*d*Piecewise((x**(2*n)/(n*(e*x)**n), Ne(n,
0)), (log(x), True))/e, Eq(m, -n - 1)), (A*c*m**2*x*(e*x)**m/(m**3 + 3*m**
2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 3*A*c*m*n*x*(e*
x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1
) + 2*A*c*m*x*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m +
2*n**2 + 3*n + 1) + 2*A*c*n**2*x*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*
n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 3*A*c*n*x*(e*x)**m/(m**3 + 3*m**2*
n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + A*c*x*(e*x)**m/(m
**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + A*d*
m**2*x*x**n*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2
*n**2 + 3*n + 1) + 2*A*d*m*n*x*x**n*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*
m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 2*A*d*m*x*x**n*(e*x)**m/(m**3 +
3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 2*A*d*n*x*
x**n*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 +
3*n + 1) + A*d*x*x**n*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*
n + 3*m + 2*n**2 + 3*n + 1) + B*c*m**2*x*x**n*(e*x)**m/(m**3 + 3*m**2*n + 3
*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 2*B*c*m*n*x*x**n*(e*x)
**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1)
+ 2*B*c*m*x*x**n*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*
m + 2*n**2 + 3*n + 1) + 2*B*c*n*x*x**n*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 +
2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + B*c*x*x**n*(e*x)**m/(m**3 + 3
*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + B*d*m**2*x*
x**(2*n)*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n*
**2 + 3*n + 1) + B*d*m*n*x*x**(2*n)*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m
*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + 2*B*d*m*x*x**(2*n)*(e*x)**m/(m**3
+ 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1) + B*d*n*x
*x**(2*n)*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n**2 + 6*m*n + 3*m + 2*n
**2 + 3*n + 1) + B*d*x*x**(2*n)*(e*x)**m/(m**3 + 3*m**2*n + 3*m**2 + 2*m*n*
**2 + 6*m*n + 3*m + 2*n**2 + 3*n + 1), True))

```

**Giac** [B] Leaf count of result is larger than twice the leaf count of optimal. 327 vs. 2(68) = 136.

time = 2.28, size = 327, normalized size = 4.95

$Bd^2xz^{2n} + Bd^2mz^{2n} + Bdm^2z^{2n} + Ad^2xz^{2n} + 2Bdmz^{2n} + 2Adm^2z^{2n} + 2A^2m^2z^{2n} + 3A^2mz^{2n} + 3A^2m^2z^{2n} + 2A^2m^2z^{2n} + 2Bdmz^{2n} + 2Bdm^2z^{2n} + 2Adm^2z^{2n} + 2Adm^2z^{2n} + 2Adm^2z^{2n} + 2Adm^2z^{2n} + 3A^2mz^{2n} + Bdm^2z^{2n} + Bdm^2z^{2n} + Adm^2z^{2n} + Adm^2z^{2n}$   
 $m^3 + 3m^2n + 2m^2 + 3n^2 + 6mn + 2n^2 + 3m + 3n + 1$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="giac")

```

[Out] (B*d*m^2*x*x^m*x^(2*n)*e^m + B*d*m*n*x*x^m*x^(2*n)*e^m + B*c*m^2*x*x^m*x^n*
e^m + A*d*m^2*x*x^m*x^n*e^m + 2*B*c*m*n*x*x^m*x^n*e^m + 2*A*d*m*n*x*x^m*x^n
*e^m + A*c*m^2*x*x^m*e^m + 3*A*c*m*n*x*x^m*e^m + 2*A*c*n^2*x*x^m*e^m + 2*B*
d*m*x*x^m*x^(2*n)*e^m + B*d*n*x*x^m*x^(2*n)*e^m + 2*B*c*m*x*x^m*x^n*e^m + 2
*A*d*m*x*x^m*x^n*e^m + 2*B*c*n*x*x^m*x^n*e^m + 2*A*d*n*x*x^m*x^n*e^m + 2*A*
c*m*x*x^m*e^m + 3*A*c*n*x*x^m*e^m + B*d*x*x^m*x^(2*n)*e^m + B*c*x*x^m*x^n*e

```

$$\frac{x^m + A*d*x*x^m*x^n*e^m + A*c*x*x^m*e^m}{(m^3 + 3*m^2*n + 2*m*n^2 + 3*m^2 + 6*m*n + 2*n^2 + 3*m + 3*n + 1)}$$

**Mupad [B]**

time = 4.83, size = 91, normalized size = 1.38

$$(e x)^m \left( \frac{A c x}{m+1} + \frac{x x^n (A d + B c) (m+2 n+1)}{m^2+3 m n+2 m+2 n^2+3 n+1} + \frac{B d x x^{2 n} (m+n+1)}{m^2+3 m n+2 m+2 n^2+3 n+1} \right)$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n),x)

[Out] (e\*x)^m\*((A\*c\*x)/(m + 1) + (x\*x^n\*(A\*d + B\*c)\*(m + 2\*n + 1))/(2\*m + 3\*n + 3\*m\*n + m^2 + 2\*n^2 + 1) + (B\*d\*x\*x^(2\*n)\*(m + n + 1))/(2\*m + 3\*n + 3\*m\*n + m^2 + 2\*n^2 + 1))

### 3.5 $\int \frac{(ex)^m(A+Bx^n)(c+dx^n)}{a+bx^n} dx$

**Optimal.** Leaf size=120

$$\frac{Bdx^{1+n}(ex)^m}{b(1+m+n)} + \frac{(bBc + Abd - aBd)(ex)^{1+m}}{b^2e(1+m)} + \frac{(Ab - aB)(bc - ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{ab^2e(1+m)}$$

[Out] B\*d\*x^(1+n)\*(e\*x)^m/b/(1+m+n)+(A\*b\*d-B\*a\*d+B\*b\*c)\*(e\*x)^(1+m)/b^2/e/(1+m)+(A\*b-B\*a)\*(-a\*d+b\*c)\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b\*x^n/a)/a/b^2/e/(1+m)

**Rubi [A]**

time = 0.08, antiderivative size = 120, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.138$ , Rules used = {584, 20, 30, 371}

$$\frac{(ex)^{m+1}(Ab - aB)(bc - ad) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{bx^n}{a}\right)}{ab^2e(m+1)} + \frac{(ex)^{m+1}(-aBd + Abd + bBc)}{b^2e(m+1)} + \frac{Bdx^{n+1}(ex)^m}{b(m+n+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n), x]

[Out] (B\*d\*x^(1 + n)\*(e\*x)^m)/(b\*(1 + m + n)) + ((b\*B\*c + A\*b\*d - a\*B\*d)\*(e\*x)^(1 + m))/(b^2\*e\*(1 + m)) + ((A\*b - a\*B)\*(b\*c - a\*d)\*(e\*x)^(1 + m)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(b\*x^n)/a])/(a\*b^2\*e\*(1 + m))

Rule 20

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_.)\*((b\_.)\*(v\_))^(n\_), x\_Symbol] :> Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m + n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

Rule 30

Int[(x\_)^(m\_.), x\_Symbol] :> Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 371

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Simp[a^p\*((c\*x)^(m + 1)/(c\*(m + 1)))\*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 584

```
Int[((g_)*(x_))^(m_)*((a_)+(b_)*(x_)^(n_))^(p_)*((c_)+(d_)*(x_)^(n_))^(q_)*((e_)+(f_)*(x_)^(n_))^(r_), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a+b*x^n)^p*(c+d*x^n)^q*(e+f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n) (c + dx^n)}{a + bx^n} dx &= \int \left( \frac{(bBc + Abd - aBd)(ex)^m}{b^2} + \frac{Bdx^n(ex)^m}{b} + \frac{(Ab - aB)(bc - ad)(ex)^m}{b^2(a + bx^n)} \right) dx \\ &= \frac{(bBc + Abd - aBd)(ex)^{1+m}}{b^2e(1+m)} + \frac{(Bd) \int x^n (ex)^m dx}{b} + \frac{((Ab - aB)(bc - ad)(ex)^{1+m})}{b^2} \\ &= \frac{(bBc + Abd - aBd)(ex)^{1+m}}{b^2e(1+m)} + \frac{(Ab - aB)(bc - ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}, -\frac{bx^n}{a}\right)}{ab^2e(1+m)} \\ &= \frac{Bdx^{1+n}(ex)^m}{b(1+m+n)} + \frac{(bBc + Abd - aBd)(ex)^{1+m}}{b^2e(1+m)} + \frac{(Ab - aB)(bc - ad)(ex)^{1+m}}{ab^2} \end{aligned}$$

**Mathematica [A]**

time = 0.18, size = 115, normalized size = 0.96

$$\frac{x(ex)^m (Ab^2c(1+m+n) - (Ab - aB)(bc - ad)(1+m+n) + abBd(1+m)x^n + (Ab - aB)(bc - ad)(1+m+n) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}, -\frac{bx^n}{a}\right))}{ab^2(1+m)(1+m+n)}$$

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(A + B*x^n)*(c + d*x^n))/(a + b*x^n), x]
```

```
[Out] (x*(e*x)^m*(A*b^2*c*(1 + m + n) - (A*b - a*B)*(b*c - a*d)*(1 + m + n) + a*b*B*d*(1 + m)*x^n + (A*b - a*B)*(b*c - a*d)*(1 + m + n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(b*x^n)/a]))/(a*b^2*(1 + m)*(1 + m + n))
```

**Maple [F]**

time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)}{a + bx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(A+B*x^n)*(c+d*x^n)/(a+b*x^n), x)
```

```
[Out] int((e*x)^m*(A+B*x^n)*(c+d*x^n)/(a+b*x^n), x)
```

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)/(a+b*x^n),x, algorithm="maxima")
```

```
[Out] ((b^2*c*e^m - a*b*d*e^m)*A - (a*b*c*e^m - a^2*d*e^m)*B)*integrate(x^m/(b^3*
x^n + a*b^2), x) + ((m*e^m + e^m)*B*b*d*x*e^(m*log(x) + n*log(x)) + ((m*e^m
+ (n + 1)*e^m)*A*b*d + ((m*e^m + (n + 1)*e^m)*b*c - (m*e^m + (n + 1)*e^m)*
a*d)*B)*x*x^m)/((m^2 + m*(n + 2) + n + 1)*b^2)
```

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)/(a+b*x^n),x, algorithm="fricas")
```

```
[Out] integral((B*d*x^(2*n) + A*c + (B*c + A*d)*x^n)*(x*e)^m/(b*x^n + a), x)
```

**Sympy** [C] Result contains complex when optimal does not.

time = 5.67, size = 666, normalized size = 5.55

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(A+B*x**n)*(c+d*x**n)/(a+b*x**n),x)
```

```
[Out] A*c*e**m*m*x*x**m*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1/n)*gamma(m/
n + 1/n)/(a*n**2*gamma(m/n + 1 + 1/n)) + A*c*e**m*x*x**m*lerchphi(b*x**n*ex
p_polar(I*pi)/a, 1, m/n + 1/n)*gamma(m/n + 1/n)/(a*n**2*gamma(m/n + 1 + 1/n
)) + A*d*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 +
1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + A*d*e**m*x*x**m*
x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1
/n)/(a*n*gamma(m/n + 2 + 1/n)) + A*d*e**m*x*x**m*x**n*lerchphi(b*x**n*exp_p
olar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n + 2
+ 1/n)) + B*c*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n
+ 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + B*c*e**m*x*
x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n +
1 + 1/n)/(a*n*gamma(m/n + 2 + 1/n)) + B*c*e**m*x*x**m*x**n*lerchphi(b*x**n*
exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n
+ 2 + 1/n)) + B*d*e**m*m*x*x**m*x**n*(2*n)*lerchphi(b*x**n*exp_polar(I*pi)/a
, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n**2*gamma(m/n + 3 + 1/n)) + 2*
B*d*e**m*x*x**m*x**n*(2*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/
n)*gamma(m/n + 2 + 1/n)/(a*n*gamma(m/n + 3 + 1/n)) + B*d*e**m*x*x**m*x**n*(2*
n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n
)/(a*n**2*gamma(m/n + 3 + 1/n))
```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(d\*x^n + c)\*(x\*e)^m/(b\*x^n + a), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(e x)^m (A + B x^n) (c + d x^n)}{a + b x^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n), x)

$$3.6 \quad \int \frac{(ex)^m (A+Bx^n)(c+dx^n)}{(a+bx^n)^2} dx$$

**Optimal.** Leaf size=177

$$\frac{d(Ab(1+m) - aB(1+m+n))(ex)^{1+m}}{ab^2e(1+m)n} + \frac{(Ab - aB)(ex)^{1+m}(c+dx^n)}{abn(a+bx^n)} + \frac{(bc(aB(1+m) - Ab(1+m+n)))}{abn(a+bx^n)}$$

[Out]  $-d*(A*b*(1+m)-a*B*(1+m+n))*(e*x)^{(1+m)}/a/b^2/e/(1+m)/n+(A*b-B*a)*(e*x)^{(1+m)}*(c+d*x^n)/a/b/e/n/(a+b*x^n)+(b*c*(a*B*(1+m)-A*b*(1+m-n))+a*d*(A*b*(1+m)-a*B*(1+m+n))*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/a^2/b^2/e/(1+m)/n$

**Rubi [A]**

time = 0.16, antiderivative size = 177, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {608, 470, 371}

$$\frac{(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{bx^n}{a}\right) (bc(aB(m+1) - Ab(m-n+1)) + ad(Ab(m+1) - aB(m+n+1)))}{a^2b^2e(m+1)n} - \frac{d(ex)^{m+1}(Ab(m+1) - aB(m+n+1))}{ab^2e(m+1)n} + \frac{(ex)^{m+1}(Ab - aB)(c+dx^n)}{abn(a+bx^n)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^2, x]

[Out]  $-((d*(A*b*(1+m) - a*B*(1+m+n))*(e*x)^{(1+m)})/(a*b^2*e*(1+m)*n)) + ((A*b - a*B)*(e*x)^{(1+m)}*(c + d*x^n))/(a*b*e*n*(a + b*x^n)) + ((b*c*(a*B*(1+m) - A*b*(1+m-n)) + a*d*(A*b*(1+m) - a*B*(1+m+n)))*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((b*x^n)/a)])/(a^2*b^2*e*(1+m)*n)$

Rule 371

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Simp[a^p \* ((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 470

Int[((e\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_)), x\_Symbol] :> Simp[d\*(e\*x)^(m+1)\*((a + b\*x^n)^(p+1)/(b\*e\*(m+n\*(p+1)+1))), x] - Dist[(a\*d\*(m+1) - b\*c\*(m+n\*(p+1)+1))/(b\*(m+n\*(p+1)+1)), Int[(e\*x)^m\*(a + b\*x^n)^p, x], x] /; FreeQ[{a, b, c, d, e, m, n, p}, x] && NeQ[b\*c - a\*d, 0] && NeQ[m + n\*(p+1) + 1, 0]

Rule 608

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_.)\*((e\_) + (f\_.)\*(x\_)^(n\_)), x\_Symbol] :> Simp[(-b\*e - a\*f)\*(g\*x)^(

$m + 1) * (a + b * x^n)^{(p + 1)} * ((c + d * x^n)^q / (a * b * g * n * (p + 1)))$ ,  $x] + \text{Dist}[1 / (a * b * n * (p + 1)), \text{Int}[(g * x)^m * (a + b * x^n)^{(p + 1)} * (c + d * x^n)^{(q - 1)} * \text{Simp}[c * (b * e * n * (p + 1) + (b * e - a * f) * (m + 1)) + d * (b * e * n * (p + 1) + (b * e - a * f) * (m + n * q + 1)) * x^n, x], x], x] /;$   $\text{FreeQ}[\{a, b, c, d, e, f, g, m, n\}, x] \&\& \text{LtQ}[p, -1] \&\& \text{GtQ}[q, 0] \&\& \text{!(EqQ}[q, 1] \&\& \text{SimplerQ}[b * c - a * d, b * e - a * f])$

Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n) (c + dx^n)}{(a + bx^n)^2} dx &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)}{aben (a + bx^n)} - \int \frac{(ex)^m (-c(aB(1+m) - Ab(1+m-n)) + d(Ab(1+m) - aB(1+m-n)))}{a + bx^n} dx \\ &= -\frac{d(Ab(1+m) - aB(1+m+n))(ex)^{1+m}}{ab^2e(1+m)n} + \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)}{aben (a + bx^n)} \\ &= -\frac{d(Ab(1+m) - aB(1+m+n))(ex)^{1+m}}{ab^2e(1+m)n} + \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)}{aben (a + bx^n)} \end{aligned}$$

Mathematica [A]

time = 0.25, size = 195, normalized size = 1.10

$$\frac{x(ex)^m \left( -a^2 B d + ab(Bc + Ad) + \frac{Ab^2 c(-1-m+n)}{1+m} + \frac{Ab(-ad(1+m) + bc(1+m-n) + aB(-bc(1+m) + ad(1+m+n))}{1+m} + \frac{a(-Ab + aB)(-bc + ad)}{a + bx^n} - \frac{(Ab(-ad(1+m) + bc(1+m-n)) + aB(-bc(1+m) + ad(1+m+n))) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{1+m} \right)}{a^2 b^2 n}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^2,x]

[Out]  $(x*(e*x)^m*(-(a^2*B*d) + a*b*(B*c + A*d) + (A*b^2*c*(-1 - m + n))/(1 + m) + (A*b*(-(a*d*(1 + m)) + b*c*(1 + m - n)) + a*B*(-(b*c*(1 + m)) + a*d*(1 + m + n)))/(1 + m) + (a*(-(A*b) + a*B)*(-(b*c) + a*d))/(a + b*x^n) - ((A*b*(-(a*d*(1 + m)) + b*c*(1 + m - n)) + a*B*(-(b*c*(1 + m)) + a*d*(1 + m + n)))*\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)]/(1 + m))/(a^2 * b^2 * n)$

Maple [F]

time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)}{(a + bx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^2,x)

[Out] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^2,x)



**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^2,x, algorithm="maxima")

[Out]  $-\left(\left(m e^m - (n - 1) e^m\right) b^2 c - \left(m e^m + e^m\right) a b d\right) A - \left(\left(m e^m + e^m\right) a b^2 c - \left(m e^m + (n + 1) e^m\right) a^2 d\right) B \int \frac{x^m}{\left(a b^3 n x^n + a^2 b^2 n\right)} dx + \left(B a b d n x e^{(m \log(x) + n \log(x) + m)} + \left(\left(m e^m + e^m\right) b^2 c - \left(m e^m + e^m\right) a b d\right) A - \left(\left(m e^m + e^m\right) a b^2 c - \left(m e^m + (n + 1) e^m\right) a^2 d\right) B\right) x^m / \left(\left(m n + n\right) a b^3 x^n + \left(m n + n\right) a^2 b^2\right)$

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^2,x, algorithm="fricas")

[Out]  $\int \frac{\left(B d x^{2 n} + A c + \left(B c + A d\right) x^n\right) \left(x e\right)^m}{\left(b^2 x^{2 n} + 2 a b x^n + a^2\right)} dx$

**Sympy [C]** Result contains complex when optimal does not.

time = 31.57, size = 4129, normalized size = 23.33

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)/(a+b\*x\*\*n)\*\*2,x)

[Out]  $A c \left(-e^{m m} x^{2 n} x^{m m} \operatorname{lerchphi}\left(b x^{n n} \exp _{\text {polar }}\left(I \pi\right) / a, 1, m / n + 1 / n\right) \operatorname{gamma}\left(m / n + 1 / n\right) / \left(a\left(a^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right) + b^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right)\right)\right) + e^{m m} m^n x^{n n} x^{m m} \operatorname{lerchphi}\left(b x^{n n} \exp _{\text {polar }}\left(I \pi\right) / a, 1, m / n + 1 / n\right) \operatorname{gamma}\left(m / n + 1 / n\right) / \left(a\left(a^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right) + b^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right)\right)\right) + e^{m m} m^n x^{n n} x^{m m} \operatorname{gamma}\left(m / n + 1 / n\right) / \left(a\left(a^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right) + b^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right)\right)\right) - 2 e^{m m} m^n x^{n n} x^{m m} \operatorname{lerchphi}\left(b x^{n n} \exp _{\text {polar }}\left(I \pi\right) / a, 1, m / n + 1 / n\right) \operatorname{gamma}\left(m / n + 1 / n\right) / \left(a\left(a^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right) + b^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right)\right)\right) + e^{m m} m^n x^{n n} x^{m m} \operatorname{lerchphi}\left(b x^{n n} \exp _{\text {polar }}\left(I \pi\right) / a, 1, m / n + 1 / n\right) \operatorname{gamma}\left(m / n + 1 / n\right) / \left(a\left(a^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right) + b^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right)\right)\right) + e^{m m} m^n x^{n n} x^{m m} \operatorname{gamma}\left(m / n + 1 / n\right) / \left(a\left(a^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right) + b^{n n} x^{3 n} \operatorname{gamma}\left(m / n + 1 + 1 / n\right)\right)\right) - e^{m m} m^n x^{n n} x^{m m} \operatorname{lerchphi}\left(b x^{n n} \exp _{\text {polar }}\left(I \pi\right) / a, 1, m / n + 1 / n\right) \operatorname{gamma}\left(m / n + 1 / n\right)$

$$\begin{aligned}
& / (a*(a^{n+3}\Gamma(m/n + 1 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 1 + 1/n))) - b^e \\
& **m**2*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1/n)*\Gamma \\
& (m/n + 1/n)/(a**2*(a^{n+3}\Gamma(m/n + 1 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 1 \\
& + 1/n))) + b^e**m**n*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n \\
& + 1/n)*\Gamma(m/n + 1/n)/(a**2*(a^{n+3}\Gamma(m/n + 1 + 1/n) + b^{n+3}x^{n+3}\Gamma \\
& (m/n + 1 + 1/n))) - 2*b^e**m**m*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi) \\
& /a, 1, m/n + 1/n)*\Gamma(m/n + 1/n)/(a**2*(a^{n+3}\Gamma(m/n + 1 + 1/n) + \\
& b^{n+3}x^{n+3}\Gamma(m/n + 1 + 1/n))) + b^e**m**n*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp \\
& _{\text{polar}}(I\pi)/a, 1, m/n + 1/n)*\Gamma(m/n + 1/n)/(a**2*(a^{n+3}\Gamma(m/n + \\
& 1 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 1 + 1/n))) - b^e**m**x*x**m*x**n*\text{lerchphi} \\
& (b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1/n)*\Gamma(m/n + 1/n)/(a**2*(a^{n+3}\Gamma \\
& (m/n + 1 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 1 + 1/n))) + A*d*(-e**m**2*x \\
& *x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1/n)*\Gamma(m/n + \\
& 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n \\
& ))) - e**m**n*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1 + \\
& 1/n)*\Gamma(m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma \\
& (m/n + 2 + 1/n))) + e**m**n*x*x**m*x**n*\Gamma(m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma \\
& (m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) - 2*e**m**m*x*x**m \\
& *x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1/n)*\Gamma(m/n + 1 + \\
& 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) + \\
& e**m**n**2*x*x**m*x**n*\Gamma(m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) \\
& + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) - e**m**n*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp \\
& _{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1/n)*\Gamma(m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + \\
& 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) + e**m**n*x*x**m*x**n*\Gamma \\
& (m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + \\
& 2 + 1/n))) - e**m**x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + \\
& 1 + 1/n)*\Gamma(m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3} \\
& *n*\Gamma(m/n + 2 + 1/n))) - b^e**m**m**2*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp \\
& _{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1/n)*\Gamma(m/n + 1 + 1/n)/(a**2*(a^{n+3}\Gamma(m/n + \\
& 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) - b^e**m**m**n*x*x**m*x**n*( \\
& 2*n)*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1/n)*\Gamma(m/n + 1 + 1 \\
& /n)/(a**2*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) \\
& - 2*b^e**m**m*x*x**m*x**n*(2*n)*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1 \\
& + 1/n)*\Gamma(m/n + 1 + 1/n)/(a**2*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3} \\
& *n*\Gamma(m/n + 2 + 1/n))) - b^e**m**n*x*x**m*x**n*(2*n)*\text{lerchphi}(b*x^{n+3}\exp \\
& _{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1/n)*\Gamma(m/n + 1 + 1/n)/(a**2*(a^{n+3}\Gamma(m/n \\
& + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) - b^e**m**x*x**m*x**n*(2*n)*\text{l} \\
& \text{erchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1/n)*\Gamma(m/n + 1 + 1/n)/(a \\
& **2*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n)))) + B* \\
& c*(-e**m**2*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a, 1, m/n + 1 + 1 \\
& /n)*\Gamma(m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma \\
& (m/n + 2 + 1/n))) - e**m**m**n*x*x**m*x**n*\text{lerchphi}(b*x^{n+3}\exp_{\text{polar}}(I\pi)/a \\
& , 1, m/n + 1 + 1/n)*\Gamma(m/n + 1 + 1/n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + \\
& b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) + e**m**m**n*x*x**m*x**n*\Gamma(m/n + 1 + 1 \\
& /n)/(a*(a^{n+3}\Gamma(m/n + 2 + 1/n) + b^{n+3}x^{n+3}\Gamma(m/n + 2 + 1/n))) -
\end{aligned}$$

```

2*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*g
amma(m/n + 1 + 1/n)/(a*(a*n**3*gamma(m/n + 2 + 1/n) + b*n**3*x**n*gamma(m/n
+ 2 + 1/n))) + e**m*n**2*x*x**m*x**n*gamma(m/n + 1 + 1/n)/(a*(a*n**3*gamma
(m/n + 2 + 1/n) + b*n**3*x**n*gamma(m/n + 2 + 1/n))) - e**m*n*x*x**m*x**n*l
erchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a
*(a*n**3*gamma(m/n + 2 + 1/n) + b*n**3*x**n*gamma(m/n + 2 + 1/n))) + e**m*n
*x*x**m*x**n*gamma(m/n + 1 + 1/n)/(a*(a*n**3*gamma(m/n + 2 + 1/n) + b*n**3*
x**n*gamma(m/n + 2 + 1/n))) - e**m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*
pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*(a*n**3*gamma(m/n + 2 + 1/
n) + b*n**3*x**n*gamma(m/n + 2 + 1/n))) - b*e**...

```

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^2,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(d\*x^n + c)\*(x\*e)^m/(b\*x^n + a)^2, x)

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)}{(a + bx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^2,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^2, x)

$$3.7 \quad \int \frac{(ex)^m (A+Bx^n)(c+dx^n)}{(a+bx^n)^3} dx$$

**Optimal.** Leaf size=228

$$\frac{(Ab(bc(1+m-2n) - ad(1+m-n)) - aB(bc(1+m) - ad(1+m+n)))(ex)^{1+m}}{2a^2b^2en^2(a+bx^n)} + \frac{(Ab - aB)(ex)^{1+m}(c+dx^n)}{2abn(a+bx^n)}$$

[Out]  $-1/2*(A*b*(b*c*(1+m-2*n)-a*d*(1+m-n))-a*B*(b*c*(1+m)-a*d*(1+m+n))*(e*x)^{(1+m)}/a^2/b^2/e/n^2/(a+b*x^n)+1/2*(A*b-B*a)*(e*x)^{(1+m)*(c+d*x^n)}/a/b/e/n/(a+b*x^n)^2-1/2*(b*c*(a*B*(1+m)-A*b*(1+m-2*n))*(1+m-n)+a*d*(1+m)*(A*b*(1+m-n)-a*B*(1+m+n)))*(e*x)^{(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)}/a^3/b^2/e/(1+m)/n^2$

**Rubi [A]**

time = 0.19, antiderivative size = 227, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {608, 468, 371}

$$\frac{(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+1}{n}; -\frac{bc}{a}\right) (bc(m-n+1)(aB(m+1) - Ab(m-2n+1)) + ad(m+1)(Ab(m-n+1) - aB(m+n+1)))}{2a^2b^2e(m+1)n^2} + \frac{(ex)^{m+1}(bc(aB(m+1) - Ab(m-2n+1)) + ad(Ab(m-n+1) - aB(m+n+1)))}{2a^2b^2en^2(a+bx^n)} + \frac{(ex)^{m+1}(Ab - aB)(c+dx^n)}{2abn(a+bx^n)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^3,x]

[Out]  $((b*c*(a*B*(1+m) - A*b*(1+m-2*n)) + a*d*(A*b*(1+m-n) - a*B*(1+m+n)))*(e*x)^{(1+m)}/(2*a^2*b^2*e*n^2*(a+b*x^n)) + ((A*b - a*B)*(e*x)^{(1+m)*(c+d*x^n)}/(2*a*b*e*n*(a+b*x^n)^2) - ((b*c*(a*B*(1+m) - A*b*(1+m-2*n))*(1+m-n) + a*d*(1+m)*(A*b*(1+m-n) - a*B*(1+m+n)))*(e*x)^{(1+m)*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(b*x^n)/a]})/(2*a^3*b^2*e*(1+m)*n^2)$

**Rule 371**

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

**Rule 468**

Int[((e\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_)), x\_Symbol] := Simp[(-b\*c - a\*d)\*(e\*x)^(m+1)\*((a + b\*x^n)^(p+1)/(a\*b\*e\*n\*(p+1))), x] - Dist[(a\*d\*(m+1) - b\*c\*(m+n\*(p+1)+1))/(a\*b\*n\*(p+1)), Int[(e\*x)^m\*(a + b\*x^n)^(p+1), x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && LtQ[p, -1] && (( !IntegerQ[p + 1/2] && NeQ[p, -5/4]) || !RationalQ[m] || (IGtQ[n, 0] && ILtQ[p + 1/2, 0] && LeQ[-1,

m, (-n)\*(p + 1]]))

### Rule 608

```
Int[((g_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_))^(p_.)*((c_.) + (d_.)*(x_)^(n_))^(q_.)*((e_.) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^q/(a*b*g*n*(p + 1))), x] + Dist[1/(a*b*n*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^(q - 1)*Simp[c*(b*e*n*(p + 1) + (b*e - a*f)*(m + 1)) + d*(b*e*n*(p + 1) + (b*e - a*f)*(m + n*q + 1))*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b*c - a*d, b*e - a*f])
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)(c + dx^n)}{(a + bx^n)^3} dx &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)}{2abn(a + bx^n)^2} - \frac{\int \frac{(ex)^m (-c(aB(1+m) - Ab(1+m-2n)) + d(Ab(1+m) - aB(1+m-2n))}{(a + bx^n)^2} dx}{2abn} \\ &= -\frac{(Ab(bc(1+m-2n) - ad(1+m-n)) - aB(bc(1+m) - ad(1+m-n))}{2a^2b^2en^2(a + bx^n)} \\ &= -\frac{(Ab(bc(1+m-2n) - ad(1+m-n)) - aB(bc(1+m) - ad(1+m-n))}{2a^2b^2en^2(a + bx^n)} \end{aligned}$$

**Mathematica** [B] Leaf count is larger than twice the leaf count of optimal. 1153 vs. 2(228) = 456.

time = 0.57, size = 1153, normalized size = 5.06

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^3,x]

[Out] (x\*(e\*x)^m\*(a^2\*A\*b^2\*c\*(1 + m)\*n - a^3\*b\*B\*c\*(1 + m)\*n - a^3\*A\*b\*d\*(1 + m)\*n + a^4\*B\*d\*(1 + m)\*n - a\*A\*b^2\*c\*(1 + m)\*(a + b\*x^n) + a^2\*b\*B\*c\*(1 + m)\*(a + b\*x^n) + a^2\*A\*b\*d\*(1 + m)\*(a + b\*x^n) - a^3\*B\*d\*(1 + m)\*(a + b\*x^n) - a\*A\*b^2\*c\*m\*(1 + m)\*(a + b\*x^n) + a^2\*b\*B\*c\*m\*(1 + m)\*(a + b\*x^n) + a^2\*A\*b\*d\*m\*(1 + m)\*(a + b\*x^n) - a^3\*B\*d\*m\*(1 + m)\*(a + b\*x^n) + 2\*a\*A\*b^2\*c\*(1 + m)\*n\*(a + b\*x^n) - 2\*a^3\*B\*d\*(1 + m)\*n\*(a + b\*x^n) + A\*b^2\*c\*(a + b\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)] - a\*b\*B\*c\*(a + b\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)] - a\*A\*b\*d\*(a + b\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)] + a^2\*B\*d\*(a + b\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)

$$\begin{aligned} &/n, -((b*x^n)/a)] + 2*A*b^2*c*m*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/ \\ &n, (1 + m + n)/n, -((b*x^n)/a)] - 2*a*b*B*c*m*(a + b*x^n)^2*Hypergeometric2 \\ &F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 2*a*A*b*d*m*(a + b*x^n)^2*H \\ &ypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 2*a^2*B*d*m*( \\ &a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + \\ &A*b^2*c*m^2*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, - \\ &((b*x^n)/a)] - a*b*B*c*m^2*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 \\ &+ m + n)/n, -((b*x^n)/a)] - a*A*b*d*m^2*(a + b*x^n)^2*Hypergeometric2F1[1, \\ &(1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + a^2*B*d*m^2*(a + b*x^n)^2*Hyperg \\ &eometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 3*A*b^2*c*n*(a + b \\ &*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + a*b* \\ &B*c*n*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n) \\ &)/a)] + a*A*b*d*n*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n) \\ &/n, -((b*x^n)/a)] + a^2*B*d*n*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, \\ &(1 + m + n)/n, -((b*x^n)/a)] - 3*A*b^2*c*m*n*(a + b*x^n)^2*Hypergeometric2 \\ &F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + a*b*B*c*m*n*(a + b*x^n)^2*H \\ &ypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + a*A*b*d*m*n*( \\ &a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + \\ &a^2*B*d*m*n*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, - \\ &((b*x^n)/a)] + 2*A*b^2*c*n^2*(a + b*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, \\ &(1 + m + n)/n, -((b*x^n)/a)))/(2*a^3*b^2*(1 + m)*n^2*(a + b*x^n)^2) \end{aligned}$$

**Maple [F]**

time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)(c + dx^n)}{(a + bx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^3,x)

[Out] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^3,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^3,x, algorithm="maxima")

[Out] (((m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*b^2\*c - (m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a\*b\*d)\*A - ((m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a\*b\*c - (m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a^2\*d)\*B)\*integrate(1/2\*x^m/(a^2\*b^3\*n^2\*x^n + a^3\*b^2\*n^2), x) - 1/2\*(((m\*e^m - (3\*n - 1)\*e^m)\*a\*b^2\*c - (m\*e^m - (n - 1)\*e^m)\*a^2\*b\*d)\*A - ((m\*e^m - (n - 1)\*e^m)\*a^2\*b\*c

$$- (m e^m + (n + 1) e^m) a^{3d} B) x x^m + (((m e^m - (2n - 1) e^m) b^3 c - (m e^m + e^m) a b^2 d) A - ((m e^m + e^m) a b^2 c - (m e^m + (2n + 1) e^m) a^2 b d) B) x x e^{(m \log(x) + n \log(x))} / (a^2 b^4 n^2 x^{2n} + 2 a^3 b^3 n^2 x^n + a^4 b^2 n^2)$$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^3,x, algorithm="fricas")

[Out] integral((B\*d\*x^(2\*n) + A\*c + (B\*c + A\*d)\*x^n)\*(x\*e)^m/(b^3\*x^(3\*n) + 3\*a\*b^2\*x^(2\*n) + 3\*a^2\*b\*x^n + a^3), x)

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)/(a+b\*x\*\*n)\*\*3,x)

[Out] Timed out

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)/(a+b\*x^n)^3,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(d\*x^n + c)\*(x\*e)^m/(b\*x^n + a)^3, x)

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(e x)^m (A + B x^n) (c + d x^n)}{(a + b x^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^3,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n))/(a + b\*x^n)^3, x)

### 3.8 $\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=318

$$\frac{a^2c(3Abc + aBc + 2aAd)x^{1+n}(ex)^m}{1 + m + n} + \frac{a(aBc(3bc + 2ad) + A(3b^2c^2 + 6abcd + a^2d^2))x^{1+2n}(ex)^m}{1 + m + 2n} + \frac{(aB(3b^2c^2 + 6abcd + a^2d^2))x^{1+3n}(ex)^m}{1 + m + 3n} + \frac{(a^2c(2Ad + aBc + 3Abc) + b^2d(3a^2d + 3abd(Ad + 2Bc) + b^2c(2Ad + Bc)))x^{1+4n}(ex)^m}{1 + m + 4n} + \frac{(b^3Bd^2 + 3a^2b^2d^2 + 3a^2b^2d^2)x^{1+5n}(ex)^m}{1 + m + 5n} + \frac{(a^3Ac^2 + 3a^2b^2d^2)x^{1+6n}(ex)^m}{1 + m + 6n} + \frac{a^3Ac^2(e^x)^{1+m}}{e^{1+m}}$$

[Out]  $a^2c*(2*A*a*d+3*A*b*c+B*a*c)*x^{(1+n)}*(e*x)^m/(1+m+n)+a*(a*B*c*(2*a*d+3*b*c)+A*(a^2*d^2+6*a*b*c*d+3*b^2*c^2))*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+(a*B*(a^2*d^2+6*a*b*c*d+3*b^2*c^2)+A*b*(3*a^2*d^2+6*a*b*c*d+b^2*c^2))*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+b*(3*a^2*B*d^2+3*a*b*d*(A*d+2*B*c)+b^2*c*(2*A*d+B*c))*x^{(1+4*n)}*(e*x)^m/(1+m+4*n)+b^2*d*(A*b*d+3*B*a*d+2*B*b*c)*x^{(1+5*n)}*(e*x)^m/(1+m+5*n)+b^3*B*d^2*x^{(1+6*n)}*(e*x)^m/(1+m+6*n)+a^3*A*c^2*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.28, antiderivative size = 318, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {584, 20, 30}

$$\frac{a^3Ac^2(e^x)^{m+1}}{e^{m+1}} + \frac{a^{2n+1}(ex)^m(A(a^2d^2 + 6abcd + 3b^2c^2) + aB(2ad + 3bc))}{m + 2n + 1} + \frac{a^{2n+1}(ex)^m(A(3a^2d^2 + 6abcd + b^2c^2) + aB(a^2d^2 + 6abcd + 3b^2c^2))}{m + 3n + 1} + \frac{b^{2n+1}(ex)^m(3a^2Bd^2 + 3abd(Ad + 2Bc) + b^2c(2Ad + Bc))}{m + 4n + 1} + \frac{a^2c^{n+1}(ex)^m(2aAd + aBc + 3Abc)}{m + n + 1} + \frac{b^2d^{n+1}(ex)^m(3aBd + Abd + 2bBc)}{m + 5n + 1} + \frac{b^3Bd^2(e^x)^m}{m + 6n + 1}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(a + b*x^n)^3*(A + B*x^n)*(c + d*x^n)^2,x]$

[Out]  $(a^2c*(3*A*b*c + a*B*c + 2*a*A*d)*x^{(1 + n)}*(e*x)^m)/(1 + m + n) + (a*(a*B*c*(3*b*c + 2*a*d) + A*(3*b^2*c^2 + 6*a*b*c*d + a^2*d^2))*x^{(1 + 2*n)}*(e*x)^m)/(1 + m + 2*n) + ((a*B*(3*b^2*c^2 + 6*a*b*c*d + a^2*d^2) + A*b*(b^2*c^2 + 6*a*b*c*d + 3*a^2*d^2))*x^{(1 + 3*n)}*(e*x)^m)/(1 + m + 3*n) + (b*(3*a^2*B*d^2 + 3*a*b*d*(2*B*c + A*d) + b^2*c*(B*c + 2*A*d))*x^{(1 + 4*n)}*(e*x)^m)/(1 + m + 4*n) + (b^2*d*(2*b*B*c + A*b*d + 3*a*B*d))*x^{(1 + 5*n)}*(e*x)^m/(1 + m + 5*n) + (b^3*B*d^2*x^{(1 + 6*n)}*(e*x)^m)/(1 + m + 6*n) + (a^3*A*c^2*(e*x)^{(1 + m)})/(e*(1 + m))$

**Rule 20**

$\text{Int}[(u_*)*((a_*)*(v_))^{(m_*)}*((b_*)*(v_))^{(n_*)}, x\_Symbol] := \text{Dist}[b^{\text{IntPart}[n]}*((b*v)^{\text{FracPart}[n]}/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]})), \text{Int}[u*(a*v)^{(m+n)}, x], x] /;$  FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

**Rule 30**

$\text{Int}[(x_*)^{(m_*)}, x\_Symbol] := \text{Simp}[x^{(m+1)}/(m+1), x] /;$  FreeQ[m, x] && N eQ[m, -1]

**Rule 584**



```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] :> Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^2 dx &= \int (a^3 Ac^2 (ex)^m + a^2 c(3Abc + aBc + 2aAd)x^n (ex)^m + a(aBc(3bc + 2ad) + b^3 Bd^2)x^{2n} (ex)^m + a^2 c(3Abc + aBc + 2aAd)x^{3n} (ex)^m) dx \\ &= \frac{a^3 Ac^2 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^2) \int x^{6n} (ex)^m dx + (a^2 c(3Abc + aBc + 2aAd)) \int x^{m+6n} (ex)^m dx \\ &= \frac{a^3 Ac^2 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^2 x^{-m} (ex)^m) \int x^{m+6n} dx + (a^2 c(3Abc + aBc + 2aAd)) \int x^{m+6n} (ex)^m dx \\ &= \frac{a^2 c(3Abc + aBc + 2aAd)x^{1+n} (ex)^m}{1+m+n} + \frac{a(aBc(3bc + 2ad) + b^3 Bd^2)x^{6n+1} (ex)^m}{1+m+6n} \end{aligned}$$

**Mathematica [A]**

time = 1.34, size = 273, normalized size = 0.86

$$x(ex)^m \left( \frac{a^3 Ac^2}{1+m} + \frac{a^2 c(3Abc + aBc + 2aAd)x^n}{1+m+n} + \frac{a(aBc(3bc + 2ad) + A(3b^2 c^2 + 6abcd + a^2 d^2))x^{2n}}{1+m+2n} + \frac{(aB(3b^2 c^2 + 6abcd + a^2 d^2) + Ab(b^2 c^2 + 6abcd + 3a^2 d^2))x^{3n}}{1+m+3n} + \frac{b(3a^2 B d^2 + 3abd(2Bc + Ad) + b^2 c(Bc + 2Ad))x^{4n}}{1+m+4n} + \frac{b^2 d(2bBc + Abd + 3aBd)x^{5n}}{1+m+5n} + \frac{b^3 B d^2 x^{6n}}{1+m+6n} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*(a + b*x^n)^3*(A + B*x^n)*(c + d*x^n)^2,x]
```

```
[Out] x*(e*x)^m*((a^3*A*c^2)/(1+m) + (a^2*c*(3*A*b*c + a*B*c + 2*a*A*d)*x^n)/(1+m+n) + (a*(a*B*c*(3*b*c + 2*a*d) + A*(3*b^2*c^2 + 6*a*b*c*d + a^2*d^2))*x^(2*n))/(1+m+2*n) + ((a*B*(3*b^2*c^2 + 6*a*b*c*d + a^2*d^2) + A*b*(b^2*c^2 + 6*a*b*c*d + 3*a^2*d^2))*x^(3*n))/(1+m+3*n) + (b*(3*a^2*B*d^2 + 3*a*b*d*(2*B*c + A*d) + b^2*c*(B*c + 2*A*d))*x^(4*n))/(1+m+4*n) + (b^2*d*(2*b*B*c + A*b*d + 3*a*B*d)*x^(5*n))/(1+m+5*n) + (b^3*B*d^2*x^(6*n))/(1+m+6*n))
```

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.50, size = 11389, normalized size = 35.81

method	result	size
risch	Expression too large to display	11389

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^2,x,method=_RETURNVERBOSE)
```

[Out] result too large to display

**Maxima** [B] Leaf count of result is larger than twice the leaf count of optimal. 702 vs.  $2(324) = 648$ .

time = 0.38, size = 702, normalized size = 2.21

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="maxima")`

[Out]  $(x*e)^{(m+1)}*A*a^3*c^2*e^{(-1)}/(m+1) + B*b^3*d^2*x*e^{(m*\log(x) + 6*n*\log(x) + m)}/(m + 6*n + 1) + 2*B*b^3*c*d*x*e^{(m*\log(x) + 5*n*\log(x) + m)}/(m + 5*n + 1) + 3*B*a*b^2*d^2*x*e^{(m*\log(x) + 5*n*\log(x) + m)}/(m + 5*n + 1) + A*b^3*d^2*x*e^{(m*\log(x) + 5*n*\log(x) + m)}/(m + 5*n + 1) + B*b^3*c^2*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m + 4*n + 1) + 6*B*a*b^2*c*d*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m + 4*n + 1) + 2*A*b^3*c*d*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m + 4*n + 1) + 3*B*a^2*b*d^2*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m + 4*n + 1) + 3*A*a*b^2*d^2*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m + 4*n + 1) + 3*B*a*b^2*c^2*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m + 3*n + 1) + A*b^3*c^2*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m + 3*n + 1) + 6*B*a^2*b*c*d*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m + 3*n + 1) + 6*A*a*b^2*c*d*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m + 3*n + 1) + B*a^3*d^2*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m + 3*n + 1) + 3*A*a^2*b*d^2*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m + 3*n + 1) + 3*B*a^2*b*c^2*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m + 2*n + 1) + 3*A*a*b^2*c^2*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m + 2*n + 1) + 2*B*a^3*c*d*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m + 2*n + 1) + 6*A*a^2*b*c*d*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m + 2*n + 1) + A*a^3*d^2*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m + 2*n + 1) + B*a^3*c^2*x*e^{(m*\log(x) + n*\log(x) + m)}/(m + n + 1) + 3*A*a^2*b*c^2*x*e^{(m*\log(x) + n*\log(x) + m)}/(m + n + 1) + 2*A*a^3*c*d*x*e^{(m*\log(x) + n*\log(x) + m)}/(m + n + 1)$

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 6617 vs.  $2(324) = 648$ .

time = 1.17, size = 6617, normalized size = 20.81

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="fricas")`

[Out]  $((B*b^3*d^2*m^6 + 6*B*b^3*d^2*m^5 + 15*B*b^3*d^2*m^4 + 20*B*b^3*d^2*m^3 + 15*B*b^3*d^2*m^2 + 6*B*b^3*d^2*m + B*b^3*d^2 + 120*(B*b^3*d^2*m + B*b^3*d^2)*n^5 + 274*(B*b^3*d^2*m^2 + 2*B*b^3*d^2*m + B*b^3*d^2)*n^4 + 225*(B*b^3*d^2*m^3 + 3*B*b^3*d^2*m^2 + 3*B*b^3*d^2*m + B*b^3*d^2)*n^3 + 85*(B*b^3*d^2*m^4 + 4*B*b^3*d^2*m^3 + 6*B*b^3*d^2*m^2 + 4*B*b^3*d^2*m + B*b^3*d^2)*n^2 + 15*(B*b^3*d^2*m^5 + 5*B*b^3*d^2*m^4 + 10*B*b^3*d^2*m^3 + 10*B*b^3*d^2*m^2 + 5*$

$$\begin{aligned}
& B*b^3*d^2*m + B*b^3*d^2)*n)*x*x^{(6*n)}*e^{(m*\log(x) + m) + ((2*B*b^3*c*d + (3 \\
& *B*a*b^2 + A*b^3)*d^2)*m^6 + 2*B*b^3*c*d + 6*(2*B*b^3*c*d + (3*B*a*b^2 + A* \\
& b^3)*d^2)*m^5 + 144*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2 + (2*B*b^3*c*d + \\
& (3*B*a*b^2 + A*b^3)*d^2)*m)*n^5 + 15*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^ \\
& 2)*m^4 + 324*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2 + (2*B*b^3*c*d + (3*B*a \\
& *b^2 + A*b^3)*d^2)*m^2 + 2*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m)*n^4 + \\
& 20*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m^3 + 260*(2*B*b^3*c*d + (2*B*b \\
& ^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m^3 + (3*B*a*b^2 + A*b^3)*d^2 + 3*(2*B*b^ \\
& 3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m^2 + 3*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3) \\
& *d^2)*m)*n^3 + (3*B*a*b^2 + A*b^3)*d^2 + 15*(2*B*b^3*c*d + (3*B*a*b^2 + A*b \\
& ^3)*d^2)*m^2 + 95*(2*B*b^3*c*d + (2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m^ \\
& 4 + 4*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m^3 + (3*B*a*b^2 + A*b^3)*d^2 \\
& + 6*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m^2 + 4*(2*B*b^3*c*d + (3*B*a* \\
& b^2 + A*b^3)*d^2)*m)*n^2 + 6*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m + 16 \\
& *(2*B*b^3*c*d + (2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m^5 + 5*(2*B*b^3*c* \\
& d + (3*B*a*b^2 + A*b^3)*d^2)*m^4 + 10*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^ \\
& 2)*m^3 + (3*B*a*b^2 + A*b^3)*d^2 + 10*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^ \\
& 2)*m^2 + 5*(2*B*b^3*c*d + (3*B*a*b^2 + A*b^3)*d^2)*m)*n)*x*x^{(5*n)}*e^{(m*\log \\
& (x) + m) + ((B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*a*b^2)* \\
& d^2)*m^6 + B*b^3*c^2 + 6*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2* \\
& b + A*a*b^2)*d^2)*m^5 + 180*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a \\
& ^2*b + A*a*b^2)*d^2 + (B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + \\
& A*a*b^2)*d^2)*m)*n^5 + 15*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^ \\
& 2*b + A*a*b^2)*d^2)*m^4 + 396*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B \\
& *a^2*b + A*a*b^2)*d^2 + (B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b \\
& + A*a*b^2)*d^2)*m^2 + 2*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2* \\
& b + A*a*b^2)*d^2)*m)*n^4 + 20*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B \\
& *a^2*b + A*a*b^2)*d^2)*m^3 + 307*(B*b^3*c^2 + (B*b^3*c^2 + 2*(3*B*a*b^2 + A \\
& *b^3)*c*d + 3*(B*a^2*b + A*a*b^2)*d^2)*m^3 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3* \\
& (B*a^2*b + A*a*b^2)*d^2 + 3*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a \\
& ^2*b + A*a*b^2)*d^2)*m^2 + 3*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B* \\
& a^2*b + A*a*b^2)*d^2)*m)*n^3 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*a \\
& *b^2)*d^2 + 15*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*a*b^ \\
& 2)*d^2)*m^2 + 107*(B*b^3*c^2 + (B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*( \\
& B*a^2*b + A*a*b^2)*d^2)*m^4 + 4*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3* \\
& (B*a^2*b + A*a*b^2)*d^2)*m^3 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*a \\
& *b^2)*d^2 + 6*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*a*b^2 \\
& )*d^2)*m^2 + 4*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*a*b^ \\
& 2)*d^2)*m)*n^2 + 6*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A* \\
& a*b^2)*d^2)*m + 17*(B*b^3*c^2 + (B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3* \\
& (B*a^2*b + A*a*b^2)*d^2)*m^5 + 5*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3 \\
& *(B*a^2*b + A*a*b^2)*d^2)*m^4 + 10*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + \\
& 3*(B*a^2*b + A*a*b^2)*d^2)*m^3 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + \\
& A*a*b^2)*d^2 + 10*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*a \\
& *b^2)*d^2)*m^2 + 5*(B*b^3*c^2 + 2*(3*B*a*b^2 + A*b^3)*c*d + 3*(B*a^2*b + A*
\end{aligned}$$

```

a*b^2)*d^2)*m)*n)*x*x^(4*n)*e^(m*log(x) + m) + (((3*B*a*b^2 + A*b^3)*c^2 +
6*(B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*d^2)*m^6 + 6*((3*B*a*b^2 +
A*b^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*d^2)*m^5 + 240
*((3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*
d^2 + ((3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*
a^2*b)*d^2)*m)*n^5 + 15*((3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*c*
d + (B*a^3 + 3*A*a^2*b)*d^2)*m^4 + 508*((3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*
b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*d^2 + ((3*B*a*b^2 + A*b^3)*c^2 + 6*(
B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*d^2)*m^2 + 2*((3*B*a*b^2 + A*b
^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*d^2)*m)*n^4 + 20*
((3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*
d^2)*m^3 + 372*((3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*c*d + (B*a
^3 + 3*A*a^2*b)*d^2)*m^3 + (3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*b + A*a*b^2)*
c*d + (B*a^3 + 3*A*a^2*b)*d^2 + 3*((3*B*a*b^2 + A*b^3)*c^2 + 6*(B*a^2*b + A
*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*d^2)*m^2 + 3*((3*B*a*b^2 + A*b^3)*c^2 + 6
*(B*a^2*b + A*a*b^2)*c*d + (B*a^3 + 3*A*a^2*b)*...

```

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)**3*(A+B*x**n)*(c+d*x**n)**2,x)
```

[Out] Timed out

**Giac** [B] Leaf count of result is larger than twice the leaf count of optimal. 15358 vs.  $2(324) = 648$ .

time = 1.72, size = 15358, normalized size = 48.30

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="giac")
```

```
[Out] (B*b^3*d^2*m^6*x*x^m*x^(6*n)*e^m + 15*B*b^3*d^2*m^5*n*x*x^m*x^(6*n)*e^m + 8
5*B*b^3*d^2*m^4*n^2*x*x^m*x^(6*n)*e^m + 225*B*b^3*d^2*m^3*n^3*x*x^m*x^(6*n)
*e^m + 274*B*b^3*d^2*m^2*n^4*x*x^m*x^(6*n)*e^m + 120*B*b^3*d^2*m*n^5*x*x^m*
x^(6*n)*e^m + 2*B*b^3*c*d*m^6*x*x^m*x^(5*n)*e^m + 3*B*a*b^2*d^2*m^6*x*x^m*x
^(5*n)*e^m + A*b^3*d^2*m^6*x*x^m*x^(5*n)*e^m + 32*B*b^3*c*d*m^5*n*x*x^m*x^(
5*n)*e^m + 48*B*a*b^2*d^2*m^5*n*x*x^m*x^(5*n)*e^m + 16*A*b^3*d^2*m^5*n*x*x^
m*x^(5*n)*e^m + 190*B*b^3*c*d*m^4*n^2*x*x^m*x^(5*n)*e^m + 285*B*a*b^2*d^2*m
^4*n^2*x*x^m*x^(5*n)*e^m + 95*A*b^3*d^2*m^4*n^2*x*x^m*x^(5*n)*e^m + 520*B*b
^3*c*d*m^3*n^3*x*x^m*x^(5*n)*e^m + 780*B*a*b^2*d^2*m^3*n^3*x*x^m*x^(5*n)*e^
m + 260*A*b^3*d^2*m^3*n^3*x*x^m*x^(5*n)*e^m + 648*B*b^3*c*d*m^2*n^4*x*x^m*x

```

$$\begin{aligned}
& \cdot (5n) e^m + 972 B^2 a^2 b^2 d^2 m^2 n^4 x^m x^m x^m (5n) e^m + 324 A^2 b^3 d^2 m^2 n^4 x^m x^m x^m (5n) e^m + 288 B^2 b^3 c^2 d^2 m^2 n^5 x^m x^m x^m (5n) e^m + 432 B^2 a^2 b^2 d^2 m^2 n^5 x^m x^m x^m (5n) e^m + 144 A^2 b^3 d^2 m^2 n^5 x^m x^m x^m (5n) e^m + B^2 b^3 c^2 m^6 x^m x^m x^m (4n) e^m + 6 B^2 a^2 b^2 c^2 d^2 m^6 x^m x^m x^m (4n) e^m + 2 A^2 b^3 c^2 d^2 m^6 x^m x^m x^m (4n) e^m + 3 B^2 a^2 b^2 d^2 m^6 x^m x^m x^m (4n) e^m + 3 A^2 a^2 b^2 d^2 m^6 x^m x^m x^m (4n) e^m + 17 B^2 b^3 c^2 m^5 n x^m x^m x^m (4n) e^m + 102 B^2 a^2 b^2 c^2 d^2 m^5 n x^m x^m x^m (4n) e^m + 34 A^2 b^3 c^2 d^2 m^5 n x^m x^m x^m (4n) e^m + 51 B^2 a^2 b^2 d^2 m^5 n x^m x^m x^m (4n) e^m + 51 A^2 a^2 b^2 d^2 m^5 n x^m x^m x^m (4n) e^m + 107 B^2 b^3 c^2 m^4 n^2 x^m x^m x^m (4n) e^m + 642 B^2 a^2 b^2 c^2 d^2 m^4 n^2 x^m x^m x^m (4n) e^m + 214 A^2 b^3 c^2 d^2 m^4 n^2 x^m x^m x^m (4n) e^m + 321 B^2 a^2 b^2 d^2 m^4 n^2 x^m x^m x^m (4n) e^m + 321 A^2 a^2 b^2 d^2 m^4 n^2 x^m x^m x^m (4n) e^m + 307 B^2 b^3 c^2 m^3 n^3 x^m x^m x^m (4n) e^m + 1842 B^2 a^2 b^2 c^2 d^2 m^3 n^3 x^m x^m x^m (4n) e^m + 614 A^2 b^3 c^2 d^2 m^3 n^3 x^m x^m x^m (4n) e^m + 921 B^2 a^2 b^2 d^2 m^3 n^3 x^m x^m x^m (4n) e^m + 921 A^2 a^2 b^2 d^2 m^3 n^3 x^m x^m x^m (4n) e^m + 396 B^2 b^3 c^2 m^2 n^4 x^m x^m x^m (4n) e^m + 2376 B^2 a^2 b^2 c^2 d^2 m^2 n^4 x^m x^m x^m (4n) e^m + 792 A^2 b^3 c^2 d^2 m^2 n^4 x^m x^m x^m (4n) e^m + 1188 B^2 a^2 b^2 d^2 m^2 n^4 x^m x^m x^m (4n) e^m + 1188 A^2 a^2 b^2 d^2 m^2 n^4 x^m x^m x^m (4n) e^m + 180 B^2 b^3 c^2 m^2 n^5 x^m x^m x^m (4n) e^m + 1080 B^2 a^2 b^2 c^2 d^2 m^2 n^5 x^m x^m x^m (4n) e^m + 360 A^2 b^3 c^2 d^2 m^2 n^5 x^m x^m x^m (4n) e^m + 540 B^2 a^2 b^2 d^2 m^2 n^5 x^m x^m x^m (4n) e^m + 540 A^2 a^2 b^2 d^2 m^2 n^5 x^m x^m x^m (4n) e^m + 3 B^2 a^2 b^2 c^2 m^6 x^m x^m x^m (3n) e^m + A^2 b^3 c^2 m^6 x^m x^m x^m (3n) e^m + 6 B^2 a^2 b^2 c^2 d^2 m^6 x^m x^m x^m (3n) e^m + 6 A^2 a^2 b^2 c^2 d^2 m^6 x^m x^m x^m (3n) e^m + B^2 a^3 d^2 m^6 x^m x^m x^m (3n) e^m + 3 A^2 a^2 b^2 d^2 m^6 x^m x^m x^m (3n) e^m + 54 B^2 a^2 b^2 c^2 m^5 n x^m x^m x^m (3n) e^m + 18 A^2 b^3 c^2 m^5 n x^m x^m x^m (3n) e^m + 108 B^2 a^2 b^2 c^2 d^2 m^5 n x^m x^m x^m (3n) e^m + 108 A^2 a^2 b^2 c^2 d^2 m^5 n x^m x^m x^m (3n) e^m + 18 B^2 a^3 d^2 m^5 n x^m x^m x^m (3n) e^m + 54 A^2 a^2 b^2 d^2 m^5 n x^m x^m x^m (3n) e^m + 363 B^2 a^2 b^2 c^2 m^4 n^2 x^m x^m x^m (3n) e^m + 121 A^2 b^3 c^2 m^4 n^2 x^m x^m x^m (3n) e^m + 726 B^2 a^2 b^2 c^2 d^2 m^4 n^2 x^m x^m x^m (3n) e^m + 726 A^2 a^2 b^2 c^2 d^2 m^4 n^2 x^m x^m x^m (3n) e^m + 121 B^2 a^3 d^2 m^4 n^2 x^m x^m x^m (3n) e^m + 363 A^2 a^2 b^2 d^2 m^4 n^2 x^m x^m x^m (3n) e^m + 1116 B^2 a^2 b^2 c^2 m^3 n^3 x^m x^m x^m (3n) e^m + 372 A^2 b^3 c^2 m^3 n^3 x^m x^m x^m (3n) e^m + 2232 B^2 a^2 b^2 c^2 d^2 m^3 n^3 x^m x^m x^m (3n) e^m + 2232 A^2 a^2 b^2 c^2 d^2 m^3 n^3 x^m x^m x^m (3n) e^m + 372 B^2 a^3 d^2 m^3 n^3 x^m x^m x^m (3n) e^m + 1116 A^2 a^2 b^2 d^2 m^3 n^3 x^m x^m x^m (3n) e^m + 1524 B^2 a^2 b^2 c^2 m^2 n^4 x^m x^m x^m (3n) e^m + 508 A^2 b^3 c^2 m^2 n^4 x^m x^m x^m (3n) e^m + 3048 B^2 a^2 b^2 c^2 d^2 m^2 n^4 x^m x^m x^m (3n) e^m + 3048 A^2 a^2 b^2 c^2 d^2 m^2 n^4 x^m x^m x^m (3n) e^m + 508 B^2 a^3 d^2 m^2 n^4 x^m x^m x^m (3n) e^m + 1524 A^2 a^2 b^2 d^2 m^2 n^4 x^m x^m x^m (3n) e^m + 720 B^2 a^2 b^2 c^2 m^2 n^5 x^m x^m x^m (3n) e^m + 240 A^2 b^3 c^2 m^2 n^5 x^m x^m x^m (3n) e^m + 1440 B^2 a^2 b^2 c^2 d^2 m^2 n^5 x^m x^m x^m (3n) e^m + 1440 A^2 a^2 b^2 c^2 d^2 m^2 n^5 x^m x^m x^m (3n) e^m + 240 B^2 a^3 d^2 m^2 n^5 x^m x^m x^m (3n) e^m + 720 A^2 a^2 b^2 d^2 m^2 n^5 x^m x^m x^m (3n) e^m + 3 B^2 a^2 b^2 c^2 m^6 x^m x^m x^m (2n) e^m + 3 A^2 a^2 b^2 c^2 m^6 x^m x^m x^m (2n) e^m + 2 B^2 a^3 c^2 d^2 m^6 x^m x^m x^m (2n) e^m + 6 A^2 a^2 b^2 c^2 d^2 m^6 x^m x^m x^m (2n) e^m + A^2 a^3 d^2 m^6 x^m x^m x^m (2n) e^m + 57 B^2 a^2 b^2 c^2 m^5 n x^m x^m x^m (2n) e^m + 57 A^2 a^2 b^2 c^2 m^5 n x^m x^m x^m (2n) e^m + 38 B^2 a^3 c^2 d^2 m^5 n x^m x^m x^m (2n) e^m + 114 A^2 a^2 b^2 c^2 d^2 m^5 n x^m x^m x^m (2n) e^m + 19 A^2 a^3 d^2 m^5 n x^m x^m x^m (2n) e^m + 411 B^2 a^2 b^2 c^2 m^4 n
\end{aligned}$$

$$\begin{aligned} & \cdot 2*x*x^m*x^{(2*n)}*e^m + 411*A*a*b^2*c^2*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 274*B*a^3*c*d*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 822*A*a^2*b*c*d*m^4*n^2*x*x^m*x^{(2*n)}*e^m \\ & + 137*A*a^3*d^2*m^4*n^2*x*x^m*x^{(2*n)}*e^m + 1383*B*a^2*b*c^2*m^3*n^3*x*x^m*x^{(2*n)}*e^m + 1383*A*a*b^2*c^2*m^3*n^3*x*x^m*x^{(2*n)}*e^m + 922*B*a^3*c*d*m^3*n^3*x*x^m*x^{(2*n)}*e^m + 2766*A*a^2*b*c*d*m^3*n^3*x*x^m*x^{(2*n)}*e^m + 461 \\ & *A*a^3*d^2*m^3*n^3*x*x^m*x^{(2*n)}*e^m + 2106*B*a^2*b*c^2*m^2*n^4*x*x^m*x^{(2*n)}*e^m + 2106*A*a*b^2*c^2*m^2*n^4*x*x^m*x^{(2*n)}*e^m + 1404*B*a^3*c*d*m^2*n^4*x*x^m*x^{(2*n)}*e^m + 4212*A*a^2*b*c*d*m^2*n^4*x*x^m*x^{(2*n)}*e^m + 702*A*a^3*d^2*m^2*n^4*x*x^m*x^{(2*n)}*e^m + 1080*B*a^2*b*c^2*m*n^5*x*x^m*x^{(2*n)}*e^m \\ & + 1080*A*a*b^2*c^2*m*n^5*x*x^m*x^{(2*n)}*e^m + 720*B*a^3*c*d*m*n^5*x*x^m*x^{(2*n)}*e^m + 2160*A*a^2*b*c*d*m*n^5*x*x^m*x^{(2*n)}*e^m + 360*A*a^3*d^2*m*n^5*x*x^m*x^{(2*n)}*e^m + B*a^3*c^2*m^6*x*x^m*x^n*e^m + \dots \end{aligned}$$

Mupad [B]

time = 6.35, size = 1882, normalized size = 5.92

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)^3*(c + d*x^n)^2,x)$

[Out]  $(x*x^{(3*n)}*(e*x)^m*(A*b^3*c^2 + B*a^3*d^2 + 3*A*a^2*b*d^2 + 3*B*a*b^2*c^2 + 6*A*a*b^2*c*d + 6*B*a^2*b*c*d)*(5*m + 18*n + 72*m*n + 363*m*n^2 + 108*m^2*n + 744*m*n^3 + 72*m^3*n + 508*m*n^4 + 18*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 121*n^2 + 372*n^3 + 508*n^4 + 240*n^5 + 363*m^2*n^2 + 372*m^2*n^3 + 121*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (A*a^3*c^2*x*(e*x)^m)/(m + 1) + (a*x*x^{(2*n)}*(e*x)^m*(A*a^2*d^2 + 3*A*b^2*c^2 + 3*B*a*b*c^2 + 2*B*a^2*c*d + 6*A*a*b*c*d)*(5*m + 19*n + 76*m*n + 411*m*n^2 + 114*m^2*n + 922*m*n^3 + 76*m^3*n + 702*m*n^4 + 19*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 137*n^2 + 461*n^3 + 702*n^4 + 360*n^5 + 411*m^2*n^2 + 461*m^2*n^3 + 137*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (b*x*x^{(4*n)}*(e*x)^m*(3*B*a^2*d^2 + B*b^2*c^2 + 3*A*a*b*d^2 + 2*A*b^2*c*d + 6*B*a*b*c*d)*(5*m + 17*n + 68*m*n + 321*m*n^2 + 102*m^2*n + 614*m*n^3 + 68*m^3*n + 396*m*n^4 + 17*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 107*n^2 + 307*n^3 + 396*n^4 + 180*n^5 + 321*m^2*n^2 + 307*m^2*n^3 + 107*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m$

$$\begin{aligned}
&^2n^3 + 700m^3n^2 + 1624m^2n^4 + 735m^3n^3 + 175m^4n^2 + 1) + (a^2 \\
&*c*x*x^n*(e*x)^m*(2A*a*d + 3A*b*c + B*a*c)*(5*m + 20*n + 80*m*n + 465*m*n \\
&^2 + 120*m^2*n + 1160*m*n^3 + 80*m^3*n + 1044*m*n^4 + 20*m^4*n + 10*m^2 + 1 \\
&0*m^3 + 5*m^4 + m^5 + 155*n^2 + 580*n^3 + 1044*n^4 + 720*n^5 + 465*m^2*n^2 \\
&+ 580*m^2*n^3 + 155*m^3*n^2 + 1))/ (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m \\
&^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^ \\
&5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 \\
&+ 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^ \\
&2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (b^2*d*x*x^(5*n)*(e*x)^m*(A*b*d + \\
&3*B*a*d + 2*B*b*c)*(5*m + 16*n + 64*m*n + 285*m*n^2 + 96*m^2*n + 520*m*n^3 \\
&+ 64*m^3*n + 324*m*n^4 + 16*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 95*n^2 \\
&+ 260*n^3 + 324*n^4 + 144*n^5 + 285*m^2*n^2 + 260*m^2*n^3 + 95*m^3*n^2 + 1) \\
&))/ (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + \\
&3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + \\
&6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2 \\
&*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^ \\
&2 + 1) + (B*b^3*d^2*x*x^(6*n)*(e*x)^m*(5*m + 15*n + 60*m*n + 255*m*n^2 + 90 \\
&*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5* \\
&m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^ \\
&3 + 85*m^3*n^2 + 1))/ (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m \\
&*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 \\
&+ 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + \\
&720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m \\
&^3*n^3 + 175*m^4*n^2 + 1)
\end{aligned}$$

### 3.9 $\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=237

$$\frac{ac(aBc + 2A(bc + ad))x^{1+n}(ex)^m}{1 + m + n} + \frac{(2aBc(bc + ad) + A(b^2c^2 + 4abcd + a^2d^2))x^{1+2n}(ex)^m}{1 + m + 2n} + \frac{(a^2Bd^2 + 2abd)}{1 + m + 3n}$$

[Out]  $a*c*(a*B*c+2*A*(a*d+b*c))*x^{(1+n)}*(e*x)^m/(1+m+n)+(2*a*B*c*(a*d+b*c)+A*(a^2*d^2+4*a*b*c*d+b^2*c^2))*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+(a^2*B*d^2+2*a*b*d*(A*d+2*B*c)+b^2*c*(2*A*d+B*c))*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+b*d*(A*b*d+2*B*a*d+2*B*b*c)*x^{(1+4*n)}*(e*x)^m/(1+m+4*n)+b^2*B*d^2*x^{(1+5*n)}*(e*x)^m/(1+m+5*n)+a^2*A*c^2*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.20, antiderivative size = 237, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {584, 20, 30}

$$\frac{x^{2n+1}(ex)^m(A(a^2d^2+4abcd+b^2c^2)+2aBc(ad+bc))}{m+2n+1} + \frac{x^{3n+1}(ex)^m(a^2Bd^2+2abd(Ad+2Bc)+b^2c(2Ad+Bc))}{m+3n+1} + \frac{a^2Ac^2(ex)^{m+1}}{e(m+1)} + \frac{acx^{n+1}(ex)^m(2A(ad+bc)+aBc)}{m+n+1} + \frac{bdx^{4n+1}(ex)^m(2aBd+Abd+2bBc)}{m+4n+1} + \frac{b^2Bd^2x^{5n+1}(ex)^m}{m+5n+1}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(a + b*x^n)^2*(A + B*x^n)*(c + d*x^n)^2, x]$

[Out]  $(a*c*(a*B*c + 2*A*(b*c + a*d))*x^{(1 + n)}*(e*x)^m/(1 + m + n) + ((2*a*B*c*(b*c + a*d) + A*(b^2*c^2 + 4*a*b*c*d + a^2*d^2))*x^{(1 + 2*n)}*(e*x)^m/(1 + m + 2*n) + ((a^2*B*d^2 + 2*a*b*d*(2*B*c + A*d) + b^2*c*(B*c + 2*A*d))*x^{(1 + 3*n)}*(e*x)^m/(1 + m + 3*n) + (b*d*(2*b*B*c + A*b*d + 2*a*B*d))*x^{(1 + 4*n)}*(e*x)^m/(1 + m + 4*n) + (b^2*B*d^2*x^{(1 + 5*n)}*(e*x)^m/(1 + m + 5*n) + (a^2*A*c^2*(e*x)^{(1 + m)})/(e*(1 + m)))$

**Rule 20**

$\text{Int}[(u_.)*((a_.)*(v_.))^{(m_.)}*((b_.)*(v_.))^{(n_.)}, x\_Symbol] := \text{Dist}[b^{\text{IntPart}[n]}*((b*v)^{\text{FracPart}[n]}/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]})), \text{Int}[u*(a*v)^{(m+n)}, x], x] /;$   $\text{FreeQ}\{a, b, m, n\}, x\} \&\& \text{IntegerQ}[m] \&\& \text{IntegerQ}[n] \&\& \text{IntegerQ}[m+n]$

**Rule 30**

$\text{Int}[(x_)^{(m_.)}, x\_Symbol] := \text{Simp}[x^{(m+1)}/(m+1), x] /;$   $\text{FreeQ}[m, x] \&\& \text{NeQ}[m, -1]$

**Rule 584**

$\text{Int}[(g_.)*(x_)^{(m_.)}*((a_.) + (b_.)*(x_)^{(n_.)})^{(p_.)}*((c_.) + (d_.)*(x_)^{(n_.)})^{(q_.)}*((e_.) + (f_.)*(x_)^{(n_.)})^{(r_.)}, x\_Symbol] := \text{Int}[\text{ExpandIntegrand}[$



$(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; \text{FreeQ}[\{a, b, c, d, e, f, g, m, n\}, x] \ \&\& \ \text{IGtQ}[p, -2] \ \&\& \ \text{IGtQ}[q, 0] \ \&\& \ \text{IGtQ}[r, 0]$

Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^2 dx &= \int (a^2 Ac^2 (ex)^m + ac(aBc + 2A(bc + ad))x^n (ex)^m + (2aBc + Abc^2) x^{2n} (ex)^m) dx \\ &= \frac{a^2 Ac^2 (ex)^{1+m}}{e(1+m)} + (b^2 Bd^2) \int x^{5n} (ex)^m dx + (bd(2bBc + Abc^2) x^{2n} (ex)^m) \\ &= \frac{a^2 Ac^2 (ex)^{1+m}}{e(1+m)} + (b^2 Bd^2 x^{-m} (ex)^m) \int x^{m+5n} dx + (bd(2bBc + Abc^2) x^{2n} (ex)^m) \\ &= \frac{ac(aBc + 2A(bc + ad))x^{1+n} (ex)^m}{1+m+n} + \frac{(2aBc(bc + ad) + A(b^2 c^2 + 4abcd + a^2 d^2))x^{2n}}{1+m+2n} \end{aligned}$$

**Mathematica [A]**

time = 0.60, size = 199, normalized size = 0.84

$$x(ex)^m \left( \frac{a^2 Ac^2}{1+m} + \frac{ac(aBc + 2A(bc + ad))x^n}{1+m+n} + \frac{(2aBc(bc + ad) + A(b^2 c^2 + 4abcd + a^2 d^2))x^{2n}}{1+m+2n} + \frac{(a^2 Bd^2 + 2abd(2Bc + Ad) + b^2 c(Bc + 2Ad))x^{3n}}{1+m+3n} + \frac{bd(2bBc + Abc^2 + 2aBd)x^{4n}}{1+m+4n} + \frac{b^2 Bd^2 x^{5n}}{1+m+5n} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

[Out] x\*(e\*x)^m\*((a^2\*A\*c^2)/(1+m) + (a\*c\*(a\*B\*c + 2\*A\*(b\*c + a\*d))\*x^n)/(1+m+n) + ((2\*a\*B\*c\*(b\*c + a\*d) + A\*(b^2\*c^2 + 4\*a\*b\*c\*d + a^2\*d^2))\*x^(2\*n))/(1+m+2\*n) + ((a^2\*B\*d^2 + 2\*a\*b\*d\*(2\*B\*c + A\*d) + b^2\*c\*(B\*c + 2\*A\*d))\*x^(3\*n))/(1+m+3\*n) + (b\*d\*(2\*b\*B\*c + A\*b\*d + 2\*a\*B\*d)\*x^(4\*n))/(1+m+4\*n) + (b^2\*B\*d^2\*x^(5\*n))/(1+m+5\*n))

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.43, size = 5908, normalized size = 24.93

method	result	size
risch	Expression too large to display	5908

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n)^2,x,method=\_RETURNVERBOSE)

[Out] result too large to display

**Maxima [B]** Leaf count of result is larger than twice the leaf count of optimal. 506 vs. 2(242) = 484.

time = 0.35, size = 506, normalized size = 2.14

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="maxima")
[Out] (x*e)^(m + 1)*A*a^2*c^2*e^(-1)/(m + 1) + B*b^2*d^2*x*e^(m*log(x) + 5*n*log(x) + m)/(m + 5*n + 1) + 2*B*b^2*c*d*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + 2*B*a*b*d^2*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + A*b^2*d^2*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + B*b^2*c^2*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 4*B*a*b*c*d*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 2*A*b^2*c*d*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + B*a^2*d^2*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 2*A*a*b*d^2*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 2*B*a*b*c^2*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + A*b^2*c^2*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + 2*B*a^2*c*d*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + 4*A*a*b*c*d*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + A*a^2*d^2*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + B*a^2*c^2*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1) + 2*A*a*b*c^2*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1) + 2*A*a^2*c*d*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1)
```

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 3497 vs. 2(242) = 484.

time = 2.39, size = 3497, normalized size = 14.76

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="fricas")
[Out] ((B*b^2*d^2*m^5 + 5*B*b^2*d^2*m^4 + 10*B*b^2*d^2*m^3 + 10*B*b^2*d^2*m^2 + 5*B*b^2*d^2*m + B*b^2*d^2 + 24*(B*b^2*d^2*m + B*b^2*d^2)*n^4 + 50*(B*b^2*d^2*m^2 + 2*B*b^2*d^2*m + B*b^2*d^2)*n^3 + 35*(B*b^2*d^2*m^3 + 3*B*b^2*d^2*m^2 + 3*B*b^2*d^2*m + B*b^2*d^2)*n^2 + 10*(B*b^2*d^2*m^4 + 4*B*b^2*d^2*m^3 + 6*B*b^2*d^2*m^2 + 4*B*b^2*d^2*m + B*b^2*d^2)*n)*x^n*(5*n)*e^(m*log(x) + m) + ((2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^5 + 2*B*b^2*c*d + 5*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^4 + 30*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2) + (2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m)*n^4 + 10*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^3 + 61*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2) + (2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^2 + 2*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m)*n^3 + (2*B*a*b + A*b^2)*d^2 + 10*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^2 + 41*(2*B*b^2*c*d + (2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^3 + (2*B*a*b + A*b^2)*d^2 + 3*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^2 + 3*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m)*n^2 + 5*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m + 11*(2*B*b^2*c*d + (2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^4 + 4*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^3 + (2*B*a*b + A*b^2)*d^2 + 6*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m^2 + 4*(2*B*b^2*c*d + (2*B*a*b + A*b^2)*d^2)*m)*n)*x^n*(4*n)*e^(m*log(x) + m) + ((B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 +
```

$$\begin{aligned}
& 2*A*a*b)*d^2)*m^5 + B*b^2*c^2 + 5*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B \\
& *a^2 + 2*A*a*b)*d^2)*m^4 + 40*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 \\
& + 2*A*a*b)*d^2 + (B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)* \\
& d^2)*m)*n^4 + 10*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d \\
& ^2)*m^3 + 78*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2 + \\
& (B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2)*m^2 + 2*(B*b \\
& ^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2)*m)*n^3 + 2*(2*B*a \\
& *b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2 + 10*(B*b^2*c^2 + 2*(2*B*a*b + A*b^ \\
& 2)*c*d + (B*a^2 + 2*A*a*b)*d^2)*m^2 + 49*(B*b^2*c^2 + (B*b^2*c^2 + 2*(2*B*a \\
& *b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2)*m^3 + 2*(2*B*a*b + A*b^2)*c*d + (B \\
& *a^2 + 2*A*a*b)*d^2 + 3*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A \\
& *a*b)*d^2)*m^2 + 3*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b) \\
& *d^2)*m)*n^2 + 5*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d \\
& ^2)*m + 12*(B*b^2*c^2 + (B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A \\
& *a*b)*d^2)*m^4 + 4*(B*b^2*c^2 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b) \\
& *d^2)*m^3 + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2 + 6*(B*b^2*c^2 \\
& + 2*(2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2)*m^2 + 4*(B*b^2*c^2 + 2*( \\
& 2*B*a*b + A*b^2)*c*d + (B*a^2 + 2*A*a*b)*d^2)*m)*n)*x*x^(3*n)*e^(m*log(x) + \\
& m) + ((A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m^5 + \\
& A*a^2*d^2 + 5*(A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d) \\
& *m^4 + 60*(A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d + (A \\
& *a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m)*n^4 + 10*(A* \\
& a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m^3 + 107*(A*a^2 \\
& *d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d + (A*a^2*d^2 + (2*B* \\
& a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m^2 + 2*(A*a^2*d^2 + (2*B*a*b + \\
& A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m)*n^3 + (2*B*a*b + A*b^2)*c^2 + 2*( \\
& B*a^2 + 2*A*a*b)*c*d + 10*(A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2 \\
& *A*a*b)*c*d)*m^2 + 59*(A*a^2*d^2 + (A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*( \\
& B*a^2 + 2*A*a*b)*c*d)*m^3 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d \\
& + 3*(A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m^2 + 3* \\
& (A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m)*n^2 + 5*(A \\
& *a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m + 13*(A*a^2*d \\
& ^2 + (A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m^4 + 4* \\
& (A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m^3 + (2*B*a* \\
& b + A*b^2)*c^2 + 2*(B*a^2 + 2*A*a*b)*c*d + 6*(A*a^2*d^2 + (2*B*a*b + A*b^2) \\
& *c^2 + 2*(B*a^2 + 2*A*a*b)*c*d)*m^2 + 4*(A*a^2*d^2 + (2*B*a*b + A*b^2)*c^2 \\
& + 2*(B*a^2 + 2*A*a*b)*c*d)*m)*n)*x*x^(2*n)*e^(m*log(x) + m) + ((2*A*a^2*c*d \\
& + (B*a^2 + 2*A*a*b)*c^2)*m^5 + 2*A*a^2*c*d + 5*(2*A*a^2*c*d + (B*a^2 + 2*A \\
& *a*b)*c^2)*m^4 + 120*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2 + (2*A*a^2*c*d + \\
& (B*a^2 + 2*A*a*b)*c^2)*m)*n^4 + 10*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m^ \\
& 3 + 154*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2 + (2*A*a^2*c*d + (B*a^2 + 2*A* \\
& a*b)*c^2)*m^2 + 2*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m)*n^3 + (B*a^2 + 2 \\
& *A*a*b)*c^2 + 10*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m^2 + 71*(2*A*a^2*c* \\
& d + (2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m^3 + (B*a^2 + 2*A*a*b)*c^2 + 3*( \\
& 2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m^2 + 3*(2*A*a^2*c*d + (B*a^2 + 2*A*a*
\end{aligned}$$

$b)*c^2)*m)*n^2 + 5*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m + 14*(2*A*a^2*c*d + (2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m^4 + 4*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m^3 + (B*a^2 + 2*A*a*b)*c^2 + 6*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b)*c^2)*m^2 + 4*(2*A*a^2*c*d + (B*a^2 + 2*A*a*b...$

**Sympy [B]** Leaf count of result is larger than twice the leaf count of optimal. 71580 vs.  $2(233) = 466$ .

time = 189.29, size = 71580, normalized size = 302.03

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*2\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*2,x)

[Out] Piecewise(((A + B)\*(a + b)\*\*2\*(c + d)\*\*2\*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A\*a\*\*2\*c\*\*2\*log(x) + 2\*A\*a\*\*2\*c\*d\*x\*\*n/n + A\*a\*\*2\*d\*\*2\*x\*\*(2\*n)/(2\*n) + 2\*A\*a\*b\*c\*\*2\*x\*\*n/n + 2\*A\*a\*b\*c\*d\*x\*\*(2\*n)/n + 2\*A\*a\*b\*d\*\*2\*x\*\*(3\*n)/(3\*n) + A\*b\*\*2\*c\*\*2\*x\*\*(2\*n)/(2\*n) + 2\*A\*b\*\*2\*c\*d\*x\*\*(3\*n)/(3\*n) + A\*b\*\*2\*d\*\*2\*x\*\*(4\*n)/(4\*n) + B\*a\*\*2\*c\*\*2\*x\*\*n/n + B\*a\*\*2\*c\*d\*x\*\*(2\*n)/n + B\*a\*\*2\*d\*\*2\*x\*\*(3\*n)/(3\*n) + B\*a\*b\*c\*\*2\*x\*\*(2\*n)/n + 4\*B\*a\*b\*c\*d\*x\*\*(3\*n)/(3\*n) + B\*a\*b\*d\*\*2\*x\*\*(4\*n)/(2\*n) + B\*b\*\*2\*c\*\*2\*x\*\*(3\*n)/(3\*n) + B\*b\*\*2\*c\*d\*x\*\*(4\*n)/(2\*n) + B\*b\*\*2\*d\*\*2\*x\*\*(5\*n)/(5\*n))/e, Eq(m, -1)), (A\*a\*\*2\*c\*\*2\*Piecewise((-1/(5\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*a\*\*2\*c\*d\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + A\*a\*\*2\*d\*\*2\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*a\*b\*c\*\*2\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 4\*A\*a\*b\*c\*d\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*a\*b\*d\*\*2\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + A\*b\*\*2\*c\*\*2\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*b\*\*2\*c\*d\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + A\*b\*\*2\*d\*\*2\*Piecewise((-x\*\*(4\*n)/(n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + B\*a\*\*2\*c\*\*2\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*B\*a\*\*2\*c\*d\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + B\*a\*\*2\*d\*\*2\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*B\*a\*b\*c\*\*2\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 4\*B\*a\*b\*c\*d\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*B\*a\*b\*d\*\*2\*Piecewise((-x\*\*(4\*n)/(n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + B\*b\*\*2\*c\*\*2\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + 2\*B\*b\*\*2\*c\*d\*Piecewise((-x\*\*(4\*n)/(n\*(e\*x)\*\*(5\*n)), Ne(n, 0)), (log(x), True))/e + B\*b\*\*2\*d\*\*2\*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e\*\*(5\*n), Abs(x) < 1), (-log(1/x)/e\*\*(5\*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e\*\*(5\*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e\*\*(5\*n), True))/e, Eq(m, -5\*n - 1)), (A\*a\*\*2\*c\*\*2\*Piecewise((-1/(4\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*a\*\*2\*c\*d\*

```

Piecewise((-x**n/(3*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + A*a**2*
d**2*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e
+ 2*A*a*b*c**2*Piecewise((-x**n/(3*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), Tru
e))/e + 4*A*a*b*c*d*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (lo
g(x), True))/e + 2*A*a*b*d**2*Piecewise((-x**(3*n)/(n*(e*x)**(4*n)), Ne(n,
0)), (log(x), True))/e + A*b**2*c**2*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)
), Ne(n, 0)), (log(x), True))/e + 2*A*b**2*c*d*Piecewise((-x**(3*n)/(n*(e*x)
)**(4*n)), Ne(n, 0)), (log(x), True))/e + A*b**2*d**2*Piecewise((0, (Abs(x)
< 1) & (1/Abs(x) < 1)), (log(x)/e**(4*n), Abs(x) < 1), (-log(1/x)/e**(4*n)
, 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + meijer
g(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), True))/e + B*a**2*c**2*Piecewise
((-x**n/(3*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + 2*B*a**2*c*d*Pie
cewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + B*a**2
*d**2*Piecewise((-x**(3*n)/(n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e +
2*B*a*b*c**2*Piecewise((-x**(2*n)/(2*n*(e*x)**(4*n)), Ne(n, 0)), (log(x),
True))/e + 4*B*a*b*c*d*Piecewise((-x**(3*n)/(n*(e*x)**(4*n)), Ne(n, 0)), (l
og(x), True))/e + 2*B*a*b*d**2*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1))
, (log(x)/e**(4*n), Abs(x) < 1), (-log(1/x)/e**(4*n), 1/Abs(x) < 1), (-meij
erg(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + meijerg(((1, 1), ()), (((), (0
, 0)), x)/e**(4*n), True))/e + B*b**2*c**2*Piecewise((-x**(3*n)/(n*(e*x)**(
4*n)), Ne(n, 0)), (log(x), True))/e + 2*B*b**2*c*d*Piecewise((0, (Abs(x) <
1) & (1/Abs(x) < 1)), (log(x)/e**(4*n), Abs(x) < 1), (-log(1/x)/e**(4*n), 1
/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + meijerg((
(1, 1), ()), (((), (0, 0)), x)/e**(4*n), True))/e + B*b**2*d**2*Piecewise((x
**5*n)/(n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e, Eq(m, -4*n - 1)), (
A*a**2*c**2*Piecewise((-1/(3*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))/e
+ 2*A*a**2*c*d*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), Tru
e))/e + A*a**2*d**2*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)), (log(
x), True))/e + 2*A*a*b*c**2*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0)),
(log(x), True))/e + 4*A*a*b*c*d*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(
n, 0)), (log(x), True))/e + 2*A*a*b*d**2*Piecewise((0, (Abs(x) < 1) & (1/Ab
s(x) < 1)), (log(x)/e**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) <
1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), (
)), (((), (0, 0)), x)/e**(3*n), True))/e + A*b**2*c**2*Piecewise((-x**(2*n)/(
n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))/e + 2*A*b**2*c*d*Piecewise((0,
(Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(3*n)...

```

**Giac [B]** Leaf count of result is larger than twice the leaf count of optimal. 8103 vs. 2(242) = 484.

time = 1.98, size = 8103, normalized size = 34.19

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="giac")

[Out]  $(B*b^2*d^2*m^5*x*x^m*x^{(5*n)}*e^m + 10*B*b^2*d^2*m^4*n*x*x^m*x^{(5*n)}*e^m + 3$   
 $5*B*b^2*d^2*m^3*n^2*x*x^m*x^{(5*n)}*e^m + 50*B*b^2*d^2*m^2*n^3*x*x^m*x^{(5*n)}*e^m + 24*B*b^2*d^2*m*n^4*x*x^m*x^{(5*n)}*e^m + 2*B*b^2*c*d*m^5*x*x^m*x^{(4*n)}*e^m + 2*B*a*b*d^2*m^5*x*x^m*x^{(4*n)}*e^m + A*b^2*d^2*m^5*x*x^m*x^{(4*n)}*e^m + 22*B*b^2*c*d*m^4*n*x*x^m*x^{(4*n)}*e^m + 22*B*a*b*d^2*m^4*n*x*x^m*x^{(4*n)}*e^m + 11*A*b^2*d^2*m^4*n*x*x^m*x^{(4*n)}*e^m + 82*B*b^2*c*d*m^3*n^2*x*x^m*x^{(4*n)}*e^m + 82*B*a*b*d^2*m^3*n^2*x*x^m*x^{(4*n)}*e^m + 41*A*b^2*d^2*m^3*n^2*x*x^m*x^{(4*n)}*e^m + 122*B*b^2*c*d*m^2*n^3*x*x^m*x^{(4*n)}*e^m + 122*B*a*b*d^2*m^2*n^3*x*x^m*x^{(4*n)}*e^m + 61*A*b^2*d^2*m^2*n^3*x*x^m*x^{(4*n)}*e^m + 60*B*b^2*c*d*m*n^4*x*x^m*x^{(4*n)}*e^m + 60*B*a*b*d^2*m*n^4*x*x^m*x^{(4*n)}*e^m + 30*A*b^2*d^2*m*n^4*x*x^m*x^{(4*n)}*e^m + B*b^2*c^2*m^5*x*x^m*x^{(3*n)}*e^m + 4*B*a*b*c*d*m^5*x*x^m*x^{(3*n)}*e^m + 2*A*b^2*c*d*m^5*x*x^m*x^{(3*n)}*e^m + B*a^2*d^2*m^5*x*x^m*x^{(3*n)}*e^m + 2*A*a*b*d^2*m^5*x*x^m*x^{(3*n)}*e^m + 12*B*b^2*c^2*m^4*n*x*x^m*x^{(3*n)}*e^m + 48*B*a*b*c*d*m^4*n*x*x^m*x^{(3*n)}*e^m + 24*A*b^2*c*d*m^4*n*x*x^m*x^{(3*n)}*e^m + 12*B*a^2*d^2*m^4*n*x*x^m*x^{(3*n)}*e^m + 24*A*a*b*d^2*m^4*n*x*x^m*x^{(3*n)}*e^m + 49*B*b^2*c^2*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 196*B*a*b*c*d*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 98*A*b^2*c*d*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 49*B*a^2*d^2*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 98*A*a*b*d^2*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 78*B*b^2*c^2*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 312*B*a*b*c*d*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 156*A*b^2*c*d*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 78*B*a^2*d^2*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 156*A*a*b*d^2*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 40*B*b^2*c^2*m*n^4*x*x^m*x^{(3*n)}*e^m + 160*B*a*b*c*d*m*n^4*x*x^m*x^{(3*n)}*e^m + 80*A*b^2*c*d*m*n^4*x*x^m*x^{(3*n)}*e^m + 40*B*a^2*d^2*m*n^4*x*x^m*x^{(3*n)}*e^m + 80*A*a*b*d^2*m*n^4*x*x^m*x^{(3*n)}*e^m + 2*B*a*b*c^2*m^5*x*x^m*x^{(2*n)}*e^m + A*b^2*c^2*m^5*x*x^m*x^{(2*n)}*e^m + 2*B*a^2*c*d*m^5*x*x^m*x^{(2*n)}*e^m + 4*A*a*b*c*d*m^5*x*x^m*x^{(2*n)}*e^m + A*a^2*d^2*m^5*x*x^m*x^{(2*n)}*e^m + 26*B*a*b*c^2*m^4*n*x*x^m*x^{(2*n)}*e^m + 13*A*b^2*c^2*m^4*n*x*x^m*x^{(2*n)}*e^m + 26*B*a^2*c*d*m^4*n*x*x^m*x^{(2*n)}*e^m + 52*A*a*b*c*d*m^4*n*x*x^m*x^{(2*n)}*e^m + 13*A*a^2*d^2*m^4*n*x*x^m*x^{(2*n)}*e^m + 118*B*a*b*c^2*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 59*A*b^2*c^2*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 118*B*a^2*c*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 236*A*a*b*c*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 59*A*a^2*d^2*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 214*B*a*b*c^2*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 107*A*b^2*c^2*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 214*B*a^2*c*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 428*A*a*b*c*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 107*A*a^2*d^2*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 120*B*a*b*c^2*m*n^4*x*x^m*x^{(2*n)}*e^m + 60*A*b^2*c^2*m*n^4*x*x^m*x^{(2*n)}*e^m + 120*B*a^2*c*d*m*n^4*x*x^m*x^{(2*n)}*e^m + 240*A*a*b*c*d*m*n^4*x*x^m*x^{(2*n)}*e^m + 60*A*a^2*d^2*m*n^4*x*x^m*x^{(2*n)}*e^m + B*a^2*c^2*m^5*x*x^m*x^n*e^m + 2*A*a*b*c^2*m^5*x*x^m*x^n*e^m + 2*A*a^2*c*d*m^5*x*x^m*x^n*e^m + 14*B*a^2*c^2*m^4*n*x*x^m*x^n*e^m + 28*A*a*b*c^2*m^4*n*x*x^m*x^n*e^m + 28*A*a^2*c*d*m^4*n*x*x^m*x^n*e^m + 71*B*a^2*c^2*m^3*n^2*x*x^m*x^n*e^m + 142*A*a*b*c^2*m^3*n^2*x*x^m*x^n*e^m + 142*A*a^2*c*d*m^3*n^2*x*x^m*x^n*e^m + 154*B*a^2*c^2*m^2*n^3*x*x^m*x^n*e^m + 308*A*a*b*c^2*m^2*n^3*x*x^m*x^n*e^m + 308*A*a^2*c*d*m^2*n^3*x*x^m*x^n*e^m + 120*B*a^2*c^2*m*n^4*x*x^m*x^n*e^m + 240*A*a*b*c^2*m*n^4*x*x^m*x^n*e^m + 240*A*a^2*c*d*m*n^4*x*x^m*x^n*e^m + A*a^2*c^2*m^5*x^m*e^m + 15*A*a^2*c^2*m^4*n*x*x^m*e^m + 85*A*a^2*c^2*m^3*n^2*x*x^m*e^m +$

$$\begin{aligned}
& 225*A*a^2*c^2*m^2*n^3*x*x^m*e^m + 274*A*a^2*c^2*m*n^4*x*x^m*e^m + 120*A*a^2 \\
& *c^2*n^5*x*x^m*e^m + 5*B*b^2*d^2*m^4*x*x^m*x^(5*n)*e^m + 40*B*b^2*d^2*m^3*n \\
& *x*x^m*x^(5*n)*e^m + 105*B*b^2*d^2*m^2*n^2*x*x^m*x^(5*n)*e^m + 100*B*b^2*d^ \\
& 2*m*n^3*x*x^m*x^(5*n)*e^m + 24*B*b^2*d^2*n^4*x*x^m*x^(5*n)*e^m + 10*B*b^2*c \\
& *d*m^4*x*x^m*x^(4*n)*e^m + 10*B*a*b*d^2*m^4*x*x^m*x^(4*n)*e^m + 5*A*b^2*d^2 \\
& *m^4*x*x^m*x^(4*n)*e^m + 88*B*b^2*c*d*m^3*n*x*x^m*x^(4*n)*e^m + 88*B*a*b*d^ \\
& 2*m^3*n*x*x^m*x^(4*n)*e^m + 44*A*b^2*d^2*m^3*n*x*x^m*x^(4*n)*e^m + 246*B*b^ \\
& 2*c*d*m^2*n^2*x*x^m*x^(4*n)*e^m + 246*B*a*b*d^2*m^2*n^2*x*x^m*x^(4*n)*e^m + \\
& 123*A*b^2*d^2*m^2*n^2*x*x^m*x^(4*n)*e^m + 244*B*b^2*c*d*m*n^3*x*x^m*x^(4*n \\
& )*e^m + 244*B*a*b*d^2*m*n^3*x*x^m*x^(4*n)*e^m + 122*A*b^2*d^2*m*n^3*x*x^m*x \\
& ^{(4*n)*e^m + 60*B*b^2*c*d*n^4*x*x^m*x^(4*n)*e^m + 60*B*a*b*d^2*n^4*x*x^m*x \\
& ^{(4*n)*e^m + 30*A*b^2*d^2*n^4*x*x^m*x^(4*n)*e^m + 5*B*b^2*c^2*m^4*x*x^m*x^(3 \\
& *n)*e^m + 20*B*a*b*c*d*m^4*x*x^m*x^(3*n)*e^m + 10*A*b^2*c*d*m^4*x*x^m*x^(3* \\
& n)*e^m + 5*B*a^2*d^2*m^4*x*x^m*x^(3*n)*e^m + 10*A*a*b*d^2*m^4*x*x^m*x^(3*n) \\
& *e^m + 48*B*b^2*c^2*m^3*n*x*x^m*x^(3*n)*e^m + 192*B*a*b*c*d*m^3*n*x*x^m*x^( \\
& 3*n)*e^m + 96*A*b^2*c*d*m^3*n*x*x^m*x^(3*n)*e^m + 48*B*a^2*d^2*m^3*n*x*x^m*x \\
& ^{(3*n)*e^m + 96*A*a*b*d^2*m^3*n*x*x^m*x^(3*n)*e^m + 147*B*b^2*c^2*m^2*n^2* \\
& x*x^m*x^(3*n)*e^m + 588*B*a*b*c*d*m^2*n^2*x*x^m*x^(3*n)*e^m + 294*A*b^2*c*d \\
& *m^2*n^2*x*x^m*x^(3*n)*e^m + 147*B*a^2*d^2*m^2*n^2*x*x^m*x^(3*n)*e^m + 294* \\
& A*a*b*d^2*m^2*n^2*x*x^m*x^(3*n)*e^m + 156*B*b^2*c^2*m*n^3*x*x^m*x^(3*n)*e^m \\
& + 624*B*a*b*c*d*m*n^3*x*x^m*x^(3*n)*e^m + 312*A*b^2*c*d*m*n^3*x*x^m*x^(3*n \\
& )*e^m + 156*B*a^2*d^2*m*n^3*x*x^m*x^(3*n)*e^m + \dots
\end{aligned}$$

Mupad [B]

time = 5.59, size = 1119, normalized size = 4.72

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)^2*(c + d*x^n)^2,x)$

[Out]  $(x*x^{(2*n)}*(e*x)^m*(A*a^2*d^2 + A*b^2*c^2 + 2*B*a*b*c^2 + 2*B*a^2*c*d + 4*A$   
 $*a*b*c*d)*(4*m + 13*n + 39*m*n + 118*m*n^2 + 39*m^2*n + 107*m*n^3 + 13*m^3$   
 $n + 6*m^2 + 4*m^3 + m^4 + 59*n^2 + 107*n^3 + 60*n^4 + 59*m^2*n^2 + 1))/(5*m$   
 $+ 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4$   
 $+ 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 1$   
 $20*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (x*x^{(3*n)}*(e*x)^m*($   
 $B*a^2*d^2 + B*b^2*c^2 + 2*A*a*b*d^2 + 2*A*b^2*c*d + 4*B*a*b*c*d)*(4*m + 12*$   
 $n + 36*m*n + 98*m*n^2 + 36*m^2*n + 78*m*n^3 + 12*m^3*n + 6*m^2 + 4*m^3 + m^$   
 $4 + 49*n^2 + 78*n^3 + 40*n^4 + 49*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*$   
 $m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 1$   
 $0*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 +$   
 $225*m^2*n^3 + 85*m^3*n^2 + 1) + (A*a^2*c^2*x*(e*x)^m)/(m + 1) + (b*d*x*x^{(4$   
 $*n)}*(e*x)^m*(A*b*d + 2*B*a*d + 2*B*b*c)*(4*m + 11*n + 33*m*n + 82*m*n^2 + 3$   
 $3*m^2*n + 61*m*n^3 + 11*m^3*n + 6*m^2 + 4*m^3 + m^4 + 41*n^2 + 61*n^3 + 30*$

$$\begin{aligned}
& n^4 + 41m^2n^2 + 1)) / (5m + 15n + 60mn + 255m^2n^2 + 90m^2n + 450m^3n^3 + 60m^3n + 274m^3n^4 + 15m^4n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2n^2 + 225m^2n^3 + 85m^3n^2 + 1) \\
& + (B*b^2*d^2*x*x^{(5n)}*(e*x)^m*(4m + 10n + 30mn + 70m^2n^2 + 30m^2n + 50m^3n^3 + 10m^3n + 6m^2 + 4m^3 + m^4 + 35n^2 + 50n^3 + 24n^4 + 35m^2n^2 + 1)) / (5m + 15n + 60mn + 255m^2n^2 + 90m^2n + 450m^3n^3 + 60m^3n + 274m^3n^4 + 15m^4n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2n^2 + 225m^2n^3 + 85m^3n^2 + 1) \\
& + (a*c*x*x^n*(e*x)^m*(2A*a*d + 2A*b*c + B*a*c)*(4m + 14n + 42mn + 142m^2n^2 + 42m^2n + 154m^3n^3 + 14m^3n + 6m^2 + 4m^3 + m^4 + 71n^2 + 154n^3 + 120n^4 + 71m^2n^2 + 1)) / (5m + 15n + 60mn + 255m^2n^2 + 90m^2n + 450m^3n^3 + 60m^3n + 274m^3n^4 + 15m^4n + 10m^2 + 10m^3 + 5m^4 + m^5 + 85n^2 + 225n^3 + 274n^4 + 120n^5 + 255m^2n^2 + 225m^2n^3 + 85m^3n^2 + 1)
\end{aligned}$$



### 3.10 $\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=160

$$\frac{c(ABC + aBc + 2aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(ad(2Bc + Ad) + bc(Bc + 2Ad))x^{1+2n}(ex)^m}{1+m+2n} + \frac{d(2bBc + Abd + aBd)x^{1+3n}(ex)^m}{1+m+3n}$$

[Out]  $c*(2*A*a*d+A*b*c+B*a*c)*x^{(1+n)}*(e*x)^m/(1+m+n)+(a*d*(A*d+2*B*c)+b*c*(2*A*d+B*c))*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+d*(A*b*d+B*a*d+2*B*b*c)*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+b*B*d^2*x^{(1+4*n)}*(e*x)^m/(1+m+4*n)+a*A*c^2*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.12, antiderivative size = 160, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ ,

Rules used = {584, 20, 30}

$$\frac{cx^{n+1}(ex)^m(2aAd + aBc + Abc)}{m+n+1} + \frac{x^{2n+1}(ex)^m(ad(Ad + 2Bc) + bc(2Ad + Bc))}{m+2n+1} + \frac{dx^{3n+1}(ex)^m(aBd + Abd + 2bBc)}{m+3n+1} + \frac{aAc^2(ex)^{m+1}}{e(m+1)} + \frac{bBd^2x^{4n+1}(ex)^m}{m+4n+1}$$

Antiderivative was successfully verified.

[In] `Int[(e*x)^m*(a + b*x^n)*(A + B*x^n)*(c + d*x^n)^2,x]`

[Out]  $(c*(A*b*c + a*B*c + 2*a*A*d)*x^{(1+n)}*(e*x)^m)/(1+m+n) + ((a*d*(2*B*c + A*d) + b*c*(B*c + 2*A*d))*x^{(1+2*n)}*(e*x)^m)/(1+m+2*n) + (d*(2*b*B*c + A*b*d + a*B*d)*x^{(1+3*n)}*(e*x)^m)/(1+m+3*n) + (b*B*d^2*x^{(1+4*n)}*(e*x)^m)/(1+m+4*n) + (a*A*c^2*(e*x)^{(1+m)})/(e*(1+m))$

Rule 20

`Int[(u_.)*((a_.)*(v_))^(m_.)*((b_.)*(v_))^(n_), x_Symbol] := Dist[b^IntPart[n]*((b*v)^FracPart[n]/(a^IntPart[n]*(a*v)^FracPart[n])), Int[u*(a*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]`

Rule 30

`Int[(x_)^(m_.), x_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]`

Rule 584

`Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]`

Rubi steps

$$\begin{aligned}
\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^2 dx &= \int (aAc^2(ex)^m + c(ABC + aBc + 2aAd)x^n(ex)^m + (ad(2Bc + \\
&= \frac{aAc^2(ex)^{1+m}}{e(1+m)} + (bBd^2) \int x^{4n}(ex)^m dx + (c(ABC + aBc + 2aAd)x^n(ex)^m \\
&= \frac{aAc^2(ex)^{1+m}}{e(1+m)} + (bBd^2 x^{-m}(ex)^m) \int x^{m+4n} dx + (c(ABC + aBc + 2aAd)x^n(ex)^m \\
&= \frac{c(ABC + aBc + 2aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{(ad(2Bc + Ad) + bc(Bc + 2Ad))x^{m+n}}{1+m+n}
\end{aligned}$$

**Mathematica [A]**

time = 0.34, size = 129, normalized size = 0.81

$$x(ex)^m \left( \frac{aAc^2}{1+m} + \frac{c(ABC + aBc + 2aAd)x^n}{1+m+n} + \frac{(ad(2Bc + Ad) + bc(Bc + 2Ad))x^{2n}}{1+m+2n} + \frac{d(2bBc + Abd + aBd)x^{3n}}{1+m+3n} + \frac{bBd^2x^{4n}}{1+m+4n} \right)$$

Antiderivative was successfully verified.

**[In]** Integrate[(e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n)\*(c + d\*x^n)^2,x]

**[Out]** x\*(e\*x)^m\*((a\*A\*c^2)/(1+m) + (c\*(A\*b\*c + a\*B\*c + 2\*a\*A\*d)\*x^n)/(1+m+n) + ((a\*d\*(2\*B\*c + A\*d) + b\*c\*(B\*c + 2\*A\*d))\*x^(2\*n))/(1+m+2\*n) + (d\*(2\*b\*B\*c + A\*b\*d + a\*B\*d)\*x^(3\*n))/(1+m+3\*n) + (b\*B\*d^2\*x^(4\*n))/(1+m+4\*n))

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.38, size = 2410, normalized size = 15.06

method	result	size
risch	Expression too large to display	2410

Verification of antiderivative is not currently implemented for this CAS.

**[In]** int((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^2,x,method=\_RETURNVERBOSE)

**[Out]** x\*(19\*A\*a\*d^2\*n^2\*(x^n)^2+4\*A\*b\*c^2\*m^3\*x^n+48\*A\*a\*c\*d\*n^3\*x^n+24\*A\*b\*c^2\*m\*n^3\*x^n+6\*A\*b\*d^2\*m^2\*(x^n)^3+14\*A\*b\*d^2\*n^2\*(x^n)^3+B\*a\*c^2\*m^4\*x^n+6\*B\*a\*d^2\*m^2\*(x^n)^3+14\*B\*a\*d^2\*n^2\*(x^n)^3+56\*B\*b\*c\*d\*m\*n^2\*(x^n)^3+18\*A\*a\*c\*d\*m^3\*n\*x^n+52\*A\*a\*c\*d\*m^2\*n^2\*x^n+48\*A\*a\*c\*d\*m\*n^3\*x^n+12\*A\*a\*d^2\*m\*n^3\*(x^n)^2+2\*A\*b\*c\*d\*m^4\*(x^n)^2+(x^n)^3\*B\*a\*d^2+(x^n)^2\*A\*a\*d^2+30\*A\*a\*c^2\*m\*n+38\*A\*a\*d^2\*m\*n^2\*(x^n)^2+8\*A\*a\*c\*d\*m^3\*x^n+A\*a\*c^2+12\*B\*a\*c\*d\*m^2\*(x^n)^2+38\*B\*a\*c\*d\*n^2\*(x^n)^2+18\*A\*a\*c\*d\*x^n\*n+38\*A\*b\*c\*d\*n^2\*(x^n)^2+27\*B\*a\*c^2\*m^2\*n\*x^n+12\*A\*b\*c\*d\*m^2\*(x^n)^2+16\*A\*b\*c\*d\*(x^n)^2\*n+9\*A\*b\*c^2\*m^3\*n\*x^n+26\*A\*b\*c^2\*m^2\*n^2\*x^n+27\*A\*b\*c^2\*m\*n\*x^n+16\*B\*a\*c\*d\*(x^n)^2\*n+21\*A\*b\*d^2\*m^2\*n\*(x^n)^3+28\*A\*b\*d^2\*m\*n^2\*(x^n)^3+2\*B\*a\*c\*d\*m^4\*(x^n)^2+21\*B\*a\*d^2\*m^2\*n\*(x^n)^3

$$\begin{aligned}
& \hat{n})^3+28*B*a*d^2*m*n^2*(x^n)^3+8*B*b*c^2*m^3*n*(x^n)^2+52*A*b*c^2*m*n^2*x^n \\
& +24*B*b*c^2*m^2*n*(x^n)^2+38*B*b*c^2*m*n^2*(x^n)^2+42*B*b*c*d*m*n*(x^n)^3+5 \\
& 4*A*a*c*d*m^2*n*x^n+4*A*a*c^2*m^3+50*A*a*c^2*n^3+6*A*a*c^2*m^2+35*A*a*c^2*n \\
& ^2+(x^n)^3*A*b*d^2+(x^n)^2*B*b*c^2+x^n*c^2*A*b+x^n*c^2*B*a+4*A*a*c^2*m+4*A \\
& b*d^2*(x^n)^3+m+21*A*b*d^2*m*n*(x^n)^3+9*B*a*c^2*m^3*n*x^n+26*B*a*c^2*m^2*n \\
& ^2*x^n+B*b*d^2*(x^n)^4+8*B*a*c*d*m^3*(x^n)^2+24*B*a*c*d*n^3*(x^n)^2+21*B*a \\
& d^2*m*n*(x^n)^3+19*B*b*c^2*m^2*n^2*(x^n)^2+8*A*a*d^2*(x^n)^2*n+6*A*b*c^2*m^2 \\
& 2*x^n+26*A*b*c^2*n^2*x^n+6*B*a*c^2*m^2*x^n+26*B*a*c^2*n^2*x^n+A*a*c^2*m^4+4 \\
& 8*A*b*c*d*m^2*n*(x^n)^2+76*A*b*c*d*m*n^2*(x^n)^2+48*B*a*c*d*m^2*n*(x^n)^2+7 \\
& 6*B*a*c*d*m*n^2*(x^n)^2+10*A*a*c^2*n+24*A*a*c^2*n^4+24*A*b*c^2*n^3*x^n+4*B \\
& b*c^2*m^3*(x^n)^2+12*B*b*c^2*n^3*(x^n)^2+4*m*B*b*d^2*(x^n)^4+6*B*b*d^2*(x^n \\
& )^4*n+6*A*a*d^2*m^2*(x^n)^2+19*A*a*d^2*m^2*n^2*(x^n)^2+16*B*a*c*d*m^3*n*(x \\
& n)^2+38*B*a*c*d*m^2*n^2*(x^n)^2+24*B*a*c*d*m*n^3*(x^n)^2+42*B*b*c*d*m^2*n*( \\
& x^n)^3+6*B*b*d^2*m^3*n*(x^n)^4+11*B*b*d^2*m^2*n^2*(x^n)^4+24*B*a*c^2*m*n^3* \\
& x^n+27*B*a*c^2*m*n*x^n+24*A*a*d^2*m*n*(x^n)^2+4*A*b*c^2*x^n*m+9*A*b*c^2*x^n \\
& *n+2*A*b*c*d*(x^n)^2+4*B*a*c^2*x^n*m+12*B*b*c^2*m*n^3*(x^n)^2+8*B*b*c*d*m^3 \\
& *(x^n)^3+16*B*b*c*d*n^3*(x^n)^3+18*B*b*d^2*m*n*(x^n)^4+2*A*a*c*d*m^4*x^n+24 \\
& *A*a*d^2*m^2*n*(x^n)^2+27*A*b*c^2*m^2*n*x^n+8*B*a*c*d*(x^n)^2*m+8*A*b*c*d*m \\
& ^3*(x^n)^2+24*A*b*c*d*n^3*(x^n)^2+8*A*b*c*d*(x^n)^2*m+24*B*b*c^2*m*n*(x^n)^ \\
& 2+8*B*b*c*d*(x^n)^3+m+14*B*b*c*d*(x^n)^3*n+12*A*a*c*d*m^2*x^n+52*A*a*c*d*n^ \\
& 2*x^n+12*B*b*c*d*m^2*(x^n)^3+28*B*b*c*d*n^2*(x^n)^3+8*A*a*c*d*x^n*m+52*B*a \\
& c^2*m*n^2*x^n+104*A*a*c*d*m*n^2*x^n+48*A*b*c*d*m*n*(x^n)^2+48*B*a*c*d*m*n*( \\
& x^n)^2+54*A*a*c*d*m*n*x^n+6*B*b*d^2*m*n^3*(x^n)^4+7*A*b*d^2*m^3*n*(x^n)^3+1 \\
& 4*A*b*d^2*m^2*n^2*(x^n)^3+8*A*b*d^2*m*n^3*(x^n)^3+7*B*a*d^2*m^3*n*(x^n)^3+1 \\
& 4*B*a*d^2*m^2*n^2*(x^n)^3+8*B*a*d^2*m*n^3*(x^n)^3+2*B*b*c*d*m^4*(x^n)^3+18* \\
& B*b*d^2*m^2*n*(x^n)^4+22*B*b*d^2*m*n^2*(x^n)^4+8*A*a*d^2*m^3*n*(x^n)^2+16*B \\
& *b*c*d*m*n^3*(x^n)^3+16*A*b*c*d*m^3*n*(x^n)^2+38*A*b*c*d*m^2*n^2*(x^n)^2+24 \\
& *A*b*c*d*m*n^3*(x^n)^2+10*A*a*c^2*m^3*n+35*A*a*c^2*m^2*n^2+50*A*a*c^2*m*n^3 \\
& +9*B*a*c^2*x^n*n+2*B*a*c*d*(x^n)^2+2*A*a*c*d*x^n+14*B*b*c*d*m^3*n*(x^n)^3+2 \\
& 8*B*b*c*d*m^2*n^2*(x^n)^3+B*b*c^2*m^4*(x^n)^2+6*B*b*d^2*m^2*(x^n)^4+11*B*b \\
& d^2*n^2*(x^n)^4+4*A*a*d^2*m^3*(x^n)^2+12*A*a*d^2*n^3*(x^n)^2+A*b*c^2*m^4*x \\
& n+7*A*b*d^2*(x^n)^3*n+4*B*a*c^2*m^3*x^n+24*B*a*c^2*n^3*x^n+4*B*a*d^2*(x^n)^ \\
& 3*m+7*B*a*d^2*(x^n)^3*n+6*B*b*c^2*m^2*(x^n)^2+19*B*b*c^2*n^2*(x^n)^2+4*A*a \\
& d^2*(x^n)^2*m+4*B*b*c^2*(x^n)^2*m+B*b*d^2*m^4*(x^n)^4+A*b*d^2*m^4*(x^n)^3+B \\
& *a*d^2*m^4*(x^n)^3+4*B*b*d^2*m^3*(x^n)^4+6*B*b*d^2*n^3*(x^n)^4+A*a*d^2*m^4* \\
& (x^n)^2+4*A*b*d^2*m^3*(x^n)^3+8*A*b*d^2*n^3*(x^n)^3+4*B*a*d^2*m^3*(x^n)^3+8 \\
& *B*a*d^2*n^3*(x^n)^3+8*B*b*c^2*(x^n)^2*n+2*B*b*c*d*(x^n)^3+30*A*a*c^2*m^2*n \\
& +70*A*a*c^2*m*n^2)/(1+m)/(1+m+n)/(1+m+2*n)/(1+m+3*n)/(1+m+4*n)*exp(1/2*m*(- \\
& I*Pi*csgn(I*e*x)^3+I*Pi*csgn(I*e*x)^2*csgn(I*e)+I*Pi*csgn(I*e*x)^2*csgn(I*x \\
& )-I*Pi*csgn(I*e*x)*csgn(I*e)*csgn(I*x)+2*ln(e)+2*ln(x))
\end{aligned}$$

Maxima [A]

time = 0.37, size = 310, normalized size = 1.94

$$\frac{(x)^{m+1} A a d^{j-3}}{m+1} + \frac{B b d^{j-2} m^2 n^2 (x^n)^3}{m+4n+1} + \frac{2 B b d^{j-2} m^2 n^2 (x^n)^3}{m+3n+1} + \frac{B a d^{j-2} m^2 n^2 (x^n)^3}{m+3n+1} + \frac{A b d^{j-2} m^2 n^2 (x^n)^3}{m+3n+1} + \frac{B a d^{j-2} m^2 n^2 (x^n)^3}{m+2n+1} + \frac{2 B a d^{j-2} m^2 n^2 (x^n)^3}{m+2n+1} + \frac{2 A b d^{j-2} m^2 n^2 (x^n)^3}{m+2n+1} + \frac{A a d^{j-2} m^2 n^2 (x^n)^3}{m+2n+1} + \frac{B a d^{j-2} m^2 n^2 (x^n)^3}{m+n+1} + \frac{A b d^{j-2} m^2 n^2 (x^n)^3}{m+n+1} + \frac{2 A a d^{j-2} m^2 n^2 (x^n)^3}{m+n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="maxima")
```

```
[Out] (x*e)^(m + 1)*A*a*c^2*e^(-1)/(m + 1) + B*b*d^2*x*e^(m*log(x) + 4*n*log(x) +
m)/(m + 4*n + 1) + 2*B*b*c*d*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1)
+ B*a*d^2*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + A*b*d^2*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + B*b*c^2*x*e^(m*log(x) + 2*n*log(x)
+ m)/(m + 2*n + 1) + 2*B*a*c*d*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1)
+ 2*A*b*c*d*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + A*a*d^2*x*e^(
m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + B*a*c^2*x*e^(m*log(x) + n*log(x)
+ m)/(m + n + 1) + A*b*c^2*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1) + 2*A
*a*c*d*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1)
```

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 1411 vs.  $2(164) = 328$ .

time = 1.81, size = 1411, normalized size = 8.82

---

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)*(A+B*x^n)*(c+d*x^n)^2,x, algorithm="fricas")
```

```
[Out] ((B*b*d^2*m^4 + 4*B*b*d^2*m^3 + 6*B*b*d^2*m^2 + 4*B*b*d^2*m + B*b*d^2 + 6*(
B*b*d^2*m + B*b*d^2)*n^3 + 11*(B*b*d^2*m^2 + 2*B*b*d^2*m + B*b*d^2)*n^2 + 6
*(B*b*d^2*m^3 + 3*B*b*d^2*m^2 + 3*B*b*d^2*m + B*b*d^2)*n)*x*x^(4*n)*e^(m*lo
g(x) + m) + ((2*B*b*c*d + (B*a + A*b)*d^2)*m^4 + 2*B*b*c*d + 4*(2*B*b*c*d +
(B*a + A*b)*d^2)*m^3 + 8*(2*B*b*c*d + (B*a + A*b)*d^2 + (2*B*b*c*d + (B*a
+ A*b)*d^2)*m)*n^3 + (B*a + A*b)*d^2 + 6*(2*B*b*c*d + (B*a + A*b)*d^2)*m^2
+ 14*(2*B*b*c*d + (B*a + A*b)*d^2 + (2*B*b*c*d + (B*a + A*b)*d^2)*m^2 + 2*(
2*B*b*c*d + (B*a + A*b)*d^2)*m)*n^2 + 4*(2*B*b*c*d + (B*a + A*b)*d^2)*m + 7
*(2*B*b*c*d + (2*B*b*c*d + (B*a + A*b)*d^2)*m^3 + (B*a + A*b)*d^2 + 3*(2*B*
b*c*d + (B*a + A*b)*d^2)*m^2 + 3*(2*B*b*c*d + (B*a + A*b)*d^2)*m)*n)*x*x^(3
*n)*e^(m*log(x) + m) + ((B*b*c^2 + A*a*d^2 + 2*(B*a + A*b)*c*d)*m^4 + B*b*c
^2 + A*a*d^2 + 4*(B*b*c^2 + A*a*d^2 + 2*(B*a + A*b)*c*d)*m^3 + 12*(B*b*c^2
+ A*a*d^2 + 2*(B*a + A*b)*c*d + (B*b*c^2 + A*a*d^2 + 2*(B*a + A*b)*c*d)*m)*
n^3 + 2*(B*a + A*b)*c*d + 6*(B*b*c^2 + A*a*d^2 + 2*(B*a + A*b)*c*d)*m^2 + 1
9*(B*b*c^2 + A*a*d^2 + 2*(B*a + A*b)*c*d + (B*b*c^2 + A*a*d^2 + 2*(B*a + A
b)*c*d)*m^2 + 2*(B*b*c^2 + A*a*d^2 + 2*(B*a + A*b)*c*d)*m)*n^2 + 4*(B*b*c^2
+ A*a*d^2 + 2*(B*a + A*b)*c*d)*m + 8*(B*b*c^2 + A*a*d^2 + (B*b*c^2 + A*a*d
^2 + 2*(B*a + A*b)*c*d)*m^3 + 2*(B*a + A*b)*c*d + 3*(B*b*c^2 + A*a*d^2 + 2*
(B*a + A*b)*c*d)*m^2 + 3*(B*b*c^2 + A*a*d^2 + 2*(B*a + A*b)*c*d)*m)*n)*x*x^(
2*n)*e^(m*log(x) + m) + ((2*A*a*c*d + (B*a + A*b)*c^2)*m^4 + 2*A*a*c*d + 4
*(2*A*a*c*d + (B*a + A*b)*c^2)*m^3 + 24*(2*A*a*c*d + (B*a + A*b)*c^2 + (2*A
*a*c*d + (B*a + A*b)*c^2)*m)*n^3 + (B*a + A*b)*c^2 + 6*(2*A*a*c*d + (B*a +
A*b)*c^2)*m^2 + 26*(2*A*a*c*d + (B*a + A*b)*c^2 + (2*A*a*c*d + (B*a + A*b)*
```

$$c^2)m^2 + 2*(2*A*a*c*d + (B*a + A*b)*c^2)*m)*n^2 + 4*(2*A*a*c*d + (B*a + A*b)*c^2)*m + 9*(2*A*a*c*d + (2*A*a*c*d + (B*a + A*b)*c^2)*m^3 + (B*a + A*b)*c^2 + 3*(2*A*a*c*d + (B*a + A*b)*c^2)*m^2 + 3*(2*A*a*c*d + (B*a + A*b)*c^2)*m)*n)*x^n*e^{(m*\log(x) + m) + (A*a*c^2*m^4 + 24*A*a*c^2*n^4 + 4*A*a*c^2*m^3 + 6*A*a*c^2*m^2 + 4*A*a*c^2*m + A*a*c^2 + 50*(A*a*c^2*m + A*a*c^2)*n^3 + 35*(A*a*c^2*m^2 + 2*A*a*c^2*m + A*a*c^2)*n^2 + 10*(A*a*c^2*m^3 + 3*A*a*c^2*m^2 + 3*A*a*c^2*m + A*a*c^2)*n)*x*e^{(m*\log(x) + m)}}/(m^5 + 24*(m + 1)*n^4 + 5*m^4 + 50*(m^2 + 2*m + 1)*n^3 + 10*m^3 + 35*(m^3 + 3*m^2 + 3*m + 1)*n^2 + 10*m^2 + 10*(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n + 5*m + 1)$$

**Sympy** [B] Leaf count of result is larger than twice the leaf count of optimal.  $24932$  vs.  $2(156) = 312$ .

time = 88.96, size = 24932, normalized size = 155.82

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*2,x)

[Out] Piecewise(((A + B)\*(a + b)\*(c + d)\*\*2\*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A\*a\*c\*\*2\*log(x) + 2\*A\*a\*c\*d\*x\*\*n/n + A\*a\*d\*\*2\*x\*\*(2\*n)/(2\*n) + A\*b\*c\*\*2\*x\*\*n/n + A\*b\*c\*d\*x\*\*(2\*n)/n + B\*a\*d\*\*2\*x\*\*(3\*n)/(3\*n) + B\*b\*c\*\*2\*x\*\*n/n + B\*a\*c\*d\*x\*\*(2\*n)/n + B\*a\*d\*\*2\*x\*\*(3\*n)/(3\*n) + B\*b\*c\*\*2\*x\*\*(2\*n)/(2\*n) + 2\*B\*b\*c\*d\*x\*\*(3\*n)/(3\*n) + B\*b\*d\*\*2\*x\*\*(4\*n)/(4\*n))/e, Eq(m, -1)), (A\*a\*c\*\*2\*Piecewise((-1/(4\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*a\*c\*d\*Piecewise((-x\*\*n/(3\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + A\*a\*d\*\*2\*Piecewise((-x\*\*(2\*n)/(2\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + A\*b\*c\*\*2\*Piecewise((-x\*\*n/(3\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*b\*c\*d\*Piecewise((-x\*\*(2\*n)/(2\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + A\*b\*d\*\*2\*Piecewise((-x\*\*(3\*n)/(n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + B\*a\*c\*\*2\*Piecewise((-x\*\*n/(3\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 2\*B\*a\*c\*d\*Piecewise((-x\*\*(2\*n)/(2\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + B\*a\*d\*\*2\*Piecewise((-x\*\*(3\*n)/(n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + B\*b\*c\*\*2\*Piecewise((-x\*\*(2\*n)/(2\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 2\*B\*b\*c\*d\*Piecewise((-x\*\*(3\*n)/(n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + B\*b\*d\*\*2\*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e\*\*(4\*n), Abs(x) < 1), (-log(1/x)/e\*\*(4\*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e\*\*(4\*n) + meijerg(((1, 1), ()), ((), (0, 0)), x)/e\*\*(4\*n), True))/e, Eq(m, -4\*n - 1)), (A\*a\*c\*\*2\*Piecewise((-1/(3\*n\*(e\*x)\*\*(3\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*a\*c\*d\*Piecewise((-x\*\*n/(2\*n\*(e\*x)\*\*(3\*n)), Ne(n, 0)), (log(x), True))/e + A\*a\*d\*\*2\*Piecewise((-x\*\*(2\*n)/(n\*(e\*x)\*\*(3\*n)), Ne(n, 0)), (log(x), True))/e + A\*b\*c\*\*2\*Piecewise((-x\*\*n/(2\*n\*(e\*x)\*\*(3\*n)), Ne(n, 0)), (log(x), True))/e + 2\*A\*b\*c\*d\*Piecewise((-x\*\*(2\*n)/(n\*(e\*x)\*\*(3\*n)), Ne(n, 0)), (log(x), True))/e + A\*b\*d\*\*2\*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e\*\*(3\*n), Abs(x)

```

< 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0),
()), x)/e**(3*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(3*n), True))/
e + B*a*c**2*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True)
)/e + 2*B*a*c*d*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)), (log(x),
True))/e + B*a*d**2*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e
**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-meijerg(((), (1
, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e
**(3*n), True))/e + B*b*c**2*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)
)), (log(x), True))/e + 2*B*b*c*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) <
1)), (log(x)/e**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-m
eijerg(((), (1, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), ()), (((),
(0, 0)), x)/e**(3*n), True))/e + B*b*d**2*Piecewise((x**(4*n)/(n*(e*x)**(3
*n)), Ne(n, 0)), (log(x), True))/e, Eq(m, -3*n - 1)), (A*a*c**2*Piecewise((
-1/(2*n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + 2*A*a*c*d*Piecewise((
-x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + A*a*d**2*Piecewise((
0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n), Abs(x) < 1), (-log(1/x)
)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(2*n)
) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n), True))/e + A*b*c**2*Pi
ecewise((-x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + 2*A*b*c*d*P
iecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n), Abs(x) < 1),
(-log(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()),
x)/e**(2*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n), True))/e + A
*b*d**2*Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e
+ B*a*c**2*Piecewise((-x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e
+ 2*B*a*c*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n),
Abs(x) < 1), (-log(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), (
(0, 0), ()), x)/e**(2*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n),
True))/e + B*a*d**2*Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(n, 0)), (log(
x), True))/e + B*b*c**2*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(
x)/e**(2*n), Abs(x) < 1), (-log(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg((()
, (1, 1)), ((0, 0), ()), x)/e**(2*n) + meijerg(((1, 1), ()), (((), (0, 0)),
x)/e**(2*n), True))/e + 2*B*b*c*d*Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(
n, 0)), (log(x), True))/e + B*b*d**2*Piecewise((x**(4*n)/(2*n*(e*x)**(2*n))
, Ne(n, 0)), (log(x), True))/e, Eq(m, -2*n - 1)), (A*a*c**2*Piecewise((-1/(
n*(e*x)**n), Ne(n, 0)), (log(x), True))/e + 2*A*a*c*d*Piecewise((0, (Abs(x)
< 1) & (1/Abs(x) < 1)), (log(x)/e**n, Abs(x) < 1), (-log(1/x)/e**n, 1/Abs(
x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**n + meijerg(((1, 1), (
)), (((), (0, 0)), x)/e**n, True))/e + A*a*d**2*Piecewise((x**(2*n)/(n*(e*x)
**n), Ne(n, 0)), (log(x), True))/e + A*b*c**2*Piecewise((0, (Abs(x) < 1) &
(1/Abs(x) < 1)), (log(x)/e**n, Abs(x) < 1), (-log(1/x)/e**n, 1/Abs(x) < 1),
(-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**n ...

```

**Giac [B]** Leaf count of result is larger than twice the leaf count of optimal. 3415 vs. 2(164) = 328.

time = 0.90, size = 3415, normalized size = 21.34

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="giac")

[Out]  $(B*b*d^2*m^4*x*x^m*x^{(4*n)}*e^m + 6*B*b*d^2*m^3*n*x*x^m*x^{(4*n)}*e^m + 11*B*b*d^2*m^2*n^2*x*x^m*x^{(4*n)}*e^m + 6*B*b*d^2*m*n^3*x*x^m*x^{(4*n)}*e^m + 2*B*b*c*d*m^4*x*x^m*x^{(3*n)}*e^m + B*a*d^2*m^4*x*x^m*x^{(3*n)}*e^m + A*b*d^2*m^4*x*x^m*x^{(3*n)}*e^m + 14*B*b*c*d*m^3*n*x*x^m*x^{(3*n)}*e^m + 7*B*a*d^2*m^3*n*x*x^m*x^{(3*n)}*e^m + 7*A*b*d^2*m^3*n*x*x^m*x^{(3*n)}*e^m + 28*B*b*c*d*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 14*B*a*d^2*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 14*A*b*d^2*m^2*n^2*x*x^m*x^{(3*n)}*e^m + 16*B*b*c*d*m*n^3*x*x^m*x^{(3*n)}*e^m + 8*B*a*d^2*m*n^3*x*x^m*x^{(3*n)}*e^m + 8*A*b*d^2*m*n^3*x*x^m*x^{(3*n)}*e^m + B*b*c^2*m^4*x*x^m*x^{(2*n)}*e^m + 2*B*a*c*d*m^4*x*x^m*x^{(2*n)}*e^m + 2*A*b*c*d*m^4*x*x^m*x^{(2*n)}*e^m + A*a*d^2*m^4*x*x^m*x^{(2*n)}*e^m + 8*B*b*c^2*m^3*n*x*x^m*x^{(2*n)}*e^m + 16*B*a*c*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 16*A*b*c*d*m^3*n*x*x^m*x^{(2*n)}*e^m + 8*A*a*d^2*m^3*n*x*x^m*x^{(2*n)}*e^m + 19*B*b*c^2*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 38*B*a*c*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 38*A*b*c*d*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 19*A*a*d^2*m^2*n^2*x*x^m*x^{(2*n)}*e^m + 12*B*b*c^2*m*n^3*x*x^m*x^{(2*n)}*e^m + 24*B*a*c*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 24*A*b*c*d*m*n^3*x*x^m*x^{(2*n)}*e^m + 12*A*a*d^2*m*n^3*x*x^m*x^{(2*n)}*e^m + B*a*c^2*m^4*x*x^m*x^n*e^m + A*b*c^2*m^4*x*x^m*x^n*e^m + 2*A*a*c*d*m^4*x*x^m*x^n*e^m + 9*B*a*c^2*m^3*n*x*x^m*x^n*e^m + 9*A*b*c^2*m^3*n*x*x^m*x^n*e^m + 18*A*a*c*d*m^3*n*x*x^m*x^n*e^m + 26*B*a*c^2*m^2*n^2*x*x^m*x^n*e^m + 26*A*b*c^2*m^2*n^2*x*x^m*x^n*e^m + 52*A*a*c*d*m^2*n^2*x*x^m*x^n*e^m + 24*B*a*c^2*m*n^3*x*x^m*x^n*e^m + 24*A*b*c^2*m*n^3*x*x^m*x^n*e^m + 48*A*a*c*d*m*n^3*x*x^m*x^n*e^m + A*a*c^2*m^4*x*x^m*e^m + 10*A*a*c^2*m^3*n*x*x^m*e^m + 35*A*a*c^2*m^2*n^2*x*x^m*e^m + 50*A*a*c^2*m*n^3*x*x^m*e^m + 24*A*a*c^2*n^4*x*x^m*e^m + 4*B*b*d^2*m^3*x*x^m*x^{(4*n)}*e^m + 18*B*b*d^2*m^2*n*x*x^m*x^{(4*n)}*e^m + 22*B*b*d^2*m*n^2*x*x^m*x^{(4*n)}*e^m + 6*B*b*d^2*n^3*x*x^m*x^{(4*n)}*e^m + 8*B*b*c*d*m^3*x*x^m*x^{(3*n)}*e^m + 4*B*a*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 4*A*b*d^2*m^3*x*x^m*x^{(3*n)}*e^m + 42*B*b*c*d*m^2*n*x*x^m*x^{(3*n)}*e^m + 21*B*a*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 21*A*b*d^2*m^2*n*x*x^m*x^{(3*n)}*e^m + 56*B*b*c*d*m*n^2*x*x^m*x^{(3*n)}*e^m + 28*B*a*d^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 28*A*b*d^2*m*n^2*x*x^m*x^{(3*n)}*e^m + 16*B*b*c*d*n^3*x*x^m*x^{(3*n)}*e^m + 8*B*a*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 8*A*b*d^2*n^3*x*x^m*x^{(3*n)}*e^m + 4*B*b*c^2*m^3*x*x^m*x^{(2*n)}*e^m + 8*B*a*c*d*m^3*x*x^m*x^{(2*n)}*e^m + 8*A*b*c*d*m^3*x*x^m*x^{(2*n)}*e^m + 4*A*a*d^2*m^3*x*x^m*x^{(2*n)}*e^m + 24*B*b*c^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 48*B*a*c*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 48*A*b*c*d*m^2*n*x*x^m*x^{(2*n)}*e^m + 24*A*a*d^2*m^2*n*x*x^m*x^{(2*n)}*e^m + 38*B*b*c^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 76*B*a*c*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 76*A*b*c*d*m*n^2*x*x^m*x^{(2*n)}*e^m + 38*A*a*d^2*m*n^2*x*x^m*x^{(2*n)}*e^m + 12*B*b*c^2*n^3*x*x^m*x^{(2*n)}*e^m + 24*B*a*c*d*n^3*x*x^m*x^{(2*n)}*e^m + 24*A*b*c*d*n^3*x*x^m*x^{(2*n)}*e^m + 12*A*a*d^2*n^3*x*x^m*x^{(2*n)}*e^m + 4*B*a*c^2*m^3*x*x^m*x^n$

$$\begin{aligned}
& *e^m + 4*A*b*c^2*m^3*x^m*x^n*e^m + 8*A*a*c*d*m^3*x^m*x^n*e^m + 27*B*a*c \\
& ^2*m^2*n*x^m*x^n*e^m + 27*A*b*c^2*m^2*n*x^m*x^n*e^m + 54*A*a*c*d*m^2*n* \\
& x^m*x^n*e^m + 52*B*a*c^2*m*n^2*x^m*x^n*e^m + 52*A*b*c^2*m*n^2*x^m*x^n \\
& *e^m + 104*A*a*c*d*m*n^2*x^m*x^n*e^m + 24*B*a*c^2*n^3*x^m*x^n*e^m + 24* \\
& A*b*c^2*n^3*x^m*x^n*e^m + 48*A*a*c*d*n^3*x^m*x^n*e^m + 4*A*a*c^2*m^3*x* \\
& x^m*e^m + 30*A*a*c^2*m^2*n*x^m*x^n*e^m + 70*A*a*c^2*m*n^2*x^m*x^n*e^m + 50*A*a* \\
& c^2*n^3*x^m*x^n*e^m + 6*B*b*d^2*m^2*x^m*x^n*(4*n)*e^m + 18*B*b*d^2*m*n*x^m*x \\
& x^n*(4*n)*e^m + 11*B*b*d^2*n^2*x^m*x^n*(4*n)*e^m + 12*B*b*c*d*m^2*x^m*x^n*(3* \\
& n)*e^m + 6*B*a*d^2*m^2*x^m*x^n*(3*n)*e^m + 6*A*b*d^2*m^2*x^m*x^n*(3*n)*e^m \\
& + 42*B*b*c*d*m*n*x^m*x^n*(3*n)*e^m + 21*B*a*d^2*m*n*x^m*x^n*(3*n)*e^m + 21* \\
& A*b*d^2*m*n*x^m*x^n*(3*n)*e^m + 28*B*b*c*d*n^2*x^m*x^n*(3*n)*e^m + 14*B*a*d \\
& ^2*n^2*x^m*x^n*(3*n)*e^m + 14*A*b*d^2*n^2*x^m*x^n*(3*n)*e^m + 6*B*b*c^2*m^2 \\
& *x^m*x^n*(2*n)*e^m + 12*B*a*c*d*m^2*x^m*x^n*(2*n)*e^m + 12*A*b*c*d*m^2*x^m*x \\
& x^n*(2*n)*e^m + 6*A*a*d^2*m^2*x^m*x^n*(2*n)*e^m + 24*B*b*c^2*m*n*x^m*x^n*(2 \\
& *n)*e^m + 48*B*a*c*d*m*n*x^m*x^n*(2*n)*e^m + 48*A*b*c*d*m*n*x^m*x^n*(2*n)*e \\
& ^m + 24*A*a*d^2*m*n*x^m*x^n*(2*n)*e^m + 19*B*b*c^2*n^2*x^m*x^n*(2*n)*e^m + \\
& 38*B*a*c*d*n^2*x^m*x^n*(2*n)*e^m + 38*A*b*c*d*n^2*x^m*x^n*(2*n)*e^m + 19*A* \\
& a*d^2*n^2*x^m*x^n*(2*n)*e^m + 6*B*a*c^2*m^2*x^m*x^n*e^m + 6*A*b*c^2*m^2*x \\
& ^m*x^n*e^m + 12*A*a*c*d*m^2*x^m*x^n*e^m + 27*B*a*c^2*m*n*x^m*x^n*e^m \\
& + 27*A*b*c^2*m*n*x^m*x^n*e^m + 54*A*a*c*d*m*n*x^m*x^n*e^m + 26*B*a*c^2*n \\
& ^2*x^m*x^n*e^m + 26*A*b*c^2*n^2*x^m*x^n*e^m + 52*A*a*c*d*n^2*x^m*x^n \\
& *e^m + 6*A*a*c^2*m^2*x^m*x^n*e^m + 30*A*a*c^2*m*n*x^m*x^n*e^m + 35*A*a*c^2*n^2* \\
& x^m*x^n*e^m + 4*B*b*d^2*m*x^m*x^n*(4*n)*e^m + 6*B*b*d^2*n*x^m*x^n*(4*n)*e^m + \\
& 8*B*b*c*d*m*x^m*x^n*(3*n)*e^m + 4*B*a*d^2*m*x^m*x^n*(3*n)*e^m + 4*A*b*d^2* \\
& m*x^m*x^n*(3*n)*e^m + 14*B*b*c*d*n*x^m*x^n*(3*n)*e^m + 7*B*a*d^2*n*x^m*x^n*( \\
& 3*n)*e^m + 7*A*b*d^2*n*x^m*x^n*(3*n)*e^m + 4*B*b*c^2*m*x^m*x^n*(2*n)*e^m + \\
& 8*B*a*c*d*m*x^m*x^n*(2*n)*e^m + 8*A*b*c*d*m*x^m*x^n*(2*n)*e^m + 4*A*a*d^2* \\
& m*x^m*x^n*(2*n)*e^m + 8*B*b*c^2*n*x^m*x^n*(2*n)*e^m + 16*B*a*c*d*n*x^m*x^n \\
& (2*n)*e^m + 16*A*b*c*d*n*x^m*x^n*(2*n)*e^m + 8*...
\end{aligned}$$

**Mupad [B]**

time = 5.20, size = 588, normalized size = 3.68

---

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)*(c + d*x^n)^2, x)$

[Out]  $(x*x^{(2*n)}*(e*x)^m*(A*a*d^2 + B*b*c^2 + 2*A*b*c*d + 2*B*a*c*d)*(3*m + 8*n + 16*m*n + 19*m*n^2 + 8*m^2*n + 3*m^2 + m^3 + 19*n^2 + 12*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1) + (A*a*c^2*x*(e*x)^m)/(m + 1) + (c*x*x^n*(e*x)^m*(2*A*a*d + A*b*c + B*a*c)*(3*m + 9*n + 18*m*n + 26*m*n^2 + 9*m^2*n + 3*m^2 + m^3 + 26*n^2 + 24*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 +$



$$\begin{aligned}
& 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1) + (d*x*x^{(3*n)}*(e*x)^m*(A*b*d + B*a*d + \\
& 2*B*b*c)*(3*m + 7*n + 14*m*n + 14*m*n^2 + 7*m^2*n + 3*m^2 + m^3 + 14*n^2 + \\
& 8*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3* \\
& n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1) + (B*b \\
& *d^2*x*x^{(4*n)}*(e*x)^m*(3*m + 6*n + 12*m*n + 11*m*n^2 + 6*m^2*n + 3*m^2 + m \\
& ^3 + 11*n^2 + 6*n^3 + 1))/(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m \\
& *n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n \\
& ^2 + 1)
\end{aligned}$$

### 3.11 $\int (ex)^m (A + Bx^n) (c + dx^n)^2 dx$

**Optimal.** Leaf size=102

$$\frac{c(Bc + 2Ad)x^{1+n}(ex)^m}{1 + m + n} + \frac{d(2Bc + Ad)x^{1+2n}(ex)^m}{1 + m + 2n} + \frac{Bd^2x^{1+3n}(ex)^m}{1 + m + 3n} + \frac{Ac^2(ex)^{1+m}}{e(1 + m)}$$

[Out]  $c*(2*A*d+B*c)*x^{(1+n)}*(e*x)^m/(1+m+n)+d*(A*d+2*B*c)*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+B*d^2*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+A*c^2*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.05, antiderivative size = 102, normalized size of antiderivative = 1.00, number of steps used = 8, number of rules used = 3, integrand size = 22,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$ ,

Rules used = {459, 20, 30}

$$\frac{cx^{n+1}(ex)^m(2Ad + Bc)}{m + n + 1} + \frac{dx^{2n+1}(ex)^m(Ad + 2Bc)}{m + 2n + 1} + \frac{Ac^2(ex)^{m+1}}{e(m + 1)} + \frac{Bd^2x^{3n+1}(ex)^m}{m + 3n + 1}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(A + B*x^n)*(c + d*x^n)^2, x]$

[Out]  $(c*(B*c + 2*A*d)*x^{(1 + n)}*(e*x)^m)/(1 + m + n) + (d*(2*B*c + A*d)*x^{(1 + 2*n)}*(e*x)^m)/(1 + m + 2*n) + (B*d^2*x^{(1 + 3*n)}*(e*x)^m)/(1 + m + 3*n) + (A*c^2*(e*x)^{(1 + m)})/(e*(1 + m))$

Rule 20

$\text{Int}[(u_.)*((a_.)*(v_.))^{(m_.)}*((b_.)*(v_.))^{(n_.)}, x\_Symbol] \rightarrow \text{Dist}[b^{\text{IntPart}[n]}*((b*v)^{\text{FracPart}[n]}/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]}), \text{Int}[u*(a*v)^{(m+n)}, x], x] /;$  FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

Rule 30

$\text{Int}[(x_)^{(m_.)}, x\_Symbol] \rightarrow \text{Simp}[x^{(m+1)}/(m+1), x] /;$  FreeQ[m, x] && NeQ[m, -1]

Rule 459

$\text{Int}[((e_.)*(x_.))^{(m_.)}*((a_.) + (b_.)*(x_.)^{(n_.)})^{(p_.)}*((c_.) + (d_.)*(x_.)^{(n_.)})^{(q_.)}, x\_Symbol] \rightarrow \text{Int}[\text{ExpandIntegrand}[(e*x)^m*(a + b*x^n)^p*(c + d*x^n)^q, x], x] /;$  FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && IGtQ[p, 0] && IGtQ[q, 0]

Rubi steps

$$\begin{aligned}
\int (ex)^m (A + Bx^n) (c + dx^n)^2 dx &= \int (Ac^2(ex)^m + c(Bc + 2Ad)x^n(ex)^m + d(2Bc + Ad)x^{2n}(ex)^m + Bd^2x^{3n}(ex)^m) dx \\
&= \frac{Ac^2(ex)^{1+m}}{e(1+m)} + (Bd^2) \int x^{3n}(ex)^m dx + (d(2Bc + Ad)) \int x^{2n}(ex)^m dx \\
&= \frac{Ac^2(ex)^{1+m}}{e(1+m)} + (Bd^2x^{-m}(ex)^m) \int x^{m+3n} dx + (d(2Bc + Ad)x^{-m}(ex)^m) \int x^{m+2n} dx \\
&= \frac{c(Bc + 2Ad)x^{1+n}(ex)^m}{1+m+n} + \frac{d(2Bc + Ad)x^{1+2n}(ex)^m}{1+m+2n} + \frac{Bd^2x^{1+3n}(ex)^m}{1+m+3n}
\end{aligned}$$

**Mathematica [A]**

time = 0.11, size = 78, normalized size = 0.76

$$x(ex)^m \left( \frac{Ac^2}{1+m} + \frac{c(Bc + 2Ad)x^n}{1+m+n} + \frac{d(2Bc + Ad)x^{2n}}{1+m+2n} + \frac{Bd^2x^{3n}}{1+m+3n} \right)$$

Antiderivative was successfully verified.

`[In] Integrate[(e*x)^m*(A + B*x^n)*(c + d*x^n)^2,x]`

```
[Out] x*(e*x)^m*((A*c^2)/(1+m) + (c*(B*c + 2*A*d)*x^n)/(1+m+n) + (d*(2*B*c + A*d)*x^(2*n))/(1+m+2*n) + (B*d^2*x^(3*n))/(1+m+3*n))
```

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.36, size = 732, normalized size = 7.18

method	result
risch	$x(2Acdm^3x^n + 5Bc^2m^2nx^n + 6Bc^2mn^2x^n + 16Bcdmnx^{2n} + 6Bcdm^2x^{2n} + 8Bcdm^2nx^{2n} + 3Ad^2n^2x^{2n} + 3Ad^2x^{2n}m + 4Ad^2x^{2n}n)$

Verification of antiderivative is not currently implemented for this CAS.

`[In] int((e*x)^m*(A+B*x^n)*(c+d*x^n)^2,x,method=_RETURNVERBOSE)`

```
[Out] x*(2*B*c*d*m^3*(x^n)^2+6*B*d^2*m*n*(x^n)^3+2*A*c*d*m^3*x^n+8*A*d^2*m*n*(x^n)^2+5*B*c^2*m^2*n*x^n+6*B*c^2*m*n^2*x^n+3*A*d^2*n^2*(x^n)^2+B*c^2*m^3*x^n+3*A*d^2*(x^n)^2*m+6*A*c^2*m^2*n+11*A*c^2*m*n^2+12*A*c^2*m*n+A*c^2+(x^n)^3*B*d^2+(x^n)^2*A*d^2+4*A*d^2*(x^n)^2+n+3*B*c^2*m^2*x^n+3*m*B*d^2*(x^n)^3+3*B*d^2*(x^n)^3*n+12*A*c*d*m*n^2*x^n+16*B*c*d*m*n*(x^n)^2+6*B*c*d*m*n^2*(x^n)^2+x^n*B*c^2+3*B*c^2*x^n*m+A*c^2*m^3+8*B*c*d*m^2*n*(x^n)^2+B*d^2*m^3*(x^n)^3+3*A*c^2*m+6*A*c^2*n+6*A*c^2*n^3+3*A*c^2*m^2+11*A*c^2*n^2+20*A*c*d*m*n*x^n+10*A*c*d*m^2*n*x^n+2*B*d^2*n^2*(x^n)^3+3*A*d^2*m^2*(x^n)^2+A*d^2*m^3*(x^n)^2+3*B*d^2*m^2*(x^n)^3+6*B*c^2*n^2*x^n+2*B*c*d*(x^n)^2+2*A*c*d*x^n+5*B*c^2*x^n*n+6*A*c*d*x^n*m+6*B*c*d*m^2*(x^n)^2+6*B*c*d*n^2*(x^n)^2+6*A*c*d*m^2*x^n+12
```

$$*A*c*d^n^2*x^n+10*B*c^2*m*n*x^n+10*A*c*d*x^n*n+6*B*c*d*(x^n)^2*m+8*B*c*d*(x^n)^2*n+3*B*d^2*m^2*n*(x^n)^3+2*B*d^2*m*n^2*(x^n)^3+4*A*d^2*m^2*n*(x^n)^2+3*A*d^2*m*n^2*(x^n)^2)/(1+m)/(1+m+n)/(1+m+2*n)/(1+m+3*n)*\exp(1/2*m*(-I*Pi*csgn(I*e*x)^3+I*Pi*csgn(I*e*x)^2*csgn(I*e)+I*Pi*csgn(I*e*x)^2*csgn(I*x)-I*Pi*csgn(I*e*x)*csgn(I*e)*csgn(I*x)+2*\ln(e)+2*\ln(x)))$$

**Maxima [A]**

time = 0.32, size = 145, normalized size = 1.42

$$\frac{(xe)^{m+1}Ac^2e^{(-1)}}{m+1} + \frac{Bd^2xe^{(m\log(x)+3n\log(x)+m)}}{m+3n+1} + \frac{2Bcdxe^{(m\log(x)+2n\log(x)+m)}}{m+2n+1} + \frac{Ad^2xe^{(m\log(x)+2n\log(x)+m)}}{m+2n+1} + \frac{Bc^2xe^{(m\log(x)+n\log(x)+m)}}{m+n+1} + \frac{2Ac dx e^{(m\log(x)+n\log(x)+m)}}{m+n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="maxima")

[Out] (x\*e)^(m + 1)\*A\*c^2\*e^(-1)/(m + 1) + B\*d^2\*x\*e^(m\*log(x) + 3\*n\*log(x) + m)/(m + 3\*n + 1) + 2\*B\*c\*d\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + A\*d^2\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + B\*c^2\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1) + 2\*A\*c\*d\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1)

**Fricas [B]** Leaf count of result is larger than twice the leaf count of optimal. 515 vs. 2(105) = 210.

time = 3.53, size = 515, normalized size = 5.05

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2,x, algorithm="fricas")

[Out] ((B\*d^2\*m^3 + 3\*B\*d^2\*m^2 + 3\*B\*d^2\*m + B\*d^2 + 2\*(B\*d^2\*m + B\*d^2)\*n^2 + 3\*(B\*d^2\*m^2 + 2\*B\*d^2\*m + B\*d^2)\*n)\*x\*x^(3\*n)\*e^(m\*log(x) + m) + ((2\*B\*c\*d + A\*d^2)\*m^3 + 2\*B\*c\*d + A\*d^2 + 3\*(2\*B\*c\*d + A\*d^2)\*m^2 + 3\*(2\*B\*c\*d + A\*d^2 + (2\*B\*c\*d + A\*d^2)\*m)\*n^2 + 3\*(2\*B\*c\*d + A\*d^2)\*m + 4\*(2\*B\*c\*d + A\*d^2 + (2\*B\*c\*d + A\*d^2)\*m^2 + 2\*(2\*B\*c\*d + A\*d^2)\*m)\*n)\*x\*x^(2\*n)\*e^(m\*log(x) + m) + ((B\*c^2 + 2\*A\*c\*d)\*m^3 + B\*c^2 + 2\*A\*c\*d + 3\*(B\*c^2 + 2\*A\*c\*d)\*m^2 + 6\*(B\*c^2 + 2\*A\*c\*d + (B\*c^2 + 2\*A\*c\*d)\*m)\*n^2 + 3\*(B\*c^2 + 2\*A\*c\*d)\*m + 5\*(B\*c^2 + 2\*A\*c\*d + (B\*c^2 + 2\*A\*c\*d)\*m^2 + 2\*(B\*c^2 + 2\*A\*c\*d)\*m)\*n)\*x\*x^n\*e^(m\*log(x) + m) + (A\*c^2\*m^3 + 6\*A\*c^2\*n^3 + 3\*A\*c^2\*m^2 + 3\*A\*c^2\*m + A\*c^2 + 11\*(A\*c^2\*m + A\*c^2)\*n^2 + 6\*(A\*c^2\*m^2 + 2\*A\*c^2\*m + A\*c^2)\*n)\*x\*e^(m\*log(x) + m))/(m^4 + 6\*(m + 1)\*n^3 + 4\*m^3 + 11\*(m^2 + 2\*m + 1)\*n^2 + 6\*m^2 + 6\*(m^3 + 3\*m^2 + 3\*m + 1)\*n + 4\*m + 1)

**Sympy [B]** Leaf count of result is larger than twice the leaf count of optimal. 5794 vs. 2(94) = 188.

time = 35.26, size = 5794, normalized size = 56.80

Too large to display





```

*m^2*x*x^m*x^(2*n)*e^m + 3*A*d^2*m^2*x*x^m*x^(2*n)*e^m + 16*B*c*d*m*n*x*x^m
*x^(2*n)*e^m + 8*A*d^2*m*n*x*x^m*x^(2*n)*e^m + 6*B*c*d*n^2*x*x^m*x^(2*n)*e^
m + 3*A*d^2*n^2*x*x^m*x^(2*n)*e^m + 3*B*c^2*m^2*x*x^m*x^n*e^m + 6*A*c*d*m^2
*x*x^m*x^n*e^m + 10*B*c^2*m*n*x*x^m*x^n*e^m + 20*A*c*d*m*n*x*x^m*x^n*e^m +
6*B*c^2*n^2*x*x^m*x^n*e^m + 12*A*c*d*n^2*x*x^m*x^n*e^m + 3*A*c^2*m^2*x*x^m*
e^m + 12*A*c^2*m*n*x*x^m*e^m + 11*A*c^2*n^2*x*x^m*e^m + 3*B*d^2*m*x*x^m*x^(
3*n)*e^m + 3*B*d^2*n*x*x^m*x^(3*n)*e^m + 6*B*c*d*m*x*x^m*x^(2*n)*e^m + 3*A*
d^2*m*x*x^m*x^(2*n)*e^m + 8*B*c*d*n*x*x^m*x^(2*n)*e^m + 4*A*d^2*n*x*x^m*x^(
2*n)*e^m + 3*B*c^2*m*x*x^m*x^n*e^m + 6*A*c*d*m*x*x^m*x^n*e^m + 5*B*c^2*n*x*
x^m*x^n*e^m + 10*A*c*d*n*x*x^m*x^n*e^m + 3*A*c^2*m*x*x^m*e^m + 6*A*c^2*n*x*
x^m*e^m + B*d^2*x*x^m*x^(3*n)*e^m + 2*B*c*d*x*x^m*x^(2*n)*e^m + A*d^2*x*x^m
*x^(2*n)*e^m + B*c^2*x*x^m*x^n*e^m + 2*A*c*d*x*x^m*x^n*e^m + A*c^2*x*x^m*e^
m)/(m^4 + 6*m^3*n + 11*m^2*n^2 + 6*m*n^3 + 4*m^3 + 18*m^2*n + 22*m*n^2 + 6*
n^3 + 6*m^2 + 18*m*n + 11*n^2 + 4*m + 6*n + 1)

```

**Mupad [B]**

time = 5.11, size = 265, normalized size = 2.60

$$\frac{A^2 x (ex)^m}{m+1} + \frac{c x x^n (ex)^m (2Ad+Bc) (m^2+5mn+2m+6n^2+5n+1)}{m^3+6m^2n+3m^2+11mn^2+12mn+3m+6n^3+11n^2+6n+1} + \frac{d x x^{2n} (ex)^m (Ad+2Bc) (m^2+4mn+2m+3n^2+4n+1)}{m^3+6m^2n+3m^2+11mn^2+12mn+3m+6n^3+11n^2+6n+1} + \frac{B d^2 x x^{3n} (ex)^m (m^2+3mn+2m+2n^2+3n+1)}{m^3+6m^2n+3m^2+11mn^2+12mn+3m+6n^3+11n^2+6n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((ex)^m \cdot (A + B \cdot x^n) \cdot (c + d \cdot x^n)^2, x)$

[Out]  $(A \cdot c^2 \cdot x \cdot (ex)^m) / (m + 1) + (c \cdot x \cdot x^n \cdot (ex)^m \cdot (2 \cdot A \cdot d + B \cdot c) \cdot (2 \cdot m + 5 \cdot n + 5 \cdot m \cdot n + m^2 + 6 \cdot n^2 + 1)) / (3 \cdot m + 6 \cdot n + 12 \cdot m \cdot n + 11 \cdot m \cdot n^2 + 6 \cdot m^2 \cdot n + 3 \cdot m^2 + m^3 + 11 \cdot n^2 + 6 \cdot n^3 + 1) + (d \cdot x \cdot x^{2n} \cdot (ex)^m \cdot (A \cdot d + 2 \cdot B \cdot c) \cdot (2 \cdot m + 4 \cdot n + 4 \cdot m \cdot n + m^2 + 3 \cdot n^2 + 1)) / (3 \cdot m + 6 \cdot n + 12 \cdot m \cdot n + 11 \cdot m \cdot n^2 + 6 \cdot m^2 \cdot n + 3 \cdot m^2 + m^3 + 11 \cdot n^2 + 6 \cdot n^3 + 1) + (B \cdot d^2 \cdot x \cdot x^{3n} \cdot (ex)^m \cdot (2 \cdot m + 3 \cdot n + 3 \cdot m \cdot n + m^2 + 2 \cdot n^2 + 1)) / (3 \cdot m + 6 \cdot n + 12 \cdot m \cdot n + 11 \cdot m \cdot n^2 + 6 \cdot m^2 \cdot n + 3 \cdot m^2 + m^3 + 11 \cdot n^2 + 6 \cdot n^3 + 1)$

$$3.12 \quad \int \frac{(ex)^m (A+Bx^n)(c+dx^n)^2}{a+bx^n} dx$$

**Optimal.** Leaf size=185

$$\frac{d(2bBc + Abd - aBd)x^{1+n}(ex)^m}{b^2(1+m+n)} + \frac{Bd^2x^{1+2n}(ex)^m}{b(1+m+2n)} + \frac{(a^2Bd^2 - abd(2Bc + Ad) + b^2c(Bc + 2Ad))(ex)^{1+m}}{b^3e(1+m)} + \dots$$

[Out] d\*(A\*b\*d-B\*a\*d+2\*B\*b\*c)\*x^(1+n)\*(e\*x)^m/b^2/(1+m+n)+B\*d^2\*x^(1+2\*n)\*(e\*x)^m/b/(1+m+2\*n)+(a^2\*B\*d^2-a\*b\*d\*(A\*d+2\*B\*c)+b^2\*c\*(2\*A\*d+B\*c))\*(e\*x)^(1+m)/b^3/e/(1+m)+(A\*b-B\*a)\*(-a\*d+b\*c)^2\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b\*x^n/a)/a/b^3/e/(1+m)

**Rubi [A]**

time = 0.15, antiderivative size = 185, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.129$ , Rules used = {584, 20, 30, 371}

$$\frac{(ex)^{m+1}(a^2Bd^2 - abd(Ad + 2Bc) + b^2c(2Ad + Bc))}{b^3e(m+1)} + \frac{(ex)^{m+1}(Ab - aB)(bc - ad)^2 {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{bx^n}{a}\right)}{ab^3e(m+1)} + \frac{dx^{n+1}(ex)^m(-aBd + Abd + 2bBc)}{b^2(m+n+1)} + \frac{Bd^2x^{2n+1}(ex)^m}{b(m+2n+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n), x]

[Out] (d\*(2\*b\*B\*c + A\*b\*d - a\*B\*d)\*x^(1 + n)\*(e\*x)^m)/(b^2\*(1 + m + n)) + (B\*d^2\*x^(1 + 2\*n)\*(e\*x)^m)/(b\*(1 + m + 2\*n)) + ((a^2\*B\*d^2 - a\*b\*d\*(2\*B\*c + A\*d) + b^2\*c\*(B\*c + 2\*A\*d))\*(e\*x)^(1 + m))/(b^3\*e\*(1 + m)) + ((A\*b - a\*B)\*(b\*c - a\*d)^2\*(e\*x)^(1 + m)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(b\*x^n)/a])/(a\*b^3\*e\*(1 + m))

**Rule 20**

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_.)\*((b\_.)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

**Rule 30**

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

**Rule 371**

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])



Rule 584

```
Int[((g_)*(x_))^(m_)*((a_) + (b_)*(x_)^(n_))^(p_)*((c_) + (d_)*(x_)^(n_))^(q_)*((e_) + (f_)*(x_)^(n_))^(r_), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)(c + dx^n)^2}{a + bx^n} dx &= \int \left( \frac{(a^2Bd^2 - abd(2Bc + Ad) + b^2c(Bc + 2Ad))(ex)^m}{b^3} + \frac{d(2bBc + Ad)}{b^3} \right) dx \\ &= \frac{(a^2Bd^2 - abd(2Bc + Ad) + b^2c(Bc + 2Ad))(ex)^{1+m}}{b^3e(1+m)} + \frac{(Bd^2) \int x^{2n}(ex)^m dx}{b} \\ &= \frac{(a^2Bd^2 - abd(2Bc + Ad) + b^2c(Bc + 2Ad))(ex)^{1+m}}{b^3e(1+m)} + \frac{(Ab - aB)(bc - ad)^2}{b^3(1+m)} \\ &= \frac{d(2bBc + Abd - aBd)x^{1+n}(ex)^m}{b^2(1+m+n)} + \frac{Bd^2x^{1+2n}(ex)^m}{b(1+m+2n)} + \frac{(a^2Bd^2 - abd(2Bc + Ad) + b^2c(Bc + 2Ad))(ex)^{1+m}}{b^3e(1+m)} \end{aligned}$$

Mathematica [A]

time = 0.32, size = 156, normalized size = 0.84

$$x(ex)^m \left( \frac{(-Ab + aB)(bc - ad)^2}{ab^3(1+m)} + \frac{Ac^2}{a+am} + \frac{d(2bBc + Abd - aBd)x^n}{b^2(1+m+n)} + \frac{Bd^2x^{2n}}{b+bm+2bn} + \frac{(Ab - aB)(bc - ad)^2 {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{ab^3(1+m)} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(A + B*x^n)*(c + d*x^n)^2)/(a + b*x^n), x]
```

```
[Out] x*(e*x)^m*(((-(A*b) + a*B)*(b*c - a*d)^2)/(a*b^3*(1 + m)) + (A*c^2)/(a + a*m) + (d*(2*b*B*c + A*b*d - a*B*d)*x^n)/(b^2*(1 + m + n)) + (B*d^2*x^(2*n))/(b + b*m + 2*b*n) + ((A*b - a*B)*(b*c - a*d)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(b*x^n)/a]))/(a*b^3*(1 + m))
```

Maple [F]

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)(c + dx^n)^2}{a + bx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(A+B*x^n)*(c+d*x^n)^2/(a+b*x^n), x)
```

```
[Out] int((e*x)^m*(A+B*x^n)*(c+d*x^n)^2/(a+b*x^n), x)
```

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^2/(a+b*x^n),x, algorithm="maxima")
```

```
[Out] ((b^3*c^2*e^m - 2*a*b^2*c*d*e^m + a^2*b*d^2*e^m)*A - (a*b^2*c^2*e^m - 2*a^2
*b*c*d*e^m + a^3*d^2*e^m)*B)*integrate(x^m/(b^4*x^n + a*b^3), x) + ((m^2*e^
m + m*(n + 2)*e^m + (n + 1)*e^m)*B*b^2*d^2*x*e^(m*log(x) + 2*n*log(x)) + ((
2*(m^2*e^m + m*(3*n + 2)*e^m + (2*n^2 + 3*n + 1)*e^m)*b^2*c*d - (m^2*e^m +
m*(3*n + 2)*e^m + (2*n^2 + 3*n + 1)*e^m)*a*b*d^2)*A + ((m^2*e^m + m*(3*n +
2)*e^m + (2*n^2 + 3*n + 1)*e^m)*b^2*c^2 - 2*(m^2*e^m + m*(3*n + 2)*e^m + (2
*n^2 + 3*n + 1)*e^m)*a*b*c*d + (m^2*e^m + m*(3*n + 2)*e^m + (2*n^2 + 3*n +
1)*e^m)*a^2*d^2)*B)*x*x^m + ((m^2*e^m + 2*m*(n + 1)*e^m + (2*n + 1)*e^m)*A*
b^2*d^2 + (2*(m^2*e^m + 2*m*(n + 1)*e^m + (2*n + 1)*e^m)*b^2*c*d - (m^2*e^m
+ 2*m*(n + 1)*e^m + (2*n + 1)*e^m)*a*b*d^2)*B)*x*e^(m*log(x) + n*log(x))/
((m^3 + 3*m^2*(n + 1) + (2*n^2 + 6*n + 3)*m + 2*n^2 + 3*n + 1)*b^3)
```

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^2/(a+b*x^n),x, algorithm="fricas")
```

```
[Out] integral((B*d^2*x^(3*n) + A*c^2 + (2*B*c*d + A*d^2)*x^(2*n) + (B*c^2 + 2*A*
c*d)*x^n)*(x*e)^m/(b*x^n + a), x)
```

**Sympy [C]** Result contains complex when optimal does not.

time = 11.79, size = 1085, normalized size = 5.86

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(A+B*x**n)*(c+d*x**n)**2/(a+b*x**n),x)
```

```
[Out] A*c**2*e**m*m*x*x**m*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1/n)*gamma
(m/n + 1/n)/(a*n**2*gamma(m/n + 1 + 1/n)) + A*c**2*e**m*m*x*x**m*lerchphi(b*x
**n*exp_polar(I*pi)/a, 1, m/n + 1/n)*gamma(m/n + 1/n)/(a*n**2*gamma(m/n + 1
+ 1/n)) + 2*A*c*d*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1,
m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + 2*A*c*
d*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gam
```

```

ma(m/n + 1 + 1/n)/(a*n*gamma(m/n + 2 + 1/n)) + 2*A*c*d*e**m*x*x**m*x**n*ler
chphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n
**2*gamma(m/n + 2 + 1/n)) + A*d**2*e**m*m*x*x**m*x**n*(2*n)*lerchphi(b*x**n*e
xp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n**2*gamma(m/n
+ 3 + 1/n)) + 2*A*d**2*e**m*x*x**m*x**n*(2*n)*lerchphi(b*x**n*exp_polar(I*pi)
/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n*gamma(m/n + 3 + 1/n)) + A*d
**2*e**m*x*x**m*x**n*(2*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/
n)*gamma(m/n + 2 + 1/n)/(a*n**2*gamma(m/n + 3 + 1/n)) + B*c**2*e**m*m*x*x**
m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 +
1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + B*c**2*e**m*x*x**m*x**n*lerchphi(b*x*
**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n*gamma(m/n
+ 2 + 1/n)) + B*c**2*e**m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1
, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + 2*B*c
*d*e**m*m*x*x**m*x**n*(2*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1
/n)*gamma(m/n + 2 + 1/n)/(a*n**2*gamma(m/n + 3 + 1/n)) + 4*B*c*d*e**m*x*x**
m*x**n*(2*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n +
2 + 1/n)/(a*n*gamma(m/n + 3 + 1/n)) + 2*B*c*d*e**m*x*x**m*x**n*(2*n)*lerchph
i(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n**2*
gamma(m/n + 3 + 1/n)) + B*d**2*e**m*m*x*x**m*x**n*(3*n)*lerchphi(b*x**n*exp_p
olar(I*pi)/a, 1, m/n + 3 + 1/n)*gamma(m/n + 3 + 1/n)/(a*n**2*gamma(m/n + 4
+ 1/n)) + 3*B*d**2*e**m*x*x**m*x**n*(3*n)*lerchphi(b*x**n*exp_polar(I*pi)/a,
1, m/n + 3 + 1/n)*gamma(m/n + 3 + 1/n)/(a*n*gamma(m/n + 4 + 1/n)) + B*d**2*
e**m*x*x**m*x**n*(3*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 3 + 1/n)*g
amma(m/n + 3 + 1/n)/(a*n**2*gamma(m/n + 4 + 1/n))

```

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(d\*x^n + c)^2\*(x\*e)^m/(b\*x^n + a), x)

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)^2}{a + bx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n), x)

$$3.13 \quad \int \frac{(ex)^m (A+Bx^n)(c+dx^n)^2}{(a+bx^n)^2} dx$$

**Optimal.** Leaf size=268

$$\frac{d^2(Ab(1+m+n) - aB(1+m+2n))x^{1+n}(ex)^m}{ab^2n(1+m+n)} - \frac{d(Ab(2bc(1+m) - ad(1+m+n)) - aB(2bc(1+m) + ab^3e(1+m)n))}{ab^3e(1+m)n}$$

[Out]  $-d^2(A*b*(1+m+n)-a*B*(1+m+2*n))*x^{(1+n)}*(e*x)^m/a/b^2/n/(1+m+n)-d*(A*b*(2*b*c*(1+m)-a*d*(1+m+n))-a*B*(2*b*c*(1+m+n)-a*d*(1+m+2*n)))*(e*x)^{(1+m)}/a/b^3/e/(1+m)/n+(A*b-B*a)*(e*x)^{(1+m)}*(c+d*x^n)^2/a/b/e/n/(a+b*x^n)-(-a*d+b*c)*(A*b*(b*c*(1+m-n)-a*d*(1+m+n))-a*B*(b*c*(1+m)-a*d*(1+m+2*n)))*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/a^2/b^3/e/(1+m)/n$

**Rubi [A]**

time = 0.45, antiderivative size = 268, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.161$ , Rules used = {608, 584, 20, 30, 371}

$$\frac{(ex)^{m+1}(bc-ad)_2F_1\left(1, \frac{m+1}{n}; \frac{m+1+n}{n}, -\frac{bc}{a}\right) (Ab(bc(m-n+1)-ad(m+n+1))-aB(bc(m+1)-ad(m+2n+1)))}{a^2b^2e(m+1)n} - \frac{d(ex)^{m+1}(Ab(2bc(m+1)-ad(m+n+1))-aB(2bc(m+n+1)-ad(m+2n+1)))}{ab^2e(m+1)n} - \frac{d^2x^{m+1}(ex)^m(Ab(m+n+1)-aB(m+2n+1))}{ab^3e(m+n+1)} + \frac{(ex)^{m+1}(Ab-aB)(c+dx^n)^2}{abn(a+bx^n)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n)^2,x]

[Out]  $-((d^2(A*b*(1+m+n) - a*B*(1+m+2*n))*x^{(1+n)}*(e*x)^m)/(a*b^2*n*(1+m+n)) - (d*(A*b*(2*b*c*(1+m) - a*d*(1+m+n)) - a*B*(2*b*c*(1+m+n) - a*d*(1+m+2*n)))*(e*x)^{(1+m)}/(a*b^3*e*(1+m)*n) + ((A*b - a*B)*(e*x)^{(1+m)}*(c + d*x^n)^2)/(a*b*e*n*(a + b*x^n)) - ((b*c - a*d)*(A*b*(b*c*(1+m-n) - a*d*(1+m+n)) - a*B*(b*c*(1+m) - a*d*(1+m+2*n)))*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((b*x^n)/a)])/ (a^2*b^3*e*(1+m)*n)$

Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

Rule 30

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 371

```
Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[a^p
*((c*x)^(m + 1)/(c*(m + 1))]*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1
, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILt
Q[p, 0] || GtQ[a, 0])
```

### Rule 584

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n
_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[
(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c
, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

### Rule 608

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n
_))^(q_.)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(
m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^q/(a*b*g*n*(p + 1))), x] + Dist[1/(
a*b*n*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^(q - 1)*Simp[c*
(b*e*n*(p + 1) + (b*e - a*f)*(m + 1)) + d*(b*e*n*(p + 1) + (b*e - a*f)*(m +
n*q + 1))*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[
p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b*c - a*d, b*e - a*f])
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n) (c + dx^n)^2}{(a + bx^n)^2} dx &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)^2}{aben (a + bx^n)} - \int \frac{(ex)^m (c + dx^n) (-c(aB(1+m) - Ab(1+m-n)) + a + bx^n)}{abn} \\ &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)^2}{aben (a + bx^n)} - \int \frac{d(Ab(2bc(1+m) - ad(1+m+n)) - aB(2bc(1+m+n) - ad(1+m+n)))}{b^2} \\ &= \frac{d(Ab(2bc(1+m) - ad(1+m+n)) - aB(2bc(1+m+n) - ad(1+m+n)))}{ab^3e(1+m)n} \\ &= \frac{d(Ab(2bc(1+m) - ad(1+m+n)) - aB(2bc(1+m+n) - ad(1+m+n)))}{ab^3e(1+m)n} \\ &= \frac{d^2(Ab(1+m+n) - aB(1+m+2n))x^{1+n}(ex)^m}{ab^2n(1+m+n)} - \frac{d(Ab(2bc(1+m+n) - ad(1+m+n)))}{ab^2n(1+m+n)} \end{aligned}$$

### Mathematica [A]

time = 0.87, size = 227, normalized size = 0.85

$$\frac{x(ex)^m \left( \frac{b^2 c(Ab - aB - 2aAd)}{an(a + bx^n)} + aBd^2 \left( -\frac{2}{1+m} - \frac{a}{an + bnx^n} \right) + bd \left( Ad \left( \frac{1}{1+m} + \frac{a}{an + bnx^n} \right) + B \left( \frac{dx^n}{1+m+n} + 2c \left( \frac{1}{1+m} + \frac{a}{an + bnx^n} \right) \right) \right) + \frac{(-bc+ad)(Ab(bc(1+m-n)-ad(1+m+n))+aB(-bc(1+m)+ad(1+m+2n)))_2F1\left(1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{bx^n}{a}\right)}{a^2(1+m)n}}{b^3}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n)^2,x]

[Out] (x\*(e\*x)^m\*((b^2\*c\*(A\*b\*c - a\*B\*c - 2\*a\*A\*d))/(a\*n\*(a + b\*x^n)) + a\*B\*d^2\*(-2/(1 + m) - a/(a\*n + b\*n\*x^n)) + b\*d\*(A\*d\*((1 + m)^(-1) + a/(a\*n + b\*n\*x^n))) + B\*((d\*x^n)/(1 + m + n) + 2\*c\*((1 + m)^(-1) + a/(a\*n + b\*n\*x^n)))) + ((-(b\*c) + a\*d)\*(A\*b\*(b\*c\*(1 + m - n) - a\*d\*(1 + m + n)) + a\*B\*(-(b\*c\*(1 + m) + a\*d\*(1 + m + 2\*n)))\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(b\*x^n)/a]))/(a^2\*(1 + m)\*n))/b^3

**Maple [F]**

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)(c + dx^n)^2}{(a + bx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^2,x)

[Out] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^2,x, algorithm="maxima")

[Out] -(((m\*e^m - (n - 1)\*e^m)\*b^3\*c^2 - 2\*(m\*e^m + e^m)\*a\*b^2\*c\*d + (m\*e^m + (n + 1)\*e^m)\*a^2\*b\*d^2)\*A - ((m\*e^m + e^m)\*a\*b^2\*c^2 - 2\*(m\*e^m + (n + 1)\*e^m)\*a^2\*b\*c\*d + (m\*e^m + (2\*n + 1)\*e^m)\*a^3\*d^2)\*B)\*integrate(x^m/(a\*b^4\*n\*x^n + a^2\*b^3\*n), x) + ((m\*n\*e^m + n\*e^m)\*B\*a\*b^2\*d^2\*x\*e^(m\*log(x) + 2\*n\*log(x)) + (((m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*b^3\*c^2 - 2\*(m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a\*b^2\*c\*d + (m^2\*e^m + 2\*m\*(n + 1)\*e^m + (n^2 + 2\*n + 1)\*e^m)\*a^2\*b\*d^2)\*A - ((m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a\*b^2\*c^2 - 2\*(m^2\*e^m + 2\*m\*(n + 1)\*e^m + (n^2 + 2\*n + 1)\*e^m)\*a^2\*b\*c\*d + (m^2\*e^m + m\*(3\*n + 2)\*e^m + (2\*n^2 + 3\*n + 1)\*e^m)\*a^3\*d^2)\*B)\*x\*x^m + ((m\*n\*e^m + (n^2 + n)\*e^m)\*A\*a\*b^2\*d^2 + (2\*(m\*n\*e^m + (n^2 + n)\*e^m)\*a\*b^2\*c\*d - (m\*n\*e^m + (2\*n^2 + n)\*e^m)\*a^2\*b\*d^2)\*B)\*x\*x^m + ((m^2\*n + (n^2 + 2\*n)\*m + n^2 + n)\*a\*b^4\*x^n + (m^2\*n + (n^2 + 2\*n)\*m + n^2 + n)\*a^2\*b^3)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^2,x, algorithm="fricas")

[Out] integral((B\*d^2\*x^(3\*n) + A\*c^2 + (2\*B\*c\*d + A\*d^2)\*x^(2\*n) + (B\*c^2 + 2\*A\*c\*d)\*x^n)\*(x\*e)^m/(b^2\*x^(2\*n) + 2\*a\*b\*x^n + a^2), x)

**Sympy [F]**

time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)^2}{(a + bx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*2/(a+b\*x\*\*n)\*\*2,x)

[Out] Integral((e\*x)\*\*m\*(A + B\*x\*\*n)\*(c + d\*x\*\*n)\*\*2/(a + b\*x\*\*n)\*\*2, x)

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^2,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(d\*x^n + c)^2\*(x\*e)^m/(b\*x^n + a)^2, x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)^2}{(a + bx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n)^2,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n)^2, x)

$$3.14 \quad \int \frac{(ex)^m (A+Bx^n)(c+dx^n)^2}{(a+bx^n)^3} dx$$

**Optimal.** Leaf size=322

$$\frac{d(bc(1+m) - ad(1+m+n))(Ab(1+m) - aB(1+m+2n))(ex)^{1+m}}{2a^2b^3e(1+m)n^2} + \frac{(Ab - aB)(ex)^{1+m}(c+dx^n)^2}{2abene(a+bx^n)^2} + \frac{bc}{e}$$

[Out] 1/2\*d\*(b\*c\*(1+m)-a\*d\*(1+m+n))\*(A\*b\*(1+m)-a\*B\*(1+m+2\*n))\*(e\*x)^(1+m)/a^2/b^3  
/e/(1+m)/n^2+1/2\*(A\*b-B\*a)\*(e\*x)^(1+m)\*(c+d\*x^n)^2/a/b/e/n/(a+b\*x^n)^2+1/2\*  
(-a\*d+b\*c)\*(e\*x)^(1+m)\*(c\*(a\*B\*(1+m)-A\*b\*(1+m-2\*n))-d\*(A\*b\*(1+m)-a\*B\*(1+m+2  
\*n))\*x^n/a^2/b^2/e/n^2/(a+b\*x^n)+1/2\*(b\*c\*(a\*B\*(1+m)-A\*b\*(1+m-2\*n))\*(a\*d\*(  
1+m)-b\*c\*(1+m-n))-a\*d\*(b\*c\*(1+m)-a\*d\*(1+m+n))\*(A\*b\*(1+m)-a\*B\*(1+m+2\*n))\*(e  
\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b\*x^n/a)/a^3/b^3/e/(1+m)/n^2

**Rubi [A]**

time = 0.36, antiderivative size = 322, normalized size of antiderivative = 1.00, number of  
steps used = 4, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ ,  
Rules used = {608, 470, 371}

$(ex)^{m+1} F_1\left(1, \frac{m+1}{n}; \frac{m+1}{n}; -\frac{bx^n}{a}\right) (bc(aB(m+1) - Ab(m-2n+1))(ad(m+1) - bc(m-n+1)) - ad(Ab(m+1) - aB(m+2n+1))(b(m+1) - ad(m+n+1)))$  ;  $\frac{d(ex)^{m+1}(Ab(m+1) - aB(m+2n+1))(bc(m+1) - ad(m+n+1))}{2a^2b^3e(m+1)n^2}$  ;  $(ex)^{m+1}(bc - ad)(c(aB(m+1) - Ab(m-2n+1)) - d(Ab(m+1) - aB(m+2n+1)))$  ;  $\frac{(ex)^{m+1}(Ab - aB)(c+dx^n)^2}{2abene(a+bx^n)^2}$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n)^3,x]

[Out] (d\*(b\*c\*(1+m) - a\*d\*(1+m+n))\*(A\*b\*(1+m) - a\*B\*(1+m+2\*n))\*(e\*x)^(1+m))/(2\*a^2\*b^3\*e\*(1+m)\*n^2) + ((A\*b - a\*B)\*(e\*x)^(1+m)\*(c + d\*x^n)^2)/(2\*a\*b\*e\*n\*(a + b\*x^n)^2) + ((b\*c - a\*d)\*(e\*x)^(1+m)\*(c\*(a\*B\*(1+m) - A\*b\*(1+m-2\*n)) - d\*(A\*b\*(1+m) - a\*B\*(1+m+2\*n))\*x^n))/(2\*a^2\*b^2\*e\*n^2\*(a + b\*x^n)) + ((b\*c\*(a\*B\*(1+m) - A\*b\*(1+m-2\*n))\*(a\*d\*(1+m) - b\*c\*(1+m-n)) - a\*d\*(b\*c\*(1+m) - a\*d\*(1+m+n))\*(A\*b\*(1+m) - a\*B\*(1+m+2\*n)))\*(e\*x)^(1+m)\*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((b\*x^n)/a)]/(2\*a^3\*b^3\*e\*(1+m)\*n^2)

**Rule 371**

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

**Rule 470**

Int[((e\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_)), x\_Symbol] :> Simp[d\*(e\*x)^(m+1)\*((a + b\*x^n)^(p+1)/(b\*e\*(m+n\*(p+1)+1))), x] - Dist[(a\*d\*(m+1) - b\*c\*(m+n\*(p+1)+1))/(b\*(m+n\*(p+1)+1)), x]



+ 1) + 1)), Int[(e\*x)^m\*(a + b\*x^n)^p, x], x] /; FreeQ[{a, b, c, d, e, m, n, p}, x] && NeQ[b\*c - a\*d, 0] && NeQ[m + n\*(p + 1) + 1, 0]

### Rule 608

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_.) + (b\_.)\*(x\_)^(n\_))^(p\_)\*((c\_.) + (d\_.)\*(x\_)^(n\_))^(q\_.)\*((e\_.) + (f\_.)\*(x\_)^(n\_)), x\_Symbol] :> Simp[(-b\*e - a\*f)\*(g\*x)^(m + 1)\*(a + b\*x^n)^(p + 1)\*((c + d\*x^n)^q/(a\*b\*g\*n\*(p + 1))), x] + Dist[1/(a\*b\*n\*(p + 1)), Int[(g\*x)^m\*(a + b\*x^n)^(p + 1)\*(c + d\*x^n)^(q - 1)\*Simp[c\*(b\*e\*n\*(p + 1) + (b\*e - a\*f)\*(m + 1)) + d\*(b\*e\*n\*(p + 1) + (b\*e - a\*f)\*(m + n\*q + 1))\*x^n, x], x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b\*c - a\*d, b\*e - a\*f])

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n) (c + dx^n)^2}{(a + bx^n)^3} dx &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)^2}{2abn (a + bx^n)^2} - \frac{\int \frac{(ex)^m (c+dx^n)(-c(aB(1+m)-Ab(1+m-2n))+ (a+bx^n)^2)}{2abn} dx}{2abn} \\ &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)^2}{2abn (a + bx^n)^2} + \frac{(bc - ad)(ex)^{1+m} (c(aB(1+m) - Ab(1+m-2n)))}{2a^2b^3e(1+m)n^2} \\ &= \frac{d(bc(1+m) - ad(1+m+n))(Ab(1+m) - aB(1+m+2n))(ex)^{1+m}}{2a^2b^3e(1+m)n^2} \\ &= \frac{d(bc(1+m) - ad(1+m+n))(Ab(1+m) - aB(1+m+2n))(ex)^{1+m}}{2a^2b^3e(1+m)n^2} \end{aligned}$$

**Mathematica** [B] Leaf count is larger than twice the leaf count of optimal. 1924 vs. 2(322) = 644.

time = 1.05, size = 1924, normalized size = 5.98

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^2)/(a + b\*x^n)^3, x]

[Out] (x\*(e\*x)^m\*(a^2\*A\*b^3\*c^2\*(1+m)\*n - a^3\*b^2\*B\*c^2\*(1+m)\*n - 2\*a^3\*A\*b^2\*c\*d\*(1+m)\*n + 2\*a^4\*b\*B\*c\*d\*(1+m)\*n + a^4\*A\*b\*d^2\*(1+m)\*n - a^5\*B\*d^2\*(1+m)\*n - a\*A\*b^3\*c^2\*(1+m)\*(a + b\*x^n) + a^2\*b^2\*B\*c^2\*(1+m)\*(a + b\*x^n) + 2\*a^2\*A\*b^2\*c\*d\*(1+m)\*(a + b\*x^n) - 2\*a^3\*b\*B\*c\*d\*(1+m)\*(a + b\*x^n) - a^3\*A\*b\*d^2\*(1+m)\*(a + b\*x^n) + a^4\*B\*d^2\*(1+m)\*(a + b\*x^n) - a\*A\*b^3\*c^2\*m\*(1+m)\*(a + b\*x^n) + a^2\*b^2\*B\*c^2\*m\*(1+m)\*(a + b\*x^n) + 2\*

$$\begin{aligned}
& a^2 A b^2 c d m (1+m)(a+b x^n) - 2 a^3 b B c d m (1+m)(a+b x^n) - \\
& a^3 A b d^2 m (1+m)(a+b x^n) + a^4 B d^2 m (1+m)(a+b x^n) + 2 a^* \\
& A b^3 c^2 (1+m) n (a+b x^n) - 4 a^3 b B c d (1+m) n (a+b x^n) - 2 a^* \\
& ^3 A b d^2 (1+m) n (a+b x^n) + 4 a^4 B d^2 (1+m) n (a+b x^n) + 2 a^* \\
& ^3 B d^2 n^2 (a+b x^n)^2 + A b^3 c^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1 \\
& + m)/n, (1+m+n)/n, -((b x^n)/a)] - a b^2 B c^2 (a+b x^n)^2 \text{Hypergeom} \\
& \text{etric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] - 2 a^* A b^2 c d (a+b x \\
& ^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + 2 a^2 \\
& * b B c d (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b * \\
& x^n)/a)] + a^2 A b d^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m \\
& + n)/n, -((b x^n)/a)] - a^3 B d^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+ \\
& m)/n, (1+m+n)/n, -((b x^n)/a)] + 2 A b^3 c^2 m (a+b x^n)^2 \text{Hypergeome} \\
& \text{tric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] - 2 a^* b^2 B c^2 m (a+b \\
& * x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] - 4 a^* \\
& A b^2 c d m (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -( \\
& (b x^n)/a)] + 4 a^2 b B c d m (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, \\
& (1+m+n)/n, -((b x^n)/a)] + 2 a^2 A b d^2 m (a+b x^n)^2 \text{Hypergeometri} \\
& \text{c2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] - 2 a^3 B d^2 m (a+b x^n) \\
& ^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + A b^3 c^2 \\
& * m^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n) \\
& /a)] - a b^2 B c^2 m^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m \\
& + n)/n, -((b x^n)/a)] - 2 a^* A b^2 c d m^2 (a+b x^n)^2 \text{Hypergeometric2F1}[ \\
& 1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + 2 a^2 b B c d m^2 (a+b x^n)^ \\
& 2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + a^2 A b d^ \\
& 2 m^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n) \\
& )/a)] - a^3 B d^2 m^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m \\
& + n)/n, -((b x^n)/a)] - 3 A b^3 c^2 n (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1 \\
& + m)/n, (1+m+n)/n, -((b x^n)/a)] + a b^2 B c^2 n (a+b x^n)^2 \text{Hyperge} \\
& \text{ometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + 2 a^* A b^2 c d n (a \\
& + b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + 2 \\
& * a^2 b B c d n (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, \\
& -((b x^n)/a)] + a^2 A b d^2 n (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n \\
& , (1+m+n)/n, -((b x^n)/a)] - 3 a^3 B d^2 n (a+b x^n)^2 \text{Hypergeometric} \\
& \text{2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] - 3 A b^3 c^2 m n (a+b x^n) \\
& )^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + a b^2 B * \\
& c^2 m n (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x \\
& ^n)/a)] + 2 a^* A b^2 c d m n (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, ( \\
& 1+m+n)/n, -((b x^n)/a)] + 2 a^2 b B c d m n (a+b x^n)^2 \text{Hypergeometri} \\
& \text{c2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] + a^2 A b d^2 m n (a+b x^ \\
& n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)] - 3 a^3 B \\
& * d^2 m n (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -((b * \\
& x^n)/a)] + 2 A b^3 c^2 n^2 (a+b x^n)^2 \text{Hypergeometric2F1}[1, (1+m)/n, (1 \\
& + m+n)/n, -((b x^n)/a)] - 2 a^3 B d^2 n^2 (a+b x^n)^2 \text{Hypergeometric2F} \\
& \text{1}[1, (1+m)/n, (1+m+n)/n, -((b x^n)/a)))/(2 a^3 b^3 (1+m) n^2 (a+ \\
& b x^n)^2)
\end{aligned}$$

**Maple [F]**

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)(c + dx^n)^2}{(a + bx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

**[In]** int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^3,x)**[Out]** int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^3,x)**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

**[In]** integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^3,x, algorithm="maxima")

**[Out]** ((m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*b^3\*c^2 - 2\*(m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a\*b^2\*c\*d + (m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a^2\*b\*d^2)\*A - ((m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a\*b^2\*c^2 - 2\*(m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a^2\*b\*c\*d + (m^2\*e^m + m\*(3\*n + 2)\*e^m + (2\*n^2 + 3\*n + 1)\*e^m)\*a^3\*d^2)\*B)\*integrate(1/2\*x^m/(a^2\*b^4\*n^2\*x^n + a^3\*b^3\*n^2), x) + 1/2\*(2\*B\*a^2\*b^2\*d^2\*n^2\*x\*e^(m\*log(x) + 2\*n\*log(x) + m) - (((m^2\*e^m - m\*(3\*n - 2)\*e^m - (3\*n - 1)\*e^m)\*a\*b^3\*c^2 - 2\*(m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a^2\*b^2\*c\*d + (m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a^3\*b\*d^2)\*A - ((m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a^2\*b^2\*c^2 - 2\*(m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a^3\*b\*c\*d + (m^2\*e^m + m\*(3\*n + 2)\*e^m + (2\*n^2 + 3\*n + 1)\*e^m)\*a^4\*d^2)\*B)\*x\*x^m - (((m^2\*e^m - 2\*m\*(n - 1)\*e^m - (2\*n - 1)\*e^m)\*b^4\*c^2 - 2\*(m^2\*e^m + 2\*m\*e^m + e^m)\*a\*b^3\*c\*d + (m^2\*e^m + 2\*m\*(n + 1)\*e^m + (2\*n + 1)\*e^m)\*a^2\*b^2\*d^2)\*A - ((m^2\*e^m + 2\*m\*e^m + e^m)\*a\*b^3\*c^2 - 2\*(m^2\*e^m + 2\*m\*(n + 1)\*e^m + (2\*n + 1)\*e^m)\*a^2\*b^2\*c\*d + (m^2\*e^m + 2\*m\*(2\*n + 1)\*e^m + (4\*n^2 + 4\*n + 1)\*e^m)\*a^3\*b\*d^2)\*B)\*x\*e^(m\*log(x) + n\*log(x)))/((m\*n^2 + n^2)\*a^2\*b^5\*x^(2\*n) + 2\*(m\*n^2 + n^2)\*a^3\*b^4\*x^n + (m\*n^2 + n^2)\*a^4\*b^3)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

**[In]** integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^2/(a+b\*x^n)^3,x, algorithm="fricas")

[Out] `integral((B*d^2*x^(3*n) + A*c^2 + (2*B*c*d + A*d^2)*x^(2*n) + (B*c^2 + 2*A*c*d)*x^n)*(x*e)^m/(b^3*x^(3*n) + 3*a*b^2*x^(2*n) + 3*a^2*b*x^n + a^3), x)`

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)**m*(A+B*x**n)*(c+d*x**n)**2/(a+b*x**n)**3,x)`

[Out] Timed out

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^2/(a+b*x^n)^3,x, algorithm="giac")`

[Out] `integrate((B*x^n + A)*(d*x^n + c)^2*(x*e)^m/(b*x^n + a)^3, x)`

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)^2}{(a + bx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] `int(((e*x)^m*(A + B*x^n)*(c + d*x^n)^2)/(a + b*x^n)^3,x)`

[Out] `int(((e*x)^m*(A + B*x^n)*(c + d*x^n)^2)/(a + b*x^n)^3, x)`

### 3.15 $\int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=410

$$\frac{a^2c^2(aBc + 3A(bc + ad))x^{1+n}(ex)^m}{1 + m + n} + \frac{3ac(aBc(bc + ad) + A(b^2c^2 + 3abcd + a^2d^2))x^{1+2n}(ex)^m}{1 + m + 2n} + \frac{(3aBc(b^2c^2 + 3abd^2 + a^2d^2))x^{1+3n}(ex)^m}{1 + m + 3n} + \frac{(3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2) + 3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2))x^{1+4n}(ex)^m}{1 + m + 4n} + \frac{(3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2) + 3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2))x^{1+5n}(ex)^m}{1 + m + 5n} + \frac{(3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2) + 3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2))x^{1+6n}(ex)^m}{1 + m + 6n} + \frac{(3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2) + 3a^2Bd^2(b^2c^2 + 3abd^2 + a^2d^2))x^{1+7n}(ex)^m}{1 + m + 7n}$$

```
[Out] a^2*c^2*(a*B*c+3*A*(a*d+b*c))*x^(1+n)*(e*x)^m/(1+m+n)+3*a*c*(a*B*c*(a*d+b*c)
)+A*(a^2*d^2+3*a*b*c*d+b^2*c^2))*x^(1+2*n)*(e*x)^m/(1+m+2*n)+(3*a*B*c*(a^2*
d^2+3*a*b*c*d+b^2*c^2)+A*(a^3*d^3+9*a^2*b*c*d^2+9*a*b^2*c^2*d+b^3*c^3))*x^(
1+3*n)*(e*x)^m/(1+m+3*n)+(a^3*B*d^3+9*a*b^2*c*d*(A*d+B*c)+3*a^2*b*d^2*(A*d+
3*B*c)+b^3*c^2*(3*A*d+B*c))*x^(1+4*n)*(e*x)^m/(1+m+4*n)+3*b*d*(a^2*B*d^2+b^
2*c*(A*d+B*c)+a*b*d*(A*d+3*B*c))*x^(1+5*n)*(e*x)^m/(1+m+5*n)+b^2*d^2*(A*b*d
+3*B*a*d+3*B*b*c))*x^(1+6*n)*(e*x)^m/(1+m+6*n)+b^3*B*d^3*x^(1+7*n)*(e*x)^m/(
1+m+7*n)+a^3*A*c^3*(e*x)^(1+m)/e/(1+m)
```

**Rubi [A]**

time = 0.41, antiderivative size = 410, normalized size of antiderivative = 1.00, number of steps used = 16, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {584, 20, 30}

$\frac{a^2A^2c^{m+1}}{m+1} + \frac{3ac^2b^{m+1}(a^2d^2 + 3abd + b^2c^2) + a^2d^2(ad + bc)}{m+2n+1} + \frac{3a^2Bd^2c^{m+1}(a^2d^2 + 3abd + b^2c^2) + a^2d^2(ad + bc)}{m+3n+1} + \frac{a^2c^2b^{m+1}(a^2d^2 + 3abd + b^2c^2) + a^2d^2(ad + bc)}{m+4n+1} + \frac{a^{2m+1}(a^2Bd^2 + 3a^2Bd^2(ad + b^2c^2) + 3a^2Bd^2(ad + b^2c^2) + 3a^2Bd^2(ad + b^2c^2))}{m+5n+1} + \frac{a^{2m+1}(a^2Bd^2 + 3a^2Bd^2(ad + b^2c^2) + 3a^2Bd^2(ad + b^2c^2) + 3a^2Bd^2(ad + b^2c^2))}{m+6n+1} + \frac{a^{2m+1}(a^2Bd^2 + 3a^2Bd^2(ad + b^2c^2) + 3a^2Bd^2(ad + b^2c^2) + 3a^2Bd^2(ad + b^2c^2))}{m+7n+1}$

Antiderivative was successfully verified.

```
[In] Int[(e*x)^m*(a + b*x^n)^3*(A + B*x^n)*(c + d*x^n)^3,x]
```

```
[Out] (a^2*c^2*(a*B*c + 3*A*(b*c + a*d))*x^(1 + n)*(e*x)^m/(1 + m + n) + (3*a*c*
(a*B*c*(b*c + a*d) + A*(b^2*c^2 + 3*a*b*c*d + a^2*d^2))*x^(1 + 2*n)*(e*x)^m
)/(1 + m + 2*n) + ((3*a*B*c*(b^2*c^2 + 3*a*b*c*d + a^2*d^2) + A*(b^3*c^3 +
9*a*b^2*c^2*d + 9*a^2*b*c*d^2 + a^3*d^3))*x^(1 + 3*n)*(e*x)^m)/(1 + m + 3*n
) + ((a^3*B*d^3 + 9*a*b^2*c*d*(B*c + A*d) + 3*a^2*b*d^2*(3*B*c + A*d) + b^3
*c^2*(B*c + 3*A*d))*x^(1 + 4*n)*(e*x)^m)/(1 + m + 4*n) + (3*b*d*(a^2*B*d^2
+ b^2*c*(B*c + A*d) + a*b*d*(3*B*c + A*d))*x^(1 + 5*n)*(e*x)^m)/(1 + m + 5*
n) + (b^2*d^2*(3*b*B*c + A*b*d + 3*a*B*d))*x^(1 + 6*n)*(e*x)^m)/(1 + m + 6*n
) + (b^3*B*d^3*x^(1 + 7*n)*(e*x)^m)/(1 + m + 7*n) + (a^3*A*c^3*(e*x)^(1 + m
))/e/(1 + m))
```

**Rule 20**

```
Int[(u_)*((a_)*(v_))^(m_)*((b_)*(v_))^(n_), x_Symbol] := Dist[b^IntPart[
n]*((b*v)^FracPart[n]/(a^IntPart[n]*(a*v)^FracPart[n])), Int[u*(a*v)^(m + n
), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !
IntegerQ[m + n]
```

**Rule 30**

```
Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]
```

### Rule 584

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

### Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^3 (A + Bx^n) (c + dx^n)^3 dx &= \int (a^3 Ac^3 (ex)^m + a^2 c^2 (aBc + 3A(bc + ad)) x^n (ex)^m + 3ac(aBc + 3Ad) x^{2n} (ex)^m + (b^3 Bd^3) x^{7n} (ex)^m) dx \\ &= \frac{a^3 Ac^3 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^3) \int x^{7n} (ex)^m dx + (b^2 d^2 (3bBc + Ab^2 d)) \int x^{6n} (ex)^m dx \\ &= \frac{a^3 Ac^3 (ex)^{1+m}}{e(1+m)} + (b^3 Bd^3 x^{-m} (ex)^m) \int x^{m+7n} dx + (b^2 d^2 (3bBc + Ab^2 d)) \int x^{m+6n} dx \\ &= \frac{a^2 c^2 (aBc + 3A(bc + ad)) x^{1+n} (ex)^m}{1+m+n} + \frac{3ac(aBc(bc + ad) + A^2 d^2)}{1+m+n} x^{1+n} (ex)^m \end{aligned}$$

### Mathematica [A]

time = 1.53, size = 358, normalized size = 0.87

$$x(ex)^m \left( \frac{a^3 Ac^3}{1+m} + \frac{a^2 c^2 (aBc + 3A(bc + ad)) x^n}{1+m+n} + \frac{3ac(aBc + 3Ad) x^{2n}}{1+m+2n} + \frac{(3aBc(b^2 c^2 + 3abod + a^2 d^2) + A(b^3 c^2 + 9ab^2 c d + 9a^2 b o d^2 + a^3 d^3)) x^{3n}}{1+m+3n} + \frac{(b^3 B d^3 + 9ab^2 d(Bc + Ad) + 3a^2 b d^2 (3Bc + Ad) + b^2 d^2 (Bc + 3Ad)) x^{4n}}{1+m+4n} + \frac{3bd^2 B d^2 + b^2 d^2 (Bc + Ad) + abd(3Bc + Ad) x^{5n}}{1+m+5n} + \frac{b^2 d^2 (3bBc + Ab^2 d) x^{6n}}{1+m+6n} + \frac{b^3 B d^3 x^{7n}}{1+m+7n} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*(a + b*x^n)^3*(A + B*x^n)*(c + d*x^n)^3,x]
```

```
[Out] x*(e*x)^m*((a^3*A*c^3)/(1 + m) + (a^2*c^2*(a*B*c + 3*A*(b*c + a*d))*x^n)/(1 + m + n) + (3*a*c*(a*B*c*(b*c + a*d) + A*(b^2*c^2 + 3*a*b*c*d + a^2*d^2))*x^(2*n))/(1 + m + 2*n) + ((3*a*B*c*(b^2*c^2 + 3*a*b*c*d + a^2*d^2) + A*(b^3*c^3 + 9*a*b^2*c^2*d + 9*a^2*b*c*d^2 + a^3*d^3))*x^(3*n))/(1 + m + 3*n) + ((a^3*B*d^3 + 9*a*b^2*c*d*(B*c + A*d) + 3*a^2*b*d^2*(3*B*c + A*d) + b^3*c^2*(B*c + 3*A*d))*x^(4*n))/(1 + m + 4*n) + (3*b*d*(a^2*B*d^2 + b^2*c*(B*c + A*d) + a*b*d*(3*B*c + A*d))*x^(5*n))/(1 + m + 5*n) + (b^2*d^2*(3*b*B*c + A*b*d + 3*a*B*d))*x^(6*n))/(1 + m + 6*n) + (b^3*B*d^3*x^(7*n))/(1 + m + 7*n))
```

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.59, size = 20937, normalized size = 51.07

method	result	size
risch	Expression too large to display	20937

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^3,x,method=_RETURNVERBOSE)
```

```
[Out] result too large to display
```

**Maxima** [B] Leaf count of result is larger than twice the leaf count of optimal. 970 vs. 2(417) = 834.

time = 0.46, size = 970, normalized size = 2.37

---

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="maxima")
```

```
[Out] (x*e)^(m + 1)*A*a^3*c^3*e^(-1)/(m + 1) + B*b^3*d^3*x*e^(m*log(x) + 7*n*log(x) + m)/(m + 7*n + 1) + 3*B*b^3*c*d^2*x*e^(m*log(x) + 6*n*log(x) + m)/(m + 6*n + 1) + 3*B*a*b^2*d^3*x*e^(m*log(x) + 6*n*log(x) + m)/(m + 6*n + 1) + A*b^3*d^3*x*e^(m*log(x) + 6*n*log(x) + m)/(m + 6*n + 1) + 3*B*b^3*c^2*d*x*e^(m*log(x) + 5*n*log(x) + m)/(m + 5*n + 1) + 9*B*a*b^2*c*d^2*x*e^(m*log(x) + 5*n*log(x) + m)/(m + 5*n + 1) + 3*A*b^3*c*d^2*x*e^(m*log(x) + 5*n*log(x) + m)/(m + 5*n + 1) + 3*B*a^2*b*d^3*x*e^(m*log(x) + 5*n*log(x) + m)/(m + 5*n + 1) + 3*A*a*b^2*d^3*x*e^(m*log(x) + 5*n*log(x) + m)/(m + 5*n + 1) + B*b^3*c^3*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + 9*B*a*b^2*c^2*d*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + 3*A*b^3*c^2*d*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + 9*B*a^2*b*c*d^2*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + 9*A*a*b^2*c*d^2*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + B*a^3*d^3*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + 3*A*a^2*b*d^3*x*e^(m*log(x) + 4*n*log(x) + m)/(m + 4*n + 1) + 3*B*a*b^2*c^3*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + A*b^3*c^3*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 9*B*a^2*b*c^2*d*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 9*A*a*b^2*c^2*d*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 3*B*a^3*c*d^2*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 9*A*a^2*b*c*d^2*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + A*a^3*d^3*x*e^(m*log(x) + 3*n*log(x) + m)/(m + 3*n + 1) + 3*B*a^2*b*c^3*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + 3*A*a*b^2*c^3*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + 3*B*a^3*c^2*d*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + 9*A*a^2*b*c^2*d*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + 3*A*a^3*c*d^2*x*e^(m*log(x) + 2*n*log(x) + m)/(m + 2*n + 1) + B*a^3*c^3*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1) + 3*A*a^2*b*c^3*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1) + 3*A*a^3*c^2*d*x*e^(m*log(x) + n*log(x) + m)/(m + n + 1)
```

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 11604 vs.  $2(417) = 834$ .

time = 1.45, size = 11604, normalized size = 28.30

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="fricas")
[Out] ((B*b^3*d^3*m^7 + 7*B*b^3*d^3*m^6 + 21*B*b^3*d^3*m^5 + 35*B*b^3*d^3*m^4 + 3
5*B*b^3*d^3*m^3 + 21*B*b^3*d^3*m^2 + 7*B*b^3*d^3*m + B*b^3*d^3 + 720*(B*b^3
*d^3*m + B*b^3*d^3)*n^6 + 1764*(B*b^3*d^3*m^2 + 2*B*b^3*d^3*m + B*b^3*d^3)*
n^5 + 1624*(B*b^3*d^3*m^3 + 3*B*b^3*d^3*m^2 + 3*B*b^3*d^3*m + B*b^3*d^3)*n^
4 + 735*(B*b^3*d^3*m^4 + 4*B*b^3*d^3*m^3 + 6*B*b^3*d^3*m^2 + 4*B*b^3*d^3*m
+ B*b^3*d^3)*n^3 + 175*(B*b^3*d^3*m^5 + 5*B*b^3*d^3*m^4 + 10*B*b^3*d^3*m^3
+ 10*B*b^3*d^3*m^2 + 5*B*b^3*d^3*m + B*b^3*d^3)*n^2 + 21*(B*b^3*d^3*m^6 + 6
*B*b^3*d^3*m^5 + 15*B*b^3*d^3*m^4 + 20*B*b^3*d^3*m^3 + 15*B*b^3*d^3*m^2 + 6
*B*b^3*d^3*m + B*b^3*d^3)*n)*x*x^(7*n)*e^(m*log(x) + m) + ((3*B*b^3*c*d^2 +
(3*B*a*b^2 + A*b^3)*d^3)*m^7 + 3*B*b^3*c*d^2 + 7*(3*B*b^3*c*d^2 + (3*B*a*b
^2 + A*b^3)*d^3)*m^6 + 840*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3 + (3*B*
b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m)*n^6 + 21*(3*B*b^3*c*d^2 + (3*B*a*b^
2 + A*b^3)*d^3)*m^5 + 2038*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3 + (3*B*
b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^2 + 2*(3*B*b^3*c*d^2 + (3*B*a*b^2 +
A*b^3)*d^3)*m)*n^5 + 35*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^4 + 184
9*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3 + (3*B*b^3*c*d^2 + (3*B*a*b^2 +
A*b^3)*d^3)*m^3 + 3*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^2 + 3*(3*B*
b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m)*n^4 + (3*B*a*b^2 + A*b^3)*d^3 + 35*
(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^3 + 820*(3*B*b^3*c*d^2 + (3*B*b
^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^4 + (3*B*a*b^2 + A*b^3)*d^3 + 4*(3*B*
b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^3 + 6*(3*B*b^3*c*d^2 + (3*B*a*b^2 +
A*b^3)*d^3)*m^2 + 4*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m)*n^3 + 21*(
3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^2 + 190*(3*B*b^3*c*d^2 + (3*B*b^
3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^5 + 5*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*
b^3)*d^3)*m^4 + (3*B*a*b^2 + A*b^3)*d^3 + 10*(3*B*b^3*c*d^2 + (3*B*a*b^2 +
A*b^3)*d^3)*m^3 + 10*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^2 + 5*(3*B
*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m)*n^2 + 7*(3*B*b^3*c*d^2 + (3*B*a*b^
2 + A*b^3)*d^3)*m + 22*(3*B*b^3*c*d^2 + (3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3
)*d^3)*m^6 + 6*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^5 + 15*(3*B*b^3*
c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^4 + (3*B*a*b^2 + A*b^3)*d^3 + 20*(3*B*b^
3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m^3 + 15*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A
*b^3)*d^3)*m^2 + 6*(3*B*b^3*c*d^2 + (3*B*a*b^2 + A*b^3)*d^3)*m)*n)*x*x^(6*n
)*e^(m*log(x) + m) + 3*((B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b
+ A*a*b^2)*d^3)*m^7 + B*b^3*c^2*d + 7*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c
*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^6 + 1008*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^
3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + (B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d
```



$$\begin{aligned}
&^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^6 + 21*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3) \\
&)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^5 + 2412*(B*b^3*c^2*d + (3*B*a*b^2 + A \\
&)*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + (B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)* \\
&)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 2*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3) \\
&)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^5 + 35*(B*b^3*c^2*d + (3*B*a*b^2 + A \\
&)*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + 2144*(B*b^3*c^2*d + (3*B*a*b^2 \\
& + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + (B*b^3*c^2*d + (3*B*a*b^2 + A*b \\
&^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 3*(B*b^3*c^2*d + (3*B*a*b^2 + A* \\
&b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 3*(B*b^3*c^2*d + (3*B*a*b^2 + A \\
&)*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^4 + (3*B*a*b^2 + A*b^3)*c*d^2 + \\
&(B*a^2*b + A*a*b^2)*d^3 + 35*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B \\
&a^2*b + A*a*b^2)*d^3)*m^3 + 925*(B*b^3*c^2*d + (B*b^3*c^2*d + (3*B*a*b^2 + \\
&A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + (3*B*a*b^2 + A*b^3)*c*d^2 + \\
&(B*a^2*b + A*a*b^2)*d^3 + 4*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B*a \\
&^2*b + A*a*b^2)*d^3)*m^3 + 6*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B* \\
&a^2*b + A*a*b^2)*d^3)*m^2 + 4*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 + (B \\
&a^2*b + A*a*b^2)*d^3)*m)*n^3 + 21*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 \\
& + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 207*(B*b^3*c^2*d + (B*b^3*c^2*d + (3*B*a* \\
&b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^5 + 5*(B*b^3*c^2*d + (3*B*a \\
&)*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + (3*B*a*b^2 + A*b^3)*c* \\
&d^2 + (B*a^2*b + A*a*b^2)*d^3 + 10*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d^2 \\
& + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 10*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c*d \\
&^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 5*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3)*c* \\
&d^2 + (B*a^2*b + A*a*b^2)*d^3)*m)*n^2 + 7*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3) \\
&)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m + 23*(B*b^3*c^2*d + (B*b^3*c^2*d + (3* \\
&B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^6 + 6*(B*b^3*c^2*d + (3 \\
&)*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^5 + 15*(B*b^3*c^2*d + \\
&(3*B*a*b^2 + A*b^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^4 + (3*B*a*b^2 + A*b \\
&^3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3 + 20*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^3) \\
&)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^3 + 15*(B*b^3*c^2*d + (3*B*a*b^2 + A*b^ \\
&3)*c*d^2 + (B*a^2*b + A*a*b^2)*d^3)*m^2 + 6*(B*...
\end{aligned}$$

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*3\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*3,x)

[Out] Timed out

**Giac** [B] Leaf count of result is larger than twice the leaf count of optimal. 27792 vs. 2(417) = 834.

time = 1.93, size = 27792, normalized size = 67.79

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="giac")

[Out]  $(B*b^3*d^3*m^7*x*x^m*x^{(7*n)}*e^m + 21*B*b^3*d^3*m^6*n*x*x^m*x^{(7*n)}*e^m + 175*B*b^3*d^3*m^5*n^2*x*x^m*x^{(7*n)}*e^m + 735*B*b^3*d^3*m^4*n^3*x*x^m*x^{(7*n)}*e^m + 1624*B*b^3*d^3*m^3*n^4*x*x^m*x^{(7*n)}*e^m + 1764*B*b^3*d^3*m^2*n^5*x*x^m*x^{(7*n)}*e^m + 720*B*b^3*d^3*m*n^6*x*x^m*x^{(7*n)}*e^m + 3*B*b^3*c*d^2*m^7*x*x^m*x^{(6*n)}*e^m + 3*B*a*b^2*d^3*m^7*x*x^m*x^{(6*n)}*e^m + A*b^3*d^3*m^7*x*x^m*x^{(6*n)}*e^m + 66*B*b^3*c*d^2*m^6*n*x*x^m*x^{(6*n)}*e^m + 66*B*a*b^2*d^3*m^6*n*x*x^m*x^{(6*n)}*e^m + 22*A*b^3*d^3*m^6*n*x*x^m*x^{(6*n)}*e^m + 570*B*b^3*c*d^2*m^5*n^2*x*x^m*x^{(6*n)}*e^m + 570*B*a*b^2*d^3*m^5*n^2*x*x^m*x^{(6*n)}*e^m + 190*A*b^3*d^3*m^5*n^2*x*x^m*x^{(6*n)}*e^m + 2460*B*b^3*c*d^2*m^4*n^3*x*x^m*x^{(6*n)}*e^m + 2460*B*a*b^2*d^3*m^4*n^3*x*x^m*x^{(6*n)}*e^m + 820*A*b^3*d^3*m^4*n^3*x*x^m*x^{(6*n)}*e^m + 5547*B*b^3*c*d^2*m^3*n^4*x*x^m*x^{(6*n)}*e^m + 5547*B*a*b^2*d^3*m^3*n^4*x*x^m*x^{(6*n)}*e^m + 1849*A*b^3*d^3*m^3*n^4*x*x^m*x^{(6*n)}*e^m + 6114*B*b^3*c*d^2*m^2*n^5*x*x^m*x^{(6*n)}*e^m + 6114*B*a*b^2*d^3*m^2*n^5*x*x^m*x^{(6*n)}*e^m + 2038*A*b^3*d^3*m^2*n^5*x*x^m*x^{(6*n)}*e^m + 2520*B*b^3*c*d^2*m*n^6*x*x^m*x^{(6*n)}*e^m + 2520*B*a*b^2*d^3*m*n^6*x*x^m*x^{(6*n)}*e^m + 840*A*b^3*d^3*m*n^6*x*x^m*x^{(6*n)}*e^m + 3*B*b^3*c^2*d*m^7*x*x^m*x^{(5*n)}*e^m + 9*B*a*b^2*c*d^2*m^7*x*x^m*x^{(5*n)}*e^m + 3*A*b^3*c*d^2*m^7*x*x^m*x^{(5*n)}*e^m + 3*B*a^2*b*d^3*m^7*x*x^m*x^{(5*n)}*e^m + 3*A*a*b^2*d^3*m^7*x*x^m*x^{(5*n)}*e^m + 69*B*b^3*c^2*d*m^6*n*x*x^m*x^{(5*n)}*e^m + 207*B*a*b^2*c*d^2*m^6*n*x*x^m*x^{(5*n)}*e^m + 69*A*b^3*c*d^2*m^6*n*x*x^m*x^{(5*n)}*e^m + 69*B*a^2*b*d^3*m^6*n*x*x^m*x^{(5*n)}*e^m + 69*A*a*b^2*d^3*m^6*n*x*x^m*x^{(5*n)}*e^m + 621*B*b^3*c^2*d*m^5*n^2*x*x^m*x^{(5*n)}*e^m + 1863*B*a*b^2*c*d^2*m^5*n^2*x*x^m*x^{(5*n)}*e^m + 621*A*b^3*c*d^2*m^5*n^2*x*x^m*x^{(5*n)}*e^m + 621*B*a^2*b*d^3*m^5*n^2*x*x^m*x^{(5*n)}*e^m + 621*A*a*b^2*d^3*m^5*n^2*x*x^m*x^{(5*n)}*e^m + 2775*B*b^3*c^2*d*m^4*n^3*x*x^m*x^{(5*n)}*e^m + 8325*B*a*b^2*c*d^2*m^4*n^3*x*x^m*x^{(5*n)}*e^m + 2775*A*b^3*c*d^2*m^4*n^3*x*x^m*x^{(5*n)}*e^m + 2775*B*a^2*b*d^3*m^4*n^3*x*x^m*x^{(5*n)}*e^m + 2775*A*a*b^2*d^3*m^4*n^3*x*x^m*x^{(5*n)}*e^m + 6432*B*b^3*c^2*d*m^3*n^4*x*x^m*x^{(5*n)}*e^m + 19296*B*a*b^2*c*d^2*m^3*n^4*x*x^m*x^{(5*n)}*e^m + 6432*A*b^3*c*d^2*m^3*n^4*x*x^m*x^{(5*n)}*e^m + 6432*B*a^2*b*d^3*m^3*n^4*x*x^m*x^{(5*n)}*e^m + 7236*B*b^3*c^2*d*m^2*n^5*x*x^m*x^{(5*n)}*e^m + 21708*B*a*b^2*c*d^2*m^2*n^5*x*x^m*x^{(5*n)}*e^m + 7236*A*b^3*c*d^2*m^2*n^5*x*x^m*x^{(5*n)}*e^m + 7236*B*a^2*b*d^3*m^2*n^5*x*x^m*x^{(5*n)}*e^m + 3024*B*b^3*c^2*d*m*n^6*x*x^m*x^{(5*n)}*e^m + 9072*B*a*b^2*c*d^2*m*n^6*x*x^m*x^{(5*n)}*e^m + 3024*A*b^3*c*d^2*m*n^6*x*x^m*x^{(5*n)}*e^m + 3024*B*a^2*b*d^3*m*n^6*x*x^m*x^{(5*n)}*e^m + 3024*A*a*b^2*d^3*m*n^6*x*x^m*x^{(5*n)}*e^m + B*b^3*c^3*m^7*x*x^m*x^{(4*n)}*e^m + 9*B*a*b^2*c^2*d*m^7*x*x^m*x^{(4*n)}*e^m + 3*A*b^3*c^2*d*m^7*x*x^m*x^{(4*n)}*e^m + 9*B*a^2*b*c*d^2*m^7*x*x^m*x^{(4*n)}*e^m + 9*A*a*b^2*c*d^2*m^7*x*x^m*x^{(4*n)}*e^m + B*a^3*d^3*m^7*x*x^m*x^{(4*n)}*e^m + 3*A*a^2*b*d^3*m^7*x*x^m*x^{(4*n)}*e^m + 24*B*b^3*c^3*m^6*n*x*x^m*x^{(4*n)}*e^m + 216*B*a*b^2*c^2*d*m^6*n*x*x^m*x^{(4*n)}*e^m + 72*A*b^3*c^2*d*m^6*n*x*x^m*x^{(4*n)}*e^m$

$$\begin{aligned}
& \text{^m} + 216*B*a^2*b*c*d^2*m^6*n*x*x^m*x^(4*n)*e^m + 216*A*a*b^2*c*d^2*m^6*n*x* \\
& x^m*x^(4*n)*e^m + 24*B*a^3*d^3*m^6*n*x*x^m*x^(4*n)*e^m + 72*A*a^2*b*d^3*m^6 \\
& *n*x*x^m*x^(4*n)*e^m + 226*B*b^3*c^3*m^5*n^2*x*x^m*x^(4*n)*e^m + 2034*B*a*b \\
& ^2*c^2*d*m^5*n^2*x*x^m*x^(4*n)*e^m + 678*A*b^3*c^2*d*m^5*n^2*x*x^m*x^(4*n)* \\
& e^m + 2034*B*a^2*b*c*d^2*m^5*n^2*x*x^m*x^(4*n)*e^m + 2034*A*a*b^2*c*d^2*m^5 \\
& *n^2*x*x^m*x^(4*n)*e^m + 226*B*a^3*d^3*m^5*n^2*x*x^m*x^(4*n)*e^m + 678*A*a^ \\
& 2*b*d^3*m^5*n^2*x*x^m*x^(4*n)*e^m + 1056*B*b^3*c^3*m^4*n^3*x*x^m*x^(4*n)*e^ \\
& m + 9504*B*a*b^2*c^2*d*m^4*n^3*x*x^m*x^(4*n)*e^m + 3168*A*b^3*c^2*d*m^4*n^3 \\
& *x*x^m*x^(4*n)*e^m + 9504*B*a^2*b*c*d^2*m^4*n^3*x*x^m*x^(4*n)*e^m + 9504*A \\
& a*b^2*c*d^2*m^4*n^3*x*x^m*x^(4*n)*e^m + 1056*B*a^3*d^3*m^4*n^3*x*x^m*x^(4*n \\
& )*e^m + 3168*A*a^2*b*d^3*m^4*n^3*x*x^m*x^(4*n)*e^m + 2545*B*b^3*c^3*m^3*n^4 \\
& *x*x^m*x^(4*n)*e^m + 22905*B*a*b^2*c^2*d*m^3*n^4*x*x^m*x^(4*n)*e^m + 7635*A \\
& *b^3*c^2*d*m^3*n^4*x*x^m*x^(4*n)*e^m + 22905*B*a^2*b*c*d^2*m^3*n^4*x*x^m*x^ \\
& (4*n)*e^m + 22905*A*a*b^2*c*d^2*m^3*n^4*x*x^m*x^(4*n)*e^m + 2545*B*a^3*d^3* \\
& m^3*n^4*x*x^m*x^(4*n)*e^m + 7635*A*a^2*b*d^3*m^3*n^4*x*x^m*x^(4*n)*e^m + 29 \\
& 52*B*b^3*c^3*m^2*n^5*x*x^m*x^(4*n)*e^m + 26568*B*a*b^2*c^2*d*m^2*n^5*x*x^m* \\
& x^(4*n)*e^m + 8856*A*b^3*c^2*d*m^2*n^5*x*x^m*x^(4*n)*e^m + 26568*B*a^2*b*c* \\
& d^2*m^2*n^5*x*x^m*x^(4*n)*e^m + 26568*A*a*b^2*c*d^2*m^2*n^5*x*x^m*x^(4*n)*e \\
& ^m + 2952*B*a^3*d^3*m^2*n^5*x*x^m*x^(4*n)*e^m + 8856*A*a^2*b*d^3*m^2*n^5*x* \\
& x^m*x^(4*n)*e^m + 1260*B*b^3*c^3*m*n^6*x*x^m*x^(4*n)*e^m + 11340*B*a*b^2*c^ \\
& 2*d*m*n^6*x*x^m*x^(4*n)*e^m + 3780*A*b^3*c^2*d*m*n^6*x*x^m*x^(4*n)*e^m + 11 \\
& 340*B*a^2*b*c*d^2*m*n^6*x*x^m*x^(4*n)*e^m + 11340*A*a*b^2*c*d^2*m*n^6*x*x^m \\
& *x^(4*n)*e^m + 1260*B*a^3*d^3*m*n^6*x*x^m*x^(4*n)*e^m + 3780*A*a^2*b*d^3*m* \\
& n^6*x*x^m*x^(4*n)*e^m + 3*B*a*b^2*c^3*m^7*x*x^m*x^(3*n)*e^m + A*b^3*c^3*m^7 \\
& *x*x^m*x^(3*n)*e^m + 9*B*a^2*b*c^2*d*m^7*x*x^m*x^(3*n)*e^m + 9*A*a*b^2*c^2* \\
& d*m^7*x*x^m*x^(3*n)*e^m + 3*B*a^3*c*d^2*m^7*x*x^m*x^(3*n)*e^m + 3*B*a^3*c*d^2*m^7*x*x^m*x^(3*n)*e^m + \dots
\end{aligned}$$

**Mupad [B]**

time = 7.49, size = 2500, normalized size = 6.10

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)^3*(c + d*x^n)^3,x)$

[Out]  $(x*x^(3*n)*(e*x)^m*(A*a^3*d^3 + A*b^3*c^3 + 3*B*a*b^2*c^3 + 3*B*a^3*c*d^2 + 9*A*a*b^2*c^2*d + 9*A*a^2*b*c*d^2 + 9*B*a^2*b*c^2*d)*(6*m + 25*n + 125*m*n + 988*m*n^2 + 250*m^2*n + 3657*m*n^3 + 250*m^3*n + 6224*m*n^4 + 125*m^4*n + 3796*m*n^5 + 25*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 247*n^2 + 1219*n^3 + 3112*n^4 + 3796*n^5 + 1680*n^6 + 1482*m^2*n^2 + 3657*m^2*n^3 + 988*m^3*n^2 + 3112*m^2*n^4 + 1219*m^3*n^3 + 247*m^4*n^2 + 1))/(7*m + 28*n + 168*m*n + 1610*m*n^2 + 420*m^2*n + 7840*m*n^3 + 560*m^3*n + 20307*m*n^4 + 420*m^4*n + 26264*m*n^5 + 168*m^5*n + 13068*m*n^6 + 28*m^6*n + 21*m^2 + 35*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + m^7 + 322*n^2 + 1960*n^3 + 6769*n^4 + 1313*2*n^5 + 13068*n^6 + 5040*n^7 + 3220*m^2*n^2 + 11760*m^2*n^3 + 3220*m^3*n^2$

$$\begin{aligned}
& + 20307*m^2*n^4 + 7840*m^3*n^3 + 1610*m^4*n^2 + 13132*m^2*n^5 + 6769*m^3*n^4 \\
& + 1960*m^4*n^3 + 322*m^5*n^2 + 1) + (x*x^{(4*n)}*(e*x)^m*(B*a^3*d^3 + B*b^3 \\
& *c^3 + 3*A*a^2*b*d^3 + 3*A*b^3*c^2*d + 9*A*a*b^2*c*d^2 + 9*B*a*b^2*c^2*d + \\
& 9*B*a^2*b*c*d^2)*(6*m + 24*n + 120*m*n + 904*m*n^2 + 240*m^2*n + 3168*m*n^3 \\
& + 240*m^3*n + 5090*m*n^4 + 120*m^4*n + 2952*m*n^5 + 24*m^5*n + 15*m^2 + 20 \\
& *m^3 + 15*m^4 + 6*m^5 + m^6 + 226*n^2 + 1056*n^3 + 2545*n^4 + 2952*n^5 + 12 \\
& 60*n^6 + 1356*m^2*n^2 + 3168*m^2*n^3 + 904*m^3*n^2 + 2545*m^2*n^4 + 1056*m^ \\
& 3*n^3 + 226*m^4*n^2 + 1))/(7*m + 28*n + 168*m*n + 1610*m*n^2 + 420*m^2*n + \\
& 7840*m*n^3 + 560*m^3*n + 20307*m*n^4 + 420*m^4*n + 26264*m*n^5 + 168*m^5*n \\
& + 13068*m*n^6 + 28*m^6*n + 21*m^2 + 35*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + m^7 \\
& + 322*n^2 + 1960*n^3 + 6769*n^4 + 13132*n^5 + 13068*n^6 + 5040*n^7 + 3220*m \\
& ^2*n^2 + 11760*m^2*n^3 + 3220*m^3*n^2 + 20307*m^2*n^4 + 7840*m^3*n^3 + 1610 \\
& *m^4*n^2 + 13132*m^2*n^5 + 6769*m^3*n^4 + 1960*m^4*n^3 + 322*m^5*n^2 + 1) + \\
& (A*a^3*c^3*x*(e*x)^m)/(m + 1) + (a^2*c^2*x*x^n*(e*x)^m*(3*A*a*d + 3*A*b*c \\
& + B*a*c)*(6*m + 27*n + 135*m*n + 1180*m*n^2 + 270*m^2*n + 4995*m*n^3 + 270* \\
& m^3*n + 10208*m*n^4 + 135*m^4*n + 8028*m*n^5 + 27*m^5*n + 15*m^2 + 20*m^3 + \\
& 15*m^4 + 6*m^5 + m^6 + 295*n^2 + 1665*n^3 + 5104*n^4 + 8028*n^5 + 5040*n^6 \\
& + 1770*m^2*n^2 + 4995*m^2*n^3 + 1180*m^3*n^2 + 5104*m^2*n^4 + 1665*m^3*n^3 \\
& + 295*m^4*n^2 + 1))/(7*m + 28*n + 168*m*n + 1610*m*n^2 + 420*m^2*n + 7840* \\
& m*n^3 + 560*m^3*n + 20307*m*n^4 + 420*m^4*n + 26264*m*n^5 + 168*m^5*n + 130 \\
& 68*m*n^6 + 28*m^6*n + 21*m^2 + 35*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + m^7 + 322 \\
& *n^2 + 1960*n^3 + 6769*n^4 + 13132*n^5 + 13068*n^6 + 5040*n^7 + 3220*m^2*n^ \\
& 2 + 11760*m^2*n^3 + 3220*m^3*n^2 + 20307*m^2*n^4 + 7840*m^3*n^3 + 1610*m^4* \\
& n^2 + 13132*m^2*n^5 + 6769*m^3*n^4 + 1960*m^4*n^3 + 322*m^5*n^2 + 1) + (B*b \\
& ^3*d^3*x*x^{(7*n)}*(e*x)^m*(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 22 \\
& 05*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15* \\
& m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n \\
& ^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 7 \\
& 35*m^3*n^3 + 175*m^4*n^2 + 1))/(7*m + 28*n + 168*m*n + 1610*m*n^2 + 420*m^2 \\
& *n + 7840*m*n^3 + 560*m^3*n + 20307*m*n^4 + 420*m^4*n + 26264*m*n^5 + 168*m \\
& ^5*n + 13068*m*n^6 + 28*m^6*n + 21*m^2 + 35*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + \\
& m^7 + 322*n^2 + 1960*n^3 + 6769*n^4 + 13132*n^5 + 13068*n^6 + 5040*n^7 + 3 \\
& 220*m^2*n^2 + 11760*m^2*n^3 + 3220*m^3*n^2 + 20307*m^2*n^4 + 7840*m^3*n^3 + \\
& 1610*m^4*n^2 + 13132*m^2*n^5 + 6769*m^3*n^4 + 1960*m^4*n^3 + 322*m^5*n^2 + \\
& 1) + (3*a*c*x*x^{(2*n)}*(e*x)^m*(A*a^2*d^2 + A*b^2*c^2 + B*a*b*c^2 + B*a^2*c \\
& *d + 3*A*a*b*c*d)*(6*m + 26*n + 130*m*n + 1080*m*n^2 + 260*m^2*n + 4260*m*n \\
& ^3 + 260*m^3*n + 7858*m*n^4 + 130*m^4*n + 5274*m*n^5 + 26*m^5*n + 15*m^2 + \\
& 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 270*n^2 + 1420*n^3 + 3929*n^4 + 5274*n^5 + \\
& 2520*n^6 + 1620*m^2*n^2 + 4260*m^2*n^3 + 1080*m^3*n^2 + 3929*m^2*n^4 + 1420 \\
& *m^3*n^3 + 270*m^4*n^2 + 1))/(7*m + 28*n + 168*m*n + 1610*m*n^2 + 420*m^2*n \\
& + 7840*m*n^3 + 560*m^3*n + 20307*m*n^4 + 420*m^4*n + 26264*m*n^5 + 168*m^5 \\
& *n + 13068*m*n^6 + 28*m^6*n + 21*m^2 + 35*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + m \\
& ^7 + 322*n^2 + 1960*n^3 + 6769*n^4 + 13132*n^5 + 13068*n^6 + 5040*n^7 + 322 \\
& 0*m^2*n^2 + 11760*m^2*n^3 + 3220*m^3*n^2 + 20307*m^2*n^4 + 7840*m^3*n^3 + 1 \\
& 610*m^4*n^2 + 13132*m^2*n^5 + 6769*m^3*n^4 + 1960*m^4*n^3 + 322*m^5*n^2 + 1
\end{aligned}$$

$$\begin{aligned}
& ) + (3*b*d*x*x^{(5*n)}*(e*x)^m*(B*a^2*d^2 + B*b^2*c^2 + A*a*b*d^2 + A*b^2*c*d \\
& + 3*B*a*b*c*d)*(6*m + 23*n + 115*m*n + 828*m*n^2 + 230*m^2*n + 2775*m*n^3 \\
& + 230*m^3*n + 4288*m*n^4 + 115*m^4*n + 2412*m*n^5 + 23*m^5*n + 15*m^2 + 20* \\
& m^3 + 15*m^4 + 6*m^5 + m^6 + 207*n^2 + 925*n^3 + 2144*n^4 + 2412*n^5 + 1008 \\
& *n^6 + 1242*m^2*n^2 + 2775*m^2*n^3 + 828*m^3*n^2 + 2144*m^2*n^4 + 925*m^3*n \\
& ^3 + 207*m^4*n^2 + 1))/((7*m + 28*n + 168*m*n + 1610*m*n^2 + 420*m^2*n + 784 \\
& 0*m*n^3 + 560*m^3*n + 20307*m*n^4 + 420*m^4*n + 26264*m*n^5 + 168*m^5*n + 1 \\
& 3068*m*n^6 + 28*m^6*n + 21*m^2 + 35*m^3 + 35*m^4 + 21*m^5 + 7*m^6 + m^7 + 3 \\
& 22*n^2 + 1960*n^3 + 6769*n^4 + 13132*n^5 + 13068*n^6 + 5040*n^7 + 3220*m^2* \\
& n^2 + 11760*m^2*n^3 + 3220*m^3*n^2 + 20307*m^2*n^4 + 7840*m^3*n^3 + 1610*m^ \\
& 4*n^2 + 13132*m^2*n^5 + 6769*m^3*n^4 + 1960*m^4*n^3 + 322*m^5*n^2 + 1) + (b \\
& ^2*d^2*x*x^{(6*n)}*(e*x)^m*(A*b*d + 3*B*a*d + 3*B\dots
\end{aligned}$$

### 3.16 $\int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=310

$$\frac{ac^2(2Abc + aBc + 3aAd)x^{1+n}(ex)^m}{1 + m + n} + \frac{c(aBc(2bc + 3ad) + A(b^2c^2 + 6abcd + 3a^2d^2))x^{1+2n}(ex)^m}{1 + m + 2n} + \frac{(6abcd(Bc + Ad) + A^2b^2c^2 + 6a^2cd^2)x^{1+3n}(ex)^m}{1 + m + 3n} + \frac{(d^2a^2Bd^2 + 3b^2c^2(A*d + B*c) + 2a*b*d*(A*d + 3*B*c))x^{1+4n}(ex)^m}{1 + m + 4n} + \frac{(b^2*d^2*(3*b*B*c + A*b*d + 2*a*B*d))x^{1+5n}(ex)^m}{1 + m + 5n} + \frac{(b^2*B*d^3)x^{1+6n}(ex)^m}{1 + m + 6n} + \frac{a^2*A*c^3*(ex)^{1+m}}{e*(1+m)}$$

[Out]  $a*c^2*(3*A*a*d+2*A*b*c+B*a*c)*x^{(1+n)}*(e*x)^m/(1+m+n)+c*(a*B*c*(3*a*d+2*b*c)+A*(3*a^2*d^2+6*a*b*c*d+b^2*c^2))*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+(6*a*b*c*d*(A*d+B*c)+a^2*d^2*(A*d+3*B*c)+b^2*c^2*(3*A*d+B*c))*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+d*(a^2*B*d^2+3*b^2*c*(A*d+B*c)+2*a*b*d*(A*d+3*B*c))*x^{(1+4*n)}*(e*x)^m/(1+m+4*n)+b*d^2*(A*b*d+2*B*a*d+3*B*b*c)*x^{(1+5*n)}*(e*x)^m/(1+m+5*n)+b^2*B*d^3*x^{(1+6*n)}*(e*x)^m/(1+m+6*n)+a^2*A*c^3*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.28, antiderivative size = 310, normalized size of antiderivative = 1.00, number of steps used = 14, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {584, 20, 30}

$$\frac{c^{2m+1}(ex)^m (A(3a^2d^2 + 6abcd + b^2c^2) + aBc(3ad + 2bc))}{m + 2n + 1} + \frac{c^{2m+1}(ex)^m (a^2d^2(Ad + 3Bc) + 6abcd(Ad + Bc) + b^2c^2(3Ad + Bc))}{m + 3n + 1} + \frac{d^{2m+1}(ex)^m (a^2Bd^2 + 2abd(Ad + 3Bc) + 3b^2c(Ad + Bc))}{m + 4n + 1} + \frac{a^2A^2c^{2m+1}}{e(m+1)} + \frac{a^{2m+1}(ex)^m (3aAd + aBc + 2Abc)}{m + n + 1} + \frac{bd^{2m+1}(ex)^m (2aBd + Ad + 3bBc)}{m + 5n + 1} + \frac{b^2Bd^2c^{2m+1}(ex)^m}{m + 6n + 1}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(a + b*x^n)^2*(A + B*x^n)*(c + d*x^n)^3,x]$

[Out]  $(a*c^2*(2*A*b*c + a*B*c + 3*a*A*d)*x^{(1 + n)}*(e*x)^m)/(1 + m + n) + (c*(a*B*c*(2*b*c + 3*a*d) + A*(b^2*c^2 + 6*a*b*c*d + 3*a^2*d^2))*x^{(1 + 2*n)}*(e*x)^m)/(1 + m + 2*n) + ((6*a*b*c*d*(B*c + A*d) + a^2*d^2*(3*B*c + A*d) + b^2*c^2*(B*c + 3*A*d))*x^{(1 + 3*n)}*(e*x)^m)/(1 + m + 3*n) + (d*(a^2*B*d^2 + 3*b^2*c*(B*c + A*d) + 2*a*b*d*(3*B*c + A*d))*x^{(1 + 4*n)}*(e*x)^m)/(1 + m + 4*n) + (b*d^2*(3*b*B*c + A*b*d + 2*a*B*d))*x^{(1 + 5*n)}*(e*x)^m/(1 + m + 5*n) + (b^2*B*d^3*x^{(1 + 6*n)}*(e*x)^m)/(1 + m + 6*n) + (a^2*A*c^3*(e*x)^{(1 + m)})/(e*(1 + m))$

**Rule 20**

$\text{Int}[(u_.)*((a_.)*(v_.))^{(m_.)}*((b_.)*(v_.))^{(n_.)}, x\_Symbol] \rightarrow \text{Dist}[b^{\text{IntPart}[n]}*((b*v)^{\text{FracPart}[n]}/(a^{\text{IntPart}[n]}*(a*v)^{\text{FracPart}[n]})), \text{Int}[u*(a*v)^{(m+n)}, x], x] /;$  FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m + n]

**Rule 30**

$\text{Int}[(x_.)^{(m_.)}, x\_Symbol] \rightarrow \text{Simp}[x^{(m+1)}/(m+1), x] /;$  FreeQ[m, x] && N eQ[m, -1]

**Rule 584**

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] :> Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^2 (A + Bx^n) (c + dx^n)^3 dx &= \int (a^2 Ac^3 (ex)^m + ac^2(2Abc + aBc + 3aAd)x^n (ex)^m + c(aBc + aBc + 3aAd)x^{2n} (ex)^m + abcd(2bc + 3ad)x^{3n} (ex)^m + a^2 Bc^2 (ex)^m) dx \\ &= \frac{a^2 Ac^3 (ex)^{1+m}}{e(1+m)} + (b^2 Bd^3) \int x^{6n} (ex)^m dx + (ac^2(2Abc + aBc + 3aAd)x^n (ex)^m) \\ &= \frac{a^2 Ac^3 (ex)^{1+m}}{e(1+m)} + (b^2 Bd^3 x^{-m} (ex)^m) \int x^{m+6n} dx + (ac^2(2Abc + aBc + 3aAd)x^n (ex)^m) \\ &= \frac{ac^2(2Abc + aBc + 3aAd)x^{1+n} (ex)^m}{1+m+n} + \frac{c(aBc(2bc + 3ad) + a^2 Bc^2)}{1+m+n} \end{aligned}$$

**Mathematica [A]**

time = 1.36, size = 265, normalized size = 0.85

$$x(ex)^m \left( \frac{a^2 Ac^3}{1+m} + \frac{ac^2(2Abc + aBc + 3aAd)x^n}{1+m+n} + \frac{c(aBc(2bc + 3ad) + a^2 Bc^2 + 6abcd + 3a^2 d^2)x^{2n}}{1+m+2n} + \frac{(6abcd(Bc + Ad) + a^2 d^2(3Bc + Ad) + b^2 c^2(Bc + 3Ad))x^{3n}}{1+m+3n} + \frac{d(a^2 Bd^2 + 3b^2 c(Bc + Ad) + 2abd(3Bc + Ad))x^{4n}}{1+m+4n} + \frac{bd^2(3bBc + Abd + 2aBd)x^{5n}}{1+m+5n} + \frac{b^2 Bd^2 x^{6n}}{1+m+6n} \right)$$

Antiderivative was successfully verified.

[In] Integrate[(e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out] x\*(e\*x)^m\*((a^2\*A\*c^3)/(1+m) + (a\*c^2\*(2\*A\*b\*c + a\*B\*c + 3\*a\*A\*d)\*x^n)/(1+m+n) + (c\*(a\*B\*c\*(2\*b\*c + 3\*a\*d) + A\*(b^2\*c^2 + 6\*a\*b\*c\*d + 3\*a^2\*d^2))\*x^(2\*n))/(1+m+2\*n) + ((6\*a\*b\*c\*d\*(B\*c + A\*d) + a^2\*d^2\*(3\*B\*c + A\*d) + b^2\*c^2\*(B\*c + 3\*A\*d))\*x^(3\*n))/(1+m+3\*n) + (d\*(a^2\*B\*d^2 + 3\*b^2\*c\*(B\*c + A\*d) + 2\*a\*b\*d\*(3\*B\*c + A\*d))\*x^(4\*n))/(1+m+4\*n) + (b\*d^2\*(3\*b\*B\*c + A\*b\*d + 2\*a\*B\*d)\*x^(5\*n))/(1+m+5\*n) + (b^2\*B\*d^3\*x^(6\*n))/(1+m+6\*n))

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.50, size = 11389, normalized size = 36.74

method	result	size
risch	Expression too large to display	11389

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)\*(c+d\*x^n)^3,x,method=\_RETURNVERBOSE)

[Out] result too large to display

**Maxima** [B] Leaf count of result is larger than twice the leaf count of optimal. 702 vs.  $2(316) = 632$ .

time = 0.43, size = 702, normalized size = 2.26

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="maxima")`

[Out]  $(x^m e^{(m+1)A a^2 c^3 e^{-1}} / (m+1) + B b^2 d^3 x^m e^{(m \log(x) + 6n \log(x) + m)} / (m + 6n + 1) + 3 B b^2 c^2 d^2 x^m e^{(m \log(x) + 5n \log(x) + m)} / (m + 5n + 1) + 2 B a b d^3 x^m e^{(m \log(x) + 5n \log(x) + m)} / (m + 5n + 1) + A b^2 d^3 x^m e^{(m \log(x) + 5n \log(x) + m)} / (m + 5n + 1) + 3 B b^2 c^2 d^2 x^m e^{(m \log(x) + 4n \log(x) + m)} / (m + 4n + 1) + 6 B a a b c d^2 x^m e^{(m \log(x) + 4n \log(x) + m)} / (m + 4n + 1) + 3 A a b^2 c d^2 x^m e^{(m \log(x) + 4n \log(x) + m)} / (m + 4n + 1) + B a^2 d^3 x^m e^{(m \log(x) + 4n \log(x) + m)} / (m + 4n + 1) + 2 A a b d^3 x^m e^{(m \log(x) + 4n \log(x) + m)} / (m + 4n + 1) + B b^2 c^3 x^m e^{(m \log(x) + 3n \log(x) + m)} / (m + 3n + 1) + 6 B a a b c^2 d x^m e^{(m \log(x) + 3n \log(x) + m)} / (m + 3n + 1) + 3 A a b^2 c^2 d^2 x^m e^{(m \log(x) + 3n \log(x) + m)} / (m + 3n + 1) + 3 B a^2 c d^2 x^m e^{(m \log(x) + 3n \log(x) + m)} / (m + 3n + 1) + 6 A a a b c d^2 x^m e^{(m \log(x) + 3n \log(x) + m)} / (m + 3n + 1) + A a^2 d^3 x^m e^{(m \log(x) + 3n \log(x) + m)} / (m + 3n + 1) + 2 B a a b c^3 x^m e^{(m \log(x) + 2n \log(x) + m)} / (m + 2n + 1) + A b^2 c^3 x^m e^{(m \log(x) + 2n \log(x) + m)} / (m + 2n + 1) + 3 B a^2 c^2 d^2 x^m e^{(m \log(x) + 2n \log(x) + m)} / (m + 2n + 1) + 6 A a a b c^2 d^2 x^m e^{(m \log(x) + 2n \log(x) + m)} / (m + 2n + 1) + 3 A a^2 c d^2 x^m e^{(m \log(x) + 2n \log(x) + m)} / (m + 2n + 1) + B a^2 c^3 x^m e^{(m \log(x) + n \log(x) + m)} / (m + n + 1) + 2 A a a b c^3 x^m e^{(m \log(x) + n \log(x) + m)} / (m + n + 1) + 3 A a^2 c^2 d^2 x^m e^{(m \log(x) + n \log(x) + m)} / (m + n + 1)$

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 6536 vs.  $2(316) = 632$ .

time = 1.84, size = 6536, normalized size = 21.08

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="fricas")`

[Out]  $((B b^2 d^3 m^6 + 6 B b^2 d^3 m^5 + 15 B b^2 d^3 m^4 + 20 B b^2 d^3 m^3 + 15 B b^2 d^3 m^2 + 6 B b^2 d^3 m + B b^2 d^3 + 120 (B b^2 d^3 m + B b^2 d^3) n^5 + 274 (B b^2 d^3 m^2 + 2 B b^2 d^3 m + B b^2 d^3) n^4 + 225 (B b^2 d^3 m^3 + 3 B b^2 d^3 m^2 + 3 B b^2 d^3 m + B b^2 d^3) n^3 + 85 (B b^2 d^3 m^4 + 4 B b^2 d^3 m^3 + 6 B b^2 d^3 m^2 + 4 B b^2 d^3 m + B b^2 d^3) n^2 + 15 (B b^2 d^3 m^5 + 5 B b^2 d^3 m^4 + 10 B b^2 d^3 m^3 + 10 B b^2 d^3 m^2 + 5$



$$\begin{aligned}
& B*b^2*d^3*m + B*b^2*d^3)*n)*x*x^{(6*n)}*e^{(m*\log(x) + m) + ((3*B*b^2*c*d^2 + \\
& (2*B*a*b + A*b^2)*d^3)*m^6 + 3*B*b^2*c*d^2 + 6*(3*B*b^2*c*d^2 + (2*B*a*b + \\
& A*b^2)*d^3)*m^5 + 144*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3 + (3*B*b^2*c*d \\
& ^2 + (2*B*a*b + A*b^2)*d^3)*m)*n^5 + 15*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)* \\
& d^3)*m^4 + 324*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3 + (3*B*b^2*c*d^2 + (2 \\
& *B*a*b + A*b^2)*d^3)*m^2 + 2*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m)*n^4 \\
& + (2*B*a*b + A*b^2)*d^3 + 20*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m^3 + \\
& 260*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3 + (3*B*b^2*c*d^2 + (2*B*a*b + A \\
& *b^2)*d^3)*m^3 + 3*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m^2 + 3*(3*B*b^2 \\
& *c*d^2 + (2*B*a*b + A*b^2)*d^3)*m)*n^3 + 15*(3*B*b^2*c*d^2 + (2*B*a*b + A*b \\
& ^2)*d^3)*m^2 + 95*(3*B*b^2*c*d^2 + (3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)* \\
& m^4 + (2*B*a*b + A*b^2)*d^3 + 4*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m^3 \\
& + 6*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m^2 + 4*(3*B*b^2*c*d^2 + (2*B* \\
& a*b + A*b^2)*d^3)*m)*n^2 + 6*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m + 16 \\
& *(3*B*b^2*c*d^2 + (3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m^5 + 5*(3*B*b^2*c \\
& *d^2 + (2*B*a*b + A*b^2)*d^3)*m^4 + (2*B*a*b + A*b^2)*d^3 + 10*(3*B*b^2*c* \\
& d^2 + (2*B*a*b + A*b^2)*d^3)*m^3 + 10*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^ \\
& 3)*m^2 + 5*(3*B*b^2*c*d^2 + (2*B*a*b + A*b^2)*d^3)*m)*n)*x*x^{(5*n)}*e^{(m*\log \\
& (x) + m) + ((3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)* \\
& d^3)*m^6 + 3*B*b^2*c^2*d + 6*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + ( \\
& B*a^2 + 2*A*a*b)*d^3)*m^5 + 180*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 \\
& + (B*a^2 + 2*A*a*b)*d^3 + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a \\
& ^2 + 2*A*a*b)*d^3)*m)*n^5 + 15*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + \\
& (B*a^2 + 2*A*a*b)*d^3)*m^4 + 396*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^ \\
& 2 + (B*a^2 + 2*A*a*b)*d^3 + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B \\
& *a^2 + 2*A*a*b)*d^3)*m^2 + 2*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + ( \\
& B*a^2 + 2*A*a*b)*d^3)*m)*n^4 + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b \\
& )*d^3 + 20*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d \\
& ^3)*m^3 + 307*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b \\
& )*d^3 + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3) \\
& *m^3 + 3*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^3 \\
& )*m^2 + 3*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b)*d^ \\
& 3)*m)*n^3 + 15*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a* \\
& b)*d^3)*m^2 + 107*(3*B*b^2*c^2*d + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d \\
& ^2 + (B*a^2 + 2*A*a*b)*d^3)*m^4 + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A* \\
& a*b)*d^3 + 4*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b) \\
& *d^3)*m^3 + 6*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a*b \\
& )*d^3)*m^2 + 4*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a* \\
& b)*d^3)*m)*n^2 + 6*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2* \\
& A*a*b)*d^3)*m + 17*(3*B*b^2*c^2*d + (3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c* \\
& d^2 + (B*a^2 + 2*A*a*b)*d^3)*m^5 + 5*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c \\
& *d^2 + (B*a^2 + 2*A*a*b)*d^3)*m^4 + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2* \\
& A*a*b)*d^3 + 10*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A*a \\
& *b)*d^3)*m^3 + 10*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*A \\
& *a*b)*d^3)*m^2 + 5*(3*B*b^2*c^2*d + 3*(2*B*a*b + A*b^2)*c*d^2 + (B*a^2 + 2*
\end{aligned}$$

```

A*a*b)*d^3)*m)*n)*x*x^(4*n)*e^(m*log(x) + m) + ((B*b^2*c^3 + A*a^2*d^3 + 3*
(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^6 + B*b^2*c^3 + A*a^
2*d^3 + 6*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2
*A*a*b)*c*d^2)*m^5 + 240*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d
+ 3*(B*a^2 + 2*A*a*b)*c*d^2 + (B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)
*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m)*n^5 + 15*(B*b^2*c^3 + A*a^2*d^3 + 3*
(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^4 + 508*(B*b^2*c^3 +
A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2 + (B*b^2
*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m
^2 + 2*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*
a*b)*c*d^2)*m)*n^4 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2
+ 20*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*
b)*c*d^2)*m^3 + 372*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*d + 3*
(B*a^2 + 2*A*a*b)*c*d^2 + (B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b + A*b^2)*c^2*
d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^3 + 3*(B*b^2*c^3 + A*a^2*d^3 + 3*(2*B*a*b
+ A*b^2)*c^2*d + 3*(B*a^2 + 2*A*a*b)*c*d^2)*m^2...

```

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)**2*(A+B*x**n)*(c+d*x**n)**3,x)
```

[Out] Timed out

**Giac** [B] Leaf count of result is larger than twice the leaf count of optimal. 15358 vs. 2(316) = 632.

time = 1.81, size = 15358, normalized size = 49.54

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="giac")
```

```
[Out] (B*b^2*d^3*m^6*x*x^m*x^(6*n)*e^m + 15*B*b^2*d^3*m^5*n*x*x^m*x^(6*n)*e^m + 8
5*B*b^2*d^3*m^4*n^2*x*x^m*x^(6*n)*e^m + 225*B*b^2*d^3*m^3*n^3*x*x^m*x^(6*n)
*e^m + 274*B*b^2*d^3*m^2*n^4*x*x^m*x^(6*n)*e^m + 120*B*b^2*d^3*m*n^5*x*x^m*x
^(6*n)*e^m + 3*B*b^2*c*d^2*m^6*x*x^m*x^(5*n)*e^m + 2*B*a*b*d^3*m^6*x*x^m*x
^(5*n)*e^m + A*b^2*d^3*m^6*x*x^m*x^(5*n)*e^m + 48*B*b^2*c*d^2*m^5*n*x*x^m*x
^(5*n)*e^m + 32*B*a*b*d^3*m^5*n*x*x^m*x^(5*n)*e^m + 16*A*b^2*d^3*m^5*n*x*x^
m*x^(5*n)*e^m + 285*B*b^2*c*d^2*m^4*n^2*x*x^m*x^(5*n)*e^m + 190*B*a*b*d^3*m
^4*n^2*x*x^m*x^(5*n)*e^m + 95*A*b^2*d^3*m^4*n^2*x*x^m*x^(5*n)*e^m + 780*B*b
^2*c*d^2*m^3*n^3*x*x^m*x^(5*n)*e^m + 520*B*a*b*d^3*m^3*n^3*x*x^m*x^(5*n)*e^
m + 260*A*b^2*d^3*m^3*n^3*x*x^m*x^(5*n)*e^m + 972*B*b^2*c*d^2*m^2*n^4*x*x^m
```

$$\begin{aligned}
& *x^{(5n)}e^m + 648*B*a*b*d^3m^2n^4*x*x^m*x^{(5n)}e^m + 324*A*b^2*d^3m^2* \\
& n^4*x*x^m*x^{(5n)}e^m + 432*B*b^2*c*d^2m^n^5*x*x^m*x^{(5n)}e^m + 288*B*a*b \\
& *d^3m^n^5*x*x^m*x^{(5n)}e^m + 144*A*b^2*d^3m^n^5*x*x^m*x^{(5n)}e^m + 3*B* \\
& b^2*c^2*d*m^6*x*x^m*x^{(4n)}e^m + 6*B*a*b*c*d^2m^6*x*x^m*x^{(4n)}e^m + 3*A \\
& *b^2*c*d^2m^6*x*x^m*x^{(4n)}e^m + B*a^2*d^3m^6*x*x^m*x^{(4n)}e^m + 2*A*a* \\
& b*d^3m^6*x*x^m*x^{(4n)}e^m + 51*B*b^2*c^2*d*m^5n*x*x^m*x^{(4n)}e^m + 102* \\
& B*a*b*c*d^2m^5n*x*x^m*x^{(4n)}e^m + 51*A*b^2*c*d^2m^5n*x*x^m*x^{(4n)}e^ \\
& m + 17*B*a^2*d^3m^5n*x*x^m*x^{(4n)}e^m + 34*A*a*b*d^3m^5n*x*x^m*x^{(4n)} \\
& *e^m + 321*B*b^2*c^2*d*m^4n^2*x*x^m*x^{(4n)}e^m + 642*B*a*b*c*d^2m^4n^2* \\
& x*x^m*x^{(4n)}e^m + 321*A*b^2*c*d^2m^4n^2*x*x^m*x^{(4n)}e^m + 107*B*a^2*d \\
& ^3m^4n^2*x*x^m*x^{(4n)}e^m + 214*A*a*b*d^3m^4n^2*x*x^m*x^{(4n)}e^m + 92 \\
& 1*B*b^2*c^2*d*m^3n^3*x*x^m*x^{(4n)}e^m + 1842*B*a*b*c*d^2m^3n^3*x*x^m*x^{(4n)} \\
& (4n)*e^m + 921*A*b^2*c*d^2m^3n^3*x*x^m*x^{(4n)}e^m + 307*B*a^2*d^3m^3n \\
& ^3*x*x^m*x^{(4n)}e^m + 614*A*a*b*d^3m^3n^3*x*x^m*x^{(4n)}e^m + 1188*B*b^2 \\
& *c^2*d*m^2n^4*x*x^m*x^{(4n)}e^m + 2376*B*a*b*c*d^2m^2n^4*x*x^m*x^{(4n)}e \\
& ^m + 1188*A*b^2*c*d^2m^2n^4*x*x^m*x^{(4n)}e^m + 396*B*a^2*d^3m^2n^4*x*x \\
& ^m*x^{(4n)}e^m + 792*A*a*b*d^3m^2n^4*x*x^m*x^{(4n)}e^m + 540*B*b^2*c^2*d* \\
& m^n^5*x*x^m*x^{(4n)}e^m + 1080*B*a*b*c*d^2m^n^5*x*x^m*x^{(4n)}e^m + 540*A* \\
& b^2*c*d^2m^n^5*x*x^m*x^{(4n)}e^m + 180*B*a^2*d^3m^n^5*x*x^m*x^{(4n)}e^m + \\
& 360*A*a*b*d^3m^n^5*x*x^m*x^{(4n)}e^m + B*b^2*c^3m^6*x*x^m*x^{(3n)}e^m + \\
& 6*B*a*b*c^2*d*m^6*x*x^m*x^{(3n)}e^m + 3*A*b^2*c^2*d*m^6*x*x^m*x^{(3n)}e^m + \\
& 3*B*a^2*c*d^2m^6*x*x^m*x^{(3n)}e^m + 6*A*a*b*c*d^2m^6*x*x^m*x^{(3n)}e^m \\
& + A*a^2*d^3m^6*x*x^m*x^{(3n)}e^m + 18*B*b^2*c^3m^5n*x*x^m*x^{(3n)}e^m + \\
& 108*B*a*b*c^2*d*m^5n*x*x^m*x^{(3n)}e^m + 54*A*b^2*c^2*d*m^5n*x*x^m*x^{(3n)} \\
& )e^m + 54*B*a^2*c*d^2m^5n*x*x^m*x^{(3n)}e^m + 108*A*a*b*c*d^2m^5n*x*x^ \\
& m*x^{(3n)}e^m + 18*A*a^2*d^3m^5n*x*x^m*x^{(3n)}e^m + 121*B*b^2*c^3m^4n^ \\
& 2*x*x^m*x^{(3n)}e^m + 726*B*a*b*c^2*d*m^4n^2*x*x^m*x^{(3n)}e^m + 363*A*b^2 \\
& *c^2*d*m^4n^2*x*x^m*x^{(3n)}e^m + 363*B*a^2*c*d^2m^4n^2*x*x^m*x^{(3n)}e^ \\
& m + 726*A*a*b*c*d^2m^4n^2*x*x^m*x^{(3n)}e^m + 121*A*a^2*d^3m^4n^2*x*x^ \\
& *x^{(3n)}e^m + 372*B*b^2*c^3m^3n^3*x*x^m*x^{(3n)}e^m + 2232*B*a*b*c^2*d*m \\
& ^3n^3*x*x^m*x^{(3n)}e^m + 1116*A*b^2*c^2*d*m^3n^3*x*x^m*x^{(3n)}e^m + 111 \\
& 6*B*a^2*c*d^2m^3n^3*x*x^m*x^{(3n)}e^m + 2232*A*a*b*c*d^2m^3n^3*x*x^m*x^{(3n)} \\
& (3n)*e^m + 372*A*a^2*d^3m^3n^3*x*x^m*x^{(3n)}e^m + 508*B*b^2*c^3m^2n^4 \\
& *x*x^m*x^{(3n)}e^m + 3048*B*a*b*c^2*d*m^2n^4*x*x^m*x^{(3n)}e^m + 1524*A*b^ \\
& 2*c^2*d*m^2n^4*x*x^m*x^{(3n)}e^m + 1524*B*a^2*c*d^2m^2n^4*x*x^m*x^{(3n)}* \\
& e^m + 3048*A*a*b*c*d^2m^2n^4*x*x^m*x^{(3n)}e^m + 508*A*a^2*d^3m^2n^4*x* \\
& x^m*x^{(3n)}e^m + 240*B*b^2*c^3m^n^5*x*x^m*x^{(3n)}e^m + 1440*B*a*b*c^2*d* \\
& m^n^5*x*x^m*x^{(3n)}e^m + 720*A*b^2*c^2*d*m^n^5*x*x^m*x^{(3n)}e^m + 720*B*a \\
& ^2*c*d^2m^n^5*x*x^m*x^{(3n)}e^m + 1440*A*a*b*c*d^2m^n^5*x*x^m*x^{(3n)}e^m \\
& + 240*A*a^2*d^3m^n^5*x*x^m*x^{(3n)}e^m + 2*B*a*b*c^3m^6*x*x^m*x^{(2n)}e^ \\
& m + A*b^2*c^3m^6*x*x^m*x^{(2n)}e^m + 3*B*a^2*c^2*d*m^6*x*x^m*x^{(2n)}e^m + \\
& 6*A*a*b*c^2*d*m^6*x*x^m*x^{(2n)}e^m + 3*A*a^2*c*d^2m^6*x*x^m*x^{(2n)}e^m \\
& + 38*B*a*b*c^3m^5n*x*x^m*x^{(2n)}e^m + 19*A*b^2*c^3m^5n*x*x^m*x^{(2n)}e \\
& ^m + 57*B*a^2*c^2*d*m^5n*x*x^m*x^{(2n)}e^m + 114*A*a*b*c^2*d*m^5n*x*x^m*x \\
& ^{(2n)}e^m + 57*A*a^2*c*d^2m^5n*x*x^m*x^{(2n)}e^m + 274*B*a*b*c^3m^4n^2
\end{aligned}$$

```

*x*x^m*x^(2*n)*e^m + 137*A*b^2*c^3*m^4*n^2*x*x^m*x^(2*n)*e^m + 411*B*a^2*c^
2*d*m^4*n^2*x*x^m*x^(2*n)*e^m + 822*A*a*b*c^2*d*m^4*n^2*x*x^m*x^(2*n)*e^m +
  411*A*a^2*c*d^2*m^4*n^2*x*x^m*x^(2*n)*e^m + 922*B*a*b*c^3*m^3*n^3*x*x^m*x^
(2*n)*e^m + 461*A*b^2*c^3*m^3*n^3*x*x^m*x^(2*n)*e^m + 1383*B*a^2*c^2*d*m^3*
n^3*x*x^m*x^(2*n)*e^m + 2766*A*a*b*c^2*d*m^3*n^3*x*x^m*x^(2*n)*e^m + 1383*A
*a^2*c*d^2*m^3*n^3*x*x^m*x^(2*n)*e^m + 1404*B*a*b*c^3*m^2*n^4*x*x^m*x^(2*n)
*e^m + 702*A*b^2*c^3*m^2*n^4*x*x^m*x^(2*n)*e^m + 2106*B*a^2*c^2*d*m^2*n^4*x
*x^m*x^(2*n)*e^m + 4212*A*a*b*c^2*d*m^2*n^4*x*x^m*x^(2*n)*e^m + 2106*A*a^2*
c*d^2*m^2*n^4*x*x^m*x^(2*n)*e^m + 720*B*a*b*c^3*m*n^5*x*x^m*x^(2*n)*e^m + 3
60*A*b^2*c^3*m*n^5*x*x^m*x^(2*n)*e^m + 1080*B*a^2*c^2*d*m*n^5*x*x^m*x^(2*n)
*e^m + 2160*A*a*b*c^2*d*m*n^5*x*x^m*x^(2*n)*e^m + 1080*A*a^2*c*d^2*m*n^5*x*
x^m*x^(2*n)*e^m + B*a^2*c^3*m^6*x*x^m*x^n*e^m + ...

```

**Mupad [B]**

time = 6.41, size = 1882, normalized size = 6.07

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)^2*(c + d*x^n)^3, x)$

[Out]  $(x*x^{(3*n)}*(e*x)^m*(A*a^2*d^3 + B*b^2*c^3 + 3*A*b^2*c^2*d + 3*B*a^2*c*d^2 + 6*A*a*b*c*d^2 + 6*B*a*b*c^2*d)*(5*m + 18*n + 72*m*n + 363*m*n^2 + 108*m^2*n + 744*m*n^3 + 72*m^3*n + 508*m*n^4 + 18*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 121*n^2 + 372*n^3 + 508*n^4 + 240*n^5 + 363*m^2*n^2 + 372*m^2*n^3 + 121*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (A*a^2*c^3*x*(e*x)^m)/(m + 1) + (c*x*x^{(2*n)}*(e*x)^m*(3*A*a^2*d^2 + A*b^2*c^2 + 2*B*a*b*c^2 + 3*B*a^2*c*d + 6*A*a*b*c*d)*(5*m + 19*n + 76*m*n + 411*m*n^2 + 114*m^2*n + 922*m*n^3 + 76*m^3*n + 702*m*n^4 + 19*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 137*n^2 + 461*n^3 + 702*n^4 + 360*n^5 + 411*m^2*n^2 + 461*m^2*n^3 + 137*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (d*x*x^{(4*n)}*(e*x)^m*(B*a^2*d^2 + 3*B*b^2*c^2 + 2*A*a*b*d^2 + 3*A*b^2*c*d + 6*B*a*b*c*d)*(5*m + 17*n + 68*m*n + 321*m*n^2 + 102*m^2*n + 614*m*n^3 + 68*m^3*n + 396*m*n^4 + 17*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 107*n^2 + 307*n^3 + 396*n^4 + 180*n^5 + 321*m^2*n^2 + 307*m^2*n^3 + 107*m^3*n^2 + 1))/(6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m$

$$\begin{aligned}
&^2n^3 + 700m^3n^2 + 1624m^2n^4 + 735m^3n^3 + 175m^4n^2 + 1) + (a*c \\
&^2*x*x^n*(e*x)^m*(3*A*a*d + 2*A*b*c + B*a*c)*(5*m + 20*n + 80*m*n + 465*m*n \\
&^2 + 120*m^2*n + 1160*m*n^3 + 80*m^3*n + 1044*m*n^4 + 20*m^4*n + 10*m^2 + 1 \\
&0*m^3 + 5*m^4 + m^5 + 155*n^2 + 580*n^3 + 1044*n^4 + 720*n^5 + 465*m^2*n^2 \\
&+ 580*m^2*n^3 + 155*m^3*n^2 + 1))/ (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m \\
&^2*n + 2205*m*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^ \\
&5*n + 15*m^2 + 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 \\
&+ 1764*n^5 + 720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^ \\
&2*n^4 + 735*m^3*n^3 + 175*m^4*n^2 + 1) + (b*d^2*x*x^(5*n)*(e*x)^m*(A*b*d + \\
&2*B*a*d + 3*B*b*c)*(5*m + 16*n + 64*m*n + 285*m*n^2 + 96*m^2*n + 520*m*n^3 \\
&+ 64*m^3*n + 324*m*n^4 + 16*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 95*n^2 \\
&+ 260*n^3 + 324*n^4 + 144*n^5 + 285*m^2*n^2 + 260*m^2*n^3 + 95*m^3*n^2 + 1) \\
&))/ (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m*n^3 + 210*m^3*n + \\
&3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 + 20*m^3 + 15*m^4 + \\
&6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + 720*n^6 + 1050*m^2 \\
&*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m^3*n^3 + 175*m^4*n^ \\
&2 + 1) + (B*b^2*d^3*x*x^(6*n)*(e*x)^m*(5*m + 15*n + 60*m*n + 255*m*n^2 + 90 \\
&*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5* \\
&m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^ \\
&3 + 85*m^3*n^2 + 1))/ (6*m + 21*n + 105*m*n + 700*m*n^2 + 210*m^2*n + 2205*m \\
&*n^3 + 210*m^3*n + 3248*m*n^4 + 105*m^4*n + 1764*m*n^5 + 21*m^5*n + 15*m^2 \\
&+ 20*m^3 + 15*m^4 + 6*m^5 + m^6 + 175*n^2 + 735*n^3 + 1624*n^4 + 1764*n^5 + \\
&720*n^6 + 1050*m^2*n^2 + 2205*m^2*n^3 + 700*m^3*n^2 + 1624*m^2*n^4 + 735*m \\
&^3*n^3 + 175*m^4*n^2 + 1)
\end{aligned}$$

### 3.17 $\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=210

$$\frac{c^2(abc + aBc + 3aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{c(3ad(Bc + Ad) + bc(Bc + 3Ad))x^{1+2n}(ex)^m}{1+m+2n} + \frac{d(3bc(Bc + Ad) + ad(3Bc + Ad))x^{1+3n}(ex)^m}{1+m+3n} + \frac{d^2(3b^2c + a^2d)(ex)^m}{1+m+4n} + \frac{d^3b^2c^2(ex)^m}{1+m+5n} + \frac{a^3c^3(ex)^{m+1}}{e(m+1)}$$

[Out]  $c^2(3A^2a^2d + 3A^2b^2c + 3A^2a^2c) * x^{(1+n)} * (ex)^m / (1+m+n) + c(3a^2d(A^2d + B^2c) + b^2c(3A^2d + B^2c)) * x^{(1+2n)} * (ex)^m / (1+m+2n) + d(3b^2c(A^2d + B^2c) + a^2d(A^2d + 3B^2c)) * x^{(1+3n)} * (ex)^m / (1+m+3n) + d^2(A^2b^2d + B^2a^2d + 3B^2b^2c) * x^{(1+4n)} * (ex)^m / (1+m+4n) + b^2B^2d^3 * x^{(1+5n)} * (ex)^m / (1+m+5n) + a^3A^2c^3 * (ex)^{(1+m)} / e / (1+m)$

**Rubi [A]**

time = 0.17, antiderivative size = 210, normalized size of antiderivative = 1.00, number of steps used = 12, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {584, 20, 30}

$$\frac{c^2 x^{n+1} (ex)^m (3aAd + aBc + Abc)}{m+n+1} + \frac{d^2 x^{4n+1} (ex)^m (aBd + Abd + 3bBc)}{m+4n+1} + \frac{cx^{2n+1} (ex)^m (3ad(Ad+Bc) + bc(3Ad+Bc))}{m+2n+1} + \frac{dx^{3n+1} (ex)^m (ad(Ad+3Bc) + 3bc(Ad+Bc))}{m+3n+1} + \frac{aAc^3 (ex)^{m+1}}{e(m+1)} + \frac{bBd^3 x^{5n+1} (ex)^m}{m+5n+1}$$

Antiderivative was successfully verified.

[In] `Int[(ex)^m*(a + b*x^n)*(A + B*x^n)*(c + d*x^n)^3,x]`

[Out]  $(c^2(A^2b^2c + a^2B^2c + 3a^2A^2d)) * x^{(1+n)} * (ex)^m / (1+m+n) + (c(3a^2d(B^2c + A^2d) + b^2c(B^2c + 3A^2d))) * x^{(1+2n)} * (ex)^m / (1+m+2n) + (d(3b^2c(B^2c + A^2d) + a^2d(3B^2c + A^2d))) * x^{(1+3n)} * (ex)^m / (1+m+3n) + (d^2(3b^2B^2c + A^2b^2d + a^2B^2d)) * x^{(1+4n)} * (ex)^m / (1+m+4n) + (b^2B^2d^3 * x^{(1+5n)} * (ex)^m) / (1+m+5n) + (a^3A^2c^3 * (ex)^{(1+m)}) / (e * (1+m))$

**Rule 20**

`Int[(u_.)*((a_.)*(v_))^(m_.)*((b_.)*(v_))^(n_), x_Symbol] := Dist[b^IntPart[n]*((b*v)^FracPart[n]/(a^IntPart[n]*(a*v)^FracPart[n])), Int[u*(a*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]`

**Rule 30**

`Int[(x_)^(m_.), x_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]`

**Rule 584**

`Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]`

Rubi steps

$$\begin{aligned}
\int (ex)^m (a + bx^n) (A + Bx^n) (c + dx^n)^3 dx &= \int (aAc^3(ex)^m + c^2(abc + aBc + 3aAd)x^n(ex)^m + c(3ad(Bc + Ad) + bcE)x^{2n}(ex)^m \\
&= \frac{aAc^3(ex)^{1+m}}{e(1+m)} + (bBd^3) \int x^{5n}(ex)^m dx + (c^2(abc + aBc + 3aAd)x^n(ex)^m) \int x^{m+5n} dx + (c(3ad(Bc + Ad) + bcE)x^{2n}(ex)^m) \int x^{m+5n} dx \\
&= \frac{aAc^3(ex)^{1+m}}{e(1+m)} + (bBd^3 x^{-m}(ex)^m) \int x^{m+5n} dx + (c^2(abc + aBc + 3aAd)x^n(ex)^m) \int x^{m+5n} dx + (c(3ad(Bc + Ad) + bcE)x^{2n}(ex)^m) \int x^{m+5n} dx \\
&= \frac{c^2(abc + aBc + 3aAd)x^{1+n}(ex)^m}{1+m+n} + \frac{c(3ad(Bc + Ad) + bcE)x^{1+n}(ex)^m}{1+m+n}
\end{aligned}$$

Mathematica [A]

time = 0.61, size = 172, normalized size = 0.82

$$x(ex)^m \left( \frac{aAc^3}{1+m} + \frac{c^2(abc + aBc + 3aAd)x^n}{1+m+n} + \frac{c(3ad(Bc + Ad) + bcE)x^{2n}}{1+m+2n} + \frac{d(3bc(Bc + Ad) + ad(3Bc + Ad))x^{3n}}{1+m+3n} + \frac{d^2(3bBc + Abd + aBd)x^{4n}}{1+m+4n} + \frac{bBd^3x^{5n}}{1+m+5n} \right)$$

Antiderivative was successfully verified.

`[In] Integrate[(e*x)^m*(a + b*x^n)*(A + B*x^n)*(c + d*x^n)^3,x]`

```
[Out] x*(e*x)^m*((a*A*c^3)/(1+m) + (c^2*(A*b*c + a*B*c + 3*a*A*d)*x^n)/(1+m+n) + (c*(3*a*d*(B*c + A*d) + b*c*(B*c + 3*A*d))*x^(2*n))/(1+m+2*n) + (d*(3*b*c*(B*c + A*d) + a*d*(3*B*c + A*d))*x^(3*n))/(1+m+3*n) + (d^2*(3*b*B*c + A*b*d + a*B*d)*x^(4*n))/(1+m+4*n) + (b*B*d^3*x^(5*n))/(1+m+5*n))
```

Maple [C] Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.42, size = 4972, normalized size = 23.68

method	result	size
risch	Expression too large to display	4972

Verification of antiderivative is not currently implemented for this CAS.

`[In] int((e*x)^m*(a+b*x^n)*(A+B*x^n)*(c+d*x^n)^3,x,method=_RETURNVERBOSE)`

```
[Out] x*(15*A*a*c*d^2*(x^n)^2*m+39*A*a*c*d^2*(x^n)^2*n+56*A*b*c^3*m*n*x^n+15*A*b*c^2*d*(x^n)^2*m+39*A*b*c^2*d*(x^n)^2*n+156*B*a*c^2*d*m^3*n*(x^n)^2+531*B*a*c^2*d*m^2*n^2*(x^n)^2+642*B*a*c^2*d*m*n^3*(x^n)^2+642*A*a*c*d^2*m*n^3*(x^n)^2+156*A*b*c^2*d*m^3*n*(x^n)^2+156*A*a*c*d^2*m^3*n*(x^n)^2+531*A*a*c*d^2*m^2*n^2*(x^n)^2+156*A*b*c^2*d*m*n*(x^n)^2+180*A*a*c*d^2*n^4*(x^n)^2+72*A*a*d^3*m^2*n*(x^n)^3+147*A*a*d^3*m*n^2*(x^n)^3+14*A*b*c^3*m^4*n*x^n+71*A*b*c^3*m^3*n^2*x^n+154*A*b*c^3*m^2*n^3*x^n+120*A*a*c^3*n^5+14*A*b*c^3*x^n*n+5*B*a*c^3*x^n*m+14*B*a*c^3*x^n*n+x^n*c^3*A*b+x^n*c^3*B*a+10*B*b*d^3*m^4*n*(x^n)^5+
```

$35*B*b*d^3*m^3*n^2*(x^n)^5+50*B*b*d^3*m^2*n^3*(x^n)^5+11*B*a*d^3*m^4*n*(x^n)^4+41*B*a*d^3*m^3*n^2*(x^n)^4+61*B*a*d^3*m^2*n^3*(x^n)^4+30*B*a*d^3*m*n^4*(x^n)^4+3*B*b*c*d^2*m^5*(x^n)^4+40*B*b*d^3*m^3*n*(x^n)^5+105*B*b*d^3*m^2*n^2*(x^n)^5+100*B*b*d^3*m*n^3*(x^n)^5+A*a*c^3+120*A*b*c^3*m*n^4*x^n+15*A*b*c^2*d*m^4*(x^n)^2+180*A*b*c^2*d*n^4*(x^n)^2+123*B*a*d^3*m*n^2*(x^n)^4+13*B*b*c^3*m^4*n*(x^n)^2+59*B*b*c^3*m^3*n^2*(x^n)^2+56*B*a*c^3*m^3*n*x^n+84*B*a*c^3*m^2*n*x^n+213*B*a*c^3*m*n^2*x^n+30*B*a*c^2*d*m^2*(x^n)^2+177*B*a*c^2*d*n^2*(x^n)^2+120*B*a*c*d^2*n^4*(x^n)^3+5*A*a*c^3*m+15*A*a*c^3*n+10*B*b*d^3*m^2*(x^n)^5+35*B*b*d^3*n^2*(x^n)^5+10*A*a*d^3*m^3*(x^n)^3+78*A*a*d^3*n^3*(x^n)^3+A*b*c^3*m^5*x^n+10*A*b*d^3*m^2*(x^n)^4+41*A*b*d^3*n^2*(x^n)^4+B*a*c^3*m^5*x^n+10*B*a*d^3*m^2*(x^n)^4+41*B*a*d^3*n^2*(x^n)^4+5*B*b*c^3*m^4*(x^n)^2+3*(x^n)^3*B*b*c^2*d+3*(x^n)^2*A*a*c*d^2+3*(x^n)^2*d*c^2*A*b+3*(x^n)^2*d*c^2*B*a+3*x^n*A*a*c^2*d+120*A*b*c^3*n^4*x^n+59*B*b*c^3*n^2*(x^n)^2+10*A*b*c^3*m^2*x^n+71*A*b*c^3*n^2*x^n+10*B*a*c^3*m^2*x^n+71*B*a*c^3*n^2*x^n+5*B*b*c^3*(x^n)^2*m+107*B*b*c^3*n^3*(x^n)^2+5*A*a*d^3*(x^n)^3*m+12*A*a*d^3*(x^n)^3*n+10*A*b*c^3*m^3*x^n+154*A*b*c^3*n^3*x^n+10*B*a*c^3*m^3*x^n+154*B*a*c^3*n^3*x^n+10*B*b*c^3*m^2*(x^n)^2+5*B*a*c^3*m^4*x^n+120*B*a*c^3*n^4*x^n+60*A*a*c^3*m^3*n+255*A*a*c^3*m^2*n^2+450*A*a*c^3*m*n^3+90*A*a*c^3*m^2*n+255*A*a*c^3*m*n^2+60*A*a*c^3*m*n+B*b*c^3*m^5*(x^n)^2+5*A*b*d^3*(x^n)^4*m+120*B*b*c^2*d*n^4*(x^n)^3+30*B*b*c*d^2*m^3*(x^n)^4+183*B*b*c*d^2*n^3*(x^n)^4+66*B*a*d^3*m^2*n*(x^n)^4+A*a*c^3*m^5+5*A*a*c^3*m^4+274*A*a*c^3*n^4+10*A*a*c^3*m^3+225*A*a*c^3*n^3+10*A*a*c^3*m^2+85*A*a*c^3*n^2+321*B*a*c^2*d*n^3*(x^n)^2+30*B*a*c*d^2*m^2*(x^n)^3+147*B*a*c*d^2*n^2*(x^n)^3+78*B*b*c^3*m^2*n*(x^n)^2+177*B*b*c^3*m*n^2*(x^n)^2+B*b*d^3*(x^n)^5+A*b*d^3*(x^n)^4+B*a*d^3*(x^n)^4+A*a*d^3*(x^n)^3+B*b*c^3*(x^n)^2+13*B*b*c^3*(x^n)^2*n+5*A*b*c^3*x^n*m+48*A*a*d^3*m*n*(x^n)^3+56*A*b*c^3*m^3*n*x^n+213*A*b*c^3*m^2*n^2*x^n+308*A*b*c^3*m*n^3*x^n+30*A*b*c^2*d*m^3*(x^n)^2+12*A*a*d^3*m^4*n*(x^n)^3+49*A*a*d^3*m^3*n^2*(x^n)^3+78*A*a*d^3*m^2*n^3*(x^n)^3+40*A*a*d^3*m*n^4*(x^n)^3+3*A*b*c*d^2*m^5*(x^n)^3+24*B*b*d^3*m*n^4*(x^n)^5+11*A*b*d^3*m^4*n*(x^n)^4+40*B*b*d^3*m*n*(x^n)^5+3*A*a*c^2*d*m^5*x^n+15*A*a*c*d^2*m^4*(x^n)^2+234*A*b*c*d^2*n^3*(x^n)^3+44*A*b*d^3*m*n*(x^n)^4+14*B*a*c^3*m^4*n*x^n+71*B*a*c^3*m^3*n^2*x^n+154*B*a*c^3*m^2*n^3*x^n+120*B*a*c^3*m*n^4*x^n+15*B*a*c^2*d*m^4*(x^n)^2+180*B*a*c^2*d*n^4*(x^n)^2+30*B*a*c*d^2*m^3*(x^n)^3+234*B*a*c*d^2*n^3*(x^n)^3+36*B*a*c*d^2*(x^n)^3*n+52*B*b*c^3*m*n*(x^n)^2+15*B*b*c^2*d*(x^n)^3*m+36*B*b*c^2*d*(x^n)^3*n+30*A*a*c^2*d*m^2*x^n+213*A*a*c^2*d*n^2*x^n+15*B*b*c*d^2*(x^n)^4*m+33*B*b*c*d^2*(x^n)^4*n+30*A*a*c^2*d*m^3*x^n+462*A*a*c^2*d*n^3*x^n+30*A*a*c*d^2*m^2*(x^n)^2+41*A*b*d^3*m^3*n^2*(x^n)^4+61*A*b*d^3*m^2*n^3*(x^n)^4+30*A*b*d^3*m*n^4*(x^n)^4+56*B*a*c^3*m*n*x^n+15*B*a*c^2*d*(x^n)^2*m+39*B*a*c^2*d*(x^n)^2*n+15*A*a*c^2*d*x^n*m+42*A*a*c^2*d*x^n*n+105*B*b*d^3*m*n^2*(x^n)^5+3*A*a*c*d^2*m^5*(x^n)^2+48*A*a*d^3*m^3*n*(x^n)^3+147*A*a*d^3*m^2*n^2*(x^n)^3+147*B*a*c*d^2*m^3*n^2*(x^n)^3+234*B*a*c*d^2*m^2*n^3*(x^n)^3+120*B*a*c*d^2*m*n^4*(x^n)^3+36*B*b*c^2*d*m^4*n*(x^n)^3+147*B*b*c^2*d*m^3*n^2*(x^n)^3+177*A*b*c^2*d*n^2*(x^n)^2+15*A*b*c*d^2*(x^n)^3*m+36*A*b*c*d^2*(x^n)^3*n+144*A*b*c*d^2*m^3*n*(x^n)^3+441*A*b*c*d^2*m^2*n^2*(x^n)^3+468*A*b*c*d^2*m*n^3*(x^n)^3+39*B*a*c^2*d*m^4*n*(x^n)^2+369*B*b*c*d^2*m*n^2*(x^n)^4+42*A*a*c^2*d*m^4*n*x^n+$



$$\begin{aligned}
& 213*A*a*c^2*d*m^3*n^2*x^n+30*B*b*c^2*d*m^2*(x^n)^3+147*B*b*c^2*d*n^2*(x^n)^3 \\
& +156*A*a*d^3*m*n^3*(x^n)^3+3*A*b*c^2*d*m^5*(x^n)^2+15*A*b*c*d^2*m^4*(x^n)^3 \\
& +120*A*b*c*d^2*n^4*(x^n)^3+66*A*b*d^3*m^2*n*(x^n)^4+123*A*b*d^3*m*n^2*(x^n)^4 \\
& +3*B*a*c^2*d*m^5*(x^n)^2+15*B*a*c*d^2*m^4*(x^n)^3+30*A*b*c*d^2*m^3*(x^n)^3 \\
& +15*B*a*c*d^2*(x^n)^3+m+44*B*a*d^3*m*n*(x^n)^4+52*B*b*c^3*m^3*n*(x^n)^2+177 \\
& *B*b*c^3*m^2*n^2*(x^n)^2+214*B*b*c^3*m*n^3*(x^n)^2+30*B*b*c^2*d*m^3*(x^n)^3 \\
& +234*B*b*c^2*d*n^3*(x^n)^3+441*B*b*c^2*d*m^2*n^2*(x^n)^3+468*B*b*c^2*d*m*m \\
& n^3*(x^n)^3+198*B*b*c*d^2*m^2*n*(x^n)^4+213*B*a*c^3*m^2*n^2*x^n+107*B*b*c^3 \\
& *m^2*n^3*(x^n)^2+60*B*b*c^3*m*n^4*(x^n)^2+15*B*b*c^2*d*m^4*(x^n)^3+308*B*a \\
& c^3*m*n^3*x^n+30*B*a*c^2*d*m^3*(x^n)^2+11*A*b*d^3*(x^n)^4*n+177*A*a*c*d^2*n \\
& ^2*(x^n)^2+84*A*b*c^3*m^2*n*x^n+213*A*b*c^3*m*n^2*x^n+30*A*b*c^2*d*m^2*(x^n)^2 \\
& +321*A*b*c^2*d*n^3*(x^n)^2+30*A*b*c*d^2*m^2*(x^n)^3+147*A*b*c*d^2*n^2*(x^n)^3 \\
& +234*B*b*c^2*d*m^2*n^3*(x^n)^3+120*B*b*c^2*d*m*n^4*(x^n)^3+132*B*b*c*d^2 \\
& *m^3*n*(x^n)^4+369*B*b*c*d^2*m^2*n^2*(x^n)^4+\dots
\end{aligned}$$

**Maxima** [B] Leaf count of result is larger than twice the leaf count of optimal. 434 vs.  $2(215) = 430$ .

time = 0.36, size = 434, normalized size = 2.07

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Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="maxima")

[Out]  $(x*e)^{(m+1)}*A*a*c^3*e^{(-1)}/(m+1) + B*b*d^3*x*e^{(m*\log(x) + 5*n*\log(x) + m)}/(m+5*n+1) + 3*B*b*c*d^2*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m+4*n+1) + B*a*d^3*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m+4*n+1) + A*b*d^3*x*e^{(m*\log(x) + 4*n*\log(x) + m)}/(m+4*n+1) + 3*B*b*c^2*d*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m+3*n+1) + 3*B*a*c*d^2*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m+3*n+1) + 3*A*b*c*d^2*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m+3*n+1) + A*a*d^3*x*e^{(m*\log(x) + 3*n*\log(x) + m)}/(m+3*n+1) + B*b*c^3*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m+2*n+1) + 3*B*a*c^2*d*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m+2*n+1) + 3*A*b*c^2*d*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m+2*n+1) + 3*A*a*c*d^2*x*e^{(m*\log(x) + 2*n*\log(x) + m)}/(m+2*n+1) + B*a*c^3*x*e^{(m*\log(x) + n*\log(x) + m)}/(m+n+1) + A*b*c^3*x*e^{(m*\log(x) + n*\log(x) + m)}/(m+n+1) + 3*A*a*c^2*d*x*e^{(m*\log(x) + n*\log(x) + m)}/(m+n+1)$

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 2815 vs.  $2(215) = 430$ .

time = 1.33, size = 2815, normalized size = 13.40

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="fricas")

[Out]  $((B*b*d^3*m^5 + 5*B*b*d^3*m^4 + 10*B*b*d^3*m^3 + 10*B*b*d^3*m^2 + 5*B*b*d^3*m + B*b*d^3 + 24*(B*b*d^3*m + B*b*d^3)*n^4 + 50*(B*b*d^3*m^2 + 2*B*b*d^3*m + B*b*d^3)*n^3 + 35*(B*b*d^3*m^3 + 3*B*b*d^3*m^2 + 3*B*b*d^3*m + B*b*d^3)*n^2 + 10*(B*b*d^3*m^4 + 4*B*b*d^3*m^3 + 6*B*b*d^3*m^2 + 4*B*b*d^3*m + B*b*d^3)*n)*x*x^(5*n)*e^(m*log(x) + m) + ((3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^5 + 3*B*b*c*d^2 + 5*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^4 + 30*(3*B*b*c*d^2 + (B*a + A*b)*d^3 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n^4 + (B*a + A*b)*d^3 + 10*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^3 + 61*(3*B*b*c*d^2 + (B*a + A*b)*d^3 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^2 + 2*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n^3 + 10*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^2 + 41*(3*B*b*c*d^2 + (B*a + A*b)*d^3 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^3 + 3*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^2 + 3*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n^2 + 5*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m + 11*(3*B*b*c*d^2 + (3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^4 + (B*a + A*b)*d^3 + 4*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^3 + 6*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m^2 + 4*(3*B*b*c*d^2 + (B*a + A*b)*d^3)*m)*n)*x*x^(4*n)*e^(m*log(x) + m) + ((3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^5 + 3*B*b*c^2*d + A*a*d^3 + 5*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^4 + 40*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n^4 + 3*(B*a + A*b)*c*d^2 + 10*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^3 + 78*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^2 + 2*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n^3 + 10*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^2 + 49*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^3 + 3*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n^2 + 5*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m + 12*(3*B*b*c^2*d + A*a*d^3 + (3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^4 + 3*(B*a + A*b)*c*d^2 + 4*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^3 + 6*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m^2 + 4*(3*B*b*c^2*d + A*a*d^3 + 3*(B*a + A*b)*c*d^2)*m)*n)*x*x^(3*n)*e^(m*log(x) + m) + ((B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^5 + B*b*c^3 + 3*A*a*c*d^2 + 5*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^4 + 60*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d + (B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m)*n^4 + 3*(B*a + A*b)*c^2*d + 10*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^3 + 107*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d + (B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^2 + 2*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m)*n^3 + 10*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^2 + 59*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d + (B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^3 + 3*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^2 + 3*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m)*n^2 + 5*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m + 13*(B*b*c^3 + 3*A*a*c*d^2 + (B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^4 + 3*(B*a + A*b)*c^2*d + 4*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^3 + 6*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m^2 + 4*(B*b*c^3 + 3*A*a*c*d^2 + 3*(B*a + A*b)*c^2*d)*m)*n)*x*x^(2*n)*e^(m*log(x) + m) + ((3*A*a*c^2*d + (B*a + A*b)*c^3)*m^5 + 3*A*a*c^2*d + 5*(3*A*a*c$

$$\begin{aligned}
&^2*d + (B*a + A*b)*c^3)*m^4 + 120*(3*A*a*c^2*d + (B*a + A*b)*c^3 + (3*A*a*c \\
&^2*d + (B*a + A*b)*c^3)*m)*n^4 + (B*a + A*b)*c^3 + 10*(3*A*a*c^2*d + (B*a + \\
&A*b)*c^3)*m^3 + 154*(3*A*a*c^2*d + (B*a + A*b)*c^3 + (3*A*a*c^2*d + (B*a + \\
&A*b)*c^3)*m^2 + 2*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m)*n^3 + 10*(3*A*a*c^2*d \\
&+ (B*a + A*b)*c^3)*m^2 + 71*(3*A*a*c^2*d + (B*a + A*b)*c^3 + (3*A*a*c^2*d \\
&+ (B*a + A*b)*c^3)*m^3 + 3*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m^2 + 3*(3*A*a*c \\
&^2*d + (B*a + A*b)*c^3)*m)*n^2 + 5*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m + 14*( \\
&3*A*a*c^2*d + (3*A*a*c^2*d + (B*a + A*b)*c^3)*m^4 + (B*a + A*b)*c^3 + 4*(3* \\
&A*a*c^2*d + (B*a + A*b)*c^3)*m^3 + 6*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m^2 + \\
&4*(3*A*a*c^2*d + (B*a + A*b)*c^3)*m)*n)*x^n*e^{(m*\log(x) + m)} + (A*a*c^3*m \\
&^5 + 120*A*a*c^3*n^5 + 5*A*a*c^3*m^4 + 10*A*a*c^3*m^3 + 10*A*a*c^3*m^2 + 5* \\
&A*a*c^3*m + A*a*c^3 + 274*(A*a*c^3*m + A*a*c^3)*n^4 + 225*(A*a*c^3*m^2 + 2* \\
&A*a*c^3*m + A*a*c^3)*n^3 + 85*(A*a*c^3*m^3 + 3*A*a*c^3*m^2 + 3*A*a*c^3*m + \\
&A*a*c^3)*n^2 + 15*(A*a*c^3*m^4 + 4*A*a*c^3*m^3 + 6*A*a*c^3*m^2 + 4*A*a*c^3*m \\
&+ A*a*c^3)*n)*x*e^{(m*\log(x) + m)}/(m^6 + 120*(m + 1)*n^5 + 6*m^5 + 274*(m \\
&^2 + 2*m + 1)*n^4 + 15*m^4 + 225*(m^3 + 3*m^2 + 3*m + 1)*n^3 + 20*m^3 + 85* \\
&(m^4 + 4*m^3 + 6*m^2 + 4*m + 1)*n^2 + 15*m^2 + 15*(m^5 + 5*m^4 + 10*m^3 + 1 \\
&0*m^2 + 5*m + 1)*n + 6*m + 1)
\end{aligned}$$

**Sympy [B]** Leaf count of result is larger than twice the leaf count of optimal. 63250 vs. 2(206) = 412.

time = 180.15, size = 63250, normalized size = 301.19

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*3,x)

[Out] Piecewise(((A + B)\*(a + b)\*(c + d)\*\*3\*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A\*a\*c\*\*3\*log(x) + 3\*A\*a\*c\*\*2\*d\*x\*\*n/n + 3\*A\*a\*c\*d\*\*2\*x\*\*(2\*n)/(2\*n) + A\*a\*d\*\*3\*x\*\*(3\*n)/(3\*n) + A\*b\*c\*\*3\*x\*\*n/n + 3\*A\*b\*c\*\*2\*d\*x\*\*(2\*n)/(2\*n) + A\*b\*c\*d\*\*2\*x\*\*(3\*n)/n + A\*b\*d\*\*3\*x\*\*(4\*n)/(4\*n) + B\*a\*c\*\*3\*x\*\*n/n + 3\*B\*a\*c\*\*2\*d\*x\*\*(2\*n)/(2\*n) + B\*a\*c\*d\*\*2\*x\*\*(3\*n)/n + B\*a\*d\*\*3\*x\*\*(4\*n)/(4\*n) + B\*b\*c\*\*3\*x\*\*(2\*n)/(2\*n) + B\*b\*c\*\*2\*d\*x\*\*(3\*n)/n + 3\*B\*b\*c\*d\*\*2\*x\*\*(4\*n)/(4\*n) + B\*b\*d\*\*3\*x\*\*(5\*n)/(5\*n))/e, Eq(m, -1)), (A\*a\*c\*\*3\*Piecewise((-1/(5\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*a\*c\*\*2\*d\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*a\*c\*d\*\*2\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + A\*a\*d\*\*3\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + A\*b\*c\*\*3\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*b\*c\*\*2\*d\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*A\*b\*c\*d\*\*2\*Piecewise((-x\*\*(3\*n)/(2\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + A\*b\*d\*\*3\*Piecewise((-x\*\*(4\*n)/(n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + B\*a\*c\*\*3\*Piecewise((-x\*\*n/(4\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)), (log(x), True))/e + 3\*B\*a\*c\*\*2\*d\*Piecewise((-x\*\*(2\*n)/(3\*n\*(e\*x)\*\*(5\*n))), Ne(n, 0)),

$(\log(x), \text{True})/e + 3*B*a*c*d**2*\text{Piecewise}((-x**(3*n)/(2*n*(e*x)**(5*n))), \text{Ne}(n, 0)), (\log(x), \text{True})/e + B*a*d**3*\text{Piecewise}((-x**(4*n)/(n*(e*x)**(5*n))), \text{Ne}(n, 0)), (\log(x), \text{True})/e + B*b*c**3*\text{Piecewise}((-x**(2*n)/(3*n*(e*x)**(5*n))), \text{Ne}(n, 0)), (\log(x), \text{True})/e + 3*B*b*c**2*d*\text{Piecewise}((-x**(3*n)/(2*n*(e*x)**(5*n))), \text{Ne}(n, 0)), (\log(x), \text{True})/e + 3*B*b*c*d**2*\text{Piecewise}((-x**(4*n)/(n*(e*x)**(5*n))), \text{Ne}(n, 0)), (\log(x), \text{True})/e + B*b*d**3*\text{Piecewise}((0, (\text{Abs}(x) < 1) \& (1/\text{Abs}(x) < 1)), (\log(x)/e**(5*n), \text{Abs}(x) < 1), (-\log(1/x)/e**(5*n), 1/\text{Abs}(x) < 1), (-\text{meijerg}(((), (1, 1)), ((0, 0), ()), x)/e**(5*n) + \text{meijerg}(((1, 1), ()), (((), (0, 0)), x)/e**(5*n), \text{True}))/e, \text{Eq}(m, -5*n - 1)), (A*a*c**3*\text{Piecewise}((-1/(4*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*a*c**2*d*\text{Piecewise}((-x**n/(3*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*a*c*d**2*\text{Piecewise}((-x**(2*n)/(2*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + A*a*d**3*\text{Piecewise}((-x**(3*n)/(n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + A*b*c**3*\text{Piecewise}((-x**n/(3*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*b*c**2*d*\text{Piecewise}((-x**(2*n)/(2*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*b*c*d**2*\text{Piecewise}((-x**(3*n)/(n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + A*b*d**3*\text{Piecewise}((0, (\text{Abs}(x) < 1) \& (1/\text{Abs}(x) < 1)), (\log(x)/e**(4*n), \text{Abs}(x) < 1), (-\log(1/x)/e**(4*n), 1/\text{Abs}(x) < 1), (-\text{meijerg}(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + \text{meijerg}(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), \text{True}))/e + B*a*c**3*\text{Piecewise}((-x**n/(3*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*B*a*c**2*d*\text{Piecewise}((-x**(2*n)/(2*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*B*a*c*d**2*\text{Piecewise}((-x**(3*n)/(n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + B*a*d**3*\text{Piecewise}((0, (\text{Abs}(x) < 1) \& (1/\text{Abs}(x) < 1)), (\log(x)/e**(4*n), \text{Abs}(x) < 1), (-\log(1/x)/e**(4*n), 1/\text{Abs}(x) < 1), (-\text{meijerg}(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + \text{meijerg}(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), \text{True}))/e + B*b*c**3*\text{Piecewise}((-x**(2*n)/(2*n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*B*b*c**2*d*\text{Piecewise}((-x**(3*n)/(n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*B*b*c*d**2*\text{Piecewise}((0, (\text{Abs}(x) < 1) \& (1/\text{Abs}(x) < 1)), (\log(x)/e**(4*n), \text{Abs}(x) < 1), (-\log(1/x)/e**(4*n), 1/\text{Abs}(x) < 1), (-\text{meijerg}(((), (1, 1)), ((0, 0), ()), x)/e**(4*n) + \text{meijerg}(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), \text{True}))/e + B*b*d**3*\text{Piecewise}((x**(5*n)/(n*(e*x)**(4*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e, \text{Eq}(m, -4*n - 1)), (A*a*c**3*\text{Piecewise}((-1/(3*n*(e*x)**(3*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*a*c**2*d*\text{Piecewise}((-x**n/(2*n*(e*x)**(3*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*a*c*d**2*\text{Piecewise}((-x**(2*n)/(n*(e*x)**(3*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + A*a*d**3*\text{Piecewise}((0, (\text{Abs}(x) < 1) \& (1/\text{Abs}(x) < 1)), (\log(x)/e**(3*n), \text{Abs}(x) < 1), (-\log(1/x)/e**(3*n), 1/\text{Abs}(x) < 1), (-\text{meijerg}(((), (1, 1)), ((0, 0), ()), ()), x)/e**(3*n) + \text{meijerg}(((1, 1), ()), (((), (0, 0)), x)/e**(3*n), \text{True}))/e + A*b*c**3*\text{Piecewise}((-x**n/(2*n*(e*x)**(3*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*b*c**2*d*\text{Piecewise}((-x**(2*n)/(n*(e*x)**(3*n))), \text{Ne}(n, 0)), (\log(x), \text{True}))/e + 3*A*b*c*d**2*\text{Piecewise}((0, (\text{Abs}(x) < 1) \& (1/\text{Abs}(x) < 1)), (\log(x)/e**(3*n), \text{Abs}(x) < 1), (-\log(1/x)/e**(3*n), 1/\text{Abs}(x) < 1), (-\text{meijerg}(((), (1, 1)), ((0, 0), ()), x)/e**(3*n) + \text{meijerg}(((1, 1), ()), (((), (0, 0)), x)/e**(3*n), \text{True}))/e + A*b*d**3*\text{Piecewise}((x**(4*n)/(n*(e*x)**(3*n)))$

, Ne(n, 0)), (log(x), True))/e + B\*a\*c\*\*3\*Piecewise((-x\*\*n/(2\*n\*(e\*x)\*\*(3\*n)), Ne(n, 0)), (log(x), True))/e + 3\*B\*a\*c\*\*2\*d\*Piecewise((-x\*\*(2\*n)/(n\*(e\*x)\*\*(3\*n)), Ne(n, 0)), (log(x), True))/e + 3\*B\*a\*c\*d\*\*2\*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e\*\*(3\*n), Abs(x) < 1), (-log(1/x)/e\*\*(3\*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0,...

**Giac** [B] Leaf count of result is larger than twice the leaf count of optimal. 6927 vs.  $2(215) = 430$ .

time = 0.99, size = 6927, normalized size = 32.99

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="giac")

[Out]  $(B*b*d^3*m^5*x*x^m*x^{(5*n)}*e^m + 10*B*b*d^3*m^4*n*x*x^m*x^{(5*n)}*e^m + 35*B*b*d^3*m^3*n^2*x*x^m*x^{(5*n)}*e^m + 50*B*b*d^3*m^2*n^3*x*x^m*x^{(5*n)}*e^m + 24*B*b*d^3*m*n^4*x*x^m*x^{(5*n)}*e^m + 3*B*b*c*d^2*m^5*x*x^m*x^{(4*n)}*e^m + B*a*d^3*m^5*x*x^m*x^{(4*n)}*e^m + A*b*d^3*m^5*x*x^m*x^{(4*n)}*e^m + 33*B*b*c*d^2*m^4*n*x*x^m*x^{(4*n)}*e^m + 11*B*a*d^3*m^4*n*x*x^m*x^{(4*n)}*e^m + 11*A*b*d^3*m^4*n*x*x^m*x^{(4*n)}*e^m + 123*B*b*c*d^2*m^3*n^2*x*x^m*x^{(4*n)}*e^m + 41*B*a*d^3*m^3*n^2*x*x^m*x^{(4*n)}*e^m + 41*A*b*d^3*m^3*n^2*x*x^m*x^{(4*n)}*e^m + 183*B*b*c*d^2*m^2*n^3*x*x^m*x^{(4*n)}*e^m + 61*B*a*d^3*m^2*n^3*x*x^m*x^{(4*n)}*e^m + 61*A*b*d^3*m^2*n^3*x*x^m*x^{(4*n)}*e^m + 90*B*b*c*d^2*m*n^4*x*x^m*x^{(4*n)}*e^m + 30*B*a*d^3*m*n^4*x*x^m*x^{(4*n)}*e^m + 30*A*b*d^3*m*n^4*x*x^m*x^{(4*n)}*e^m + 3*B*b*c^2*d*m^5*x*x^m*x^{(3*n)}*e^m + 3*B*a*c*d^2*m^5*x*x^m*x^{(3*n)}*e^m + 3*A*b*c*d^2*m^5*x*x^m*x^{(3*n)}*e^m + A*a*d^3*m^5*x*x^m*x^{(3*n)}*e^m + 36*B*b*c^2*d*m^4*n*x*x^m*x^{(3*n)}*e^m + 36*B*a*c*d^2*m^4*n*x*x^m*x^{(3*n)}*e^m + 36*A*b*c*d^2*m^4*n*x*x^m*x^{(3*n)}*e^m + 12*A*a*d^3*m^4*n*x*x^m*x^{(3*n)}*e^m + 147*B*b*c^2*d*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 147*B*a*c*d^2*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 147*A*b*c*d^2*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 49*A*a*d^3*m^3*n^2*x*x^m*x^{(3*n)}*e^m + 234*B*b*c^2*d*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 234*B*a*c*d^2*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 234*A*b*c*d^2*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 78*A*a*d^3*m^2*n^3*x*x^m*x^{(3*n)}*e^m + 120*B*b*c^2*d*m*n^4*x*x^m*x^{(3*n)}*e^m + 120*B*a*c*d^2*m*n^4*x*x^m*x^{(3*n)}*e^m + 120*A*b*c*d^2*m*n^4*x*x^m*x^{(3*n)}*e^m + 40*A*a*d^3*m*n^4*x*x^m*x^{(3*n)}*e^m + B*b*c^3*m^5*x*x^m*x^{(2*n)}*e^m + 3*B*a*c^2*d*m^5*x*x^m*x^{(2*n)}*e^m + 3*A*b*c^2*d*m^5*x*x^m*x^{(2*n)}*e^m + 3*A*a*c*d^2*m^5*x*x^m*x^{(2*n)}*e^m + 13*B*b*c^3*m^4*n*x*x^m*x^{(2*n)}*e^m + 39*B*a*c^2*d*m^4*n*x*x^m*x^{(2*n)}*e^m + 39*A*b*c^2*d*m^4*n*x*x^m*x^{(2*n)}*e^m + 39*A*a*c*d^2*m^4*n*x*x^m*x^{(2*n)}*e^m + 59*B*b*c^3*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*B*a*c^2*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*b*c^2*d*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 177*A*a*c*d^2*m^3*n^2*x*x^m*x^{(2*n)}*e^m + 107*B*b*c^3*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*B*a*c^2*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*A*b*c^2*d*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 321*A*a*c*d^2*m^2*n^3*x*x^m*x^{(2*n)}*e^m + 60*B*b*c^3*m*n^4*x*x^m*x^{(2*n)}*e^m + 180*B*a*c^2*d*m*n^4*x*x^m*x^{(2*n)}*e^m + 180*A*b*c^2*d*m*$

$$\begin{aligned}
& n^4 x^m x^{(2n)} e^m + 180 A^2 a^2 c^2 d^2 m^2 n^4 x^m x^{(2n)} e^m + B^2 a^2 c^3 m^5 \\
& x^m x^{(2n)} e^m + A^2 b^2 c^3 m^5 x^m x^{(2n)} e^m + 3 A^2 a^2 c^2 d^2 m^5 x^m x^{(2n)} e^m \\
& + 14 B^2 a^2 c^3 m^4 n x^m x^{(2n)} e^m + 14 A^2 b^2 c^3 m^4 n x^m x^{(2n)} e^m + 42 A^2 a^2 \\
& c^2 d^2 m^4 n x^m x^{(2n)} e^m + 71 B^2 a^2 c^3 m^3 n^2 x^m x^{(2n)} e^m + 71 A^2 b^2 c^3 m^3 \\
& n^2 x^m x^{(2n)} e^m + 213 A^2 a^2 c^2 d^2 m^3 n^2 x^m x^{(2n)} e^m + 154 B^2 a^2 c^3 m^2 \\
& n^3 x^m x^{(2n)} e^m + 154 A^2 b^2 c^3 m^2 n^3 x^m x^{(2n)} e^m + 462 A^2 a^2 c^2 d^2 m^2 \\
& n^3 x^m x^{(2n)} e^m + 120 B^2 a^2 c^3 m^2 n^4 x^m x^{(2n)} e^m + 120 A^2 b^2 c^3 m^2 n^4 x^m \\
& x^{(2n)} e^m + 360 A^2 a^2 c^2 d^2 m^2 n^4 x^m x^{(2n)} e^m + A^2 a^2 c^3 m^5 x^m x^{(2n)} e^m + 1 \\
& 5 A^2 a^2 c^3 m^4 n x^m x^{(2n)} e^m + 85 A^2 a^2 c^3 m^3 n^2 x^m x^{(2n)} e^m + 225 A^2 a^2 c^3 m^2 \\
& n^3 x^m x^{(2n)} e^m + 274 A^2 a^2 c^3 m^2 n^4 x^m x^{(2n)} e^m + 120 A^2 a^2 c^3 n^5 x^m x^{(2n)} e^m + 5 \\
& B^2 b^2 d^3 m^4 x^m x^{(5n)} e^m + 40 B^2 b^2 d^3 m^3 n x^m x^{(5n)} e^m + 105 B^2 \\
& b^2 d^3 m^2 n^2 x^m x^{(5n)} e^m + 100 B^2 b^2 d^3 m^2 n^3 x^m x^{(5n)} e^m + 24 \\
& B^2 b^2 d^3 n^4 x^m x^{(5n)} e^m + 15 B^2 b^2 c^2 d^2 m^4 x^m x^{(4n)} e^m + 5 B^2 a^2 \\
& d^3 m^4 x^m x^{(4n)} e^m + 5 A^2 b^2 d^3 m^4 x^m x^{(4n)} e^m + 132 B^2 b^2 c^2 d^2 \\
& m^3 n x^m x^{(4n)} e^m + 44 B^2 a^2 d^3 m^3 n x^m x^{(4n)} e^m + 44 A^2 b^2 d^3 \\
& m^3 n x^m x^{(4n)} e^m + 369 B^2 b^2 c^2 d^2 m^2 n^2 x^m x^{(4n)} e^m + 123 B^2 \\
& a^2 d^3 m^2 n^2 x^m x^{(4n)} e^m + 123 A^2 b^2 d^3 m^2 n^2 x^m x^{(4n)} e^m + 3 \\
& 66 B^2 b^2 c^2 d^2 m^2 n^3 x^m x^{(4n)} e^m + 122 B^2 a^2 d^3 m^2 n^3 x^m x^{(4n)} e^m \\
& + 122 A^2 b^2 d^3 m^2 n^3 x^m x^{(4n)} e^m + 90 B^2 b^2 c^2 d^2 n^4 x^m x^{(4n)} e^m \\
& + 30 B^2 a^2 d^3 n^4 x^m x^{(4n)} e^m + 30 A^2 b^2 d^3 n^4 x^m x^{(4n)} e^m + 15 \\
& B^2 b^2 c^2 d^2 m^4 x^m x^{(3n)} e^m + 15 B^2 a^2 c^2 d^2 m^4 x^m x^{(3n)} e^m + 15 A^2 \\
& b^2 c^2 d^2 m^4 x^m x^{(3n)} e^m + 5 A^2 a^2 d^3 m^4 x^m x^{(3n)} e^m + 144 B^2 b^2 \\
& c^2 d^2 m^3 n x^m x^{(3n)} e^m + 144 B^2 a^2 c^2 d^2 m^3 n x^m x^{(3n)} e^m + 144 \\
& A^2 b^2 c^2 d^2 m^3 n x^m x^{(3n)} e^m + 48 A^2 a^2 d^3 m^3 n x^m x^{(3n)} e^m + 4 \\
& 41 B^2 b^2 c^2 d^2 m^2 n^2 x^m x^{(3n)} e^m + 441 B^2 a^2 c^2 d^2 m^2 n^2 x^m x^{(3n)} \\
& e^m + 441 A^2 b^2 c^2 d^2 m^2 n^2 x^m x^{(3n)} e^m + 147 A^2 a^2 d^3 m^2 n^2 x^m x^{(3n)} \\
& e^m + 468 B^2 b^2 c^2 d^2 m^2 n^3 x^m x^{(3n)} e^m + 468 B^2 a^2 c^2 d^2 m^2 n^3 x^m \\
& x^{(3n)} e^m + 468 A^2 b^2 c^2 d^2 m^2 n^3 x^m x^{(3n)} e^m + 156 A^2 a^2 d^3 m^2 n^3 \\
& x^m x^{(3n)} e^m + 120 B^2 b^2 c^2 d^2 n^4 x^m x^{(3n)} e^m + 120 B^2 a^2 c^2 d^2 n^4 \\
& x^m x^{(3n)} e^m + 120 A^2 b^2 c^2 d^2 n^4 x^m x^{(3n)} e^m + 40 A^2 a^2 d^3 n^4 x^m \\
& x^{(3n)} e^m + 5 B^2 b^2 c^3 m^4 x^m x^{(2n)} e^m + 15 B^2 a^2 c^3 m^4 x^m x^{(2n)} e^m \\
& + 15 A^2 b^2 c^3 m^4 x^m x^{(2n)} e^m + 15 A^2 a^2 c^3 d^2 m^4 x^m x^{(2n)} e^m + 52 B^2 b^2 \\
& c^3 m^3 n x^m x^{(2n)} e^m + 156 B^2 a^2 c^3 m^3 n x^m x^{(2n)} e^m + 156 A^2 a^2 c^3 d^2 m^3 \\
& n x^m x^{(2n)} e^m + 177 B^2 b^2 c^3 m^2 n^2 x^m x^{(2n)} e^m + 531 B^2 a^2 c^3 d^2 m^2 n^2 \\
& x^m x^{(2n)} e^m + 531 A^2 b^2 c^3 d^2 m^2 n^2 x^m x^{(2n)} e^m + 53 \\
& 1 A^2 a^2 c^3 d^2 m^2 n^2 x^m x^{(2n)} e^m + 214 B^2 b^2 \dots
\end{aligned}$$

Mupad [B]

time = 5.65, size = 1089, normalized size = 5.19

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A + B*x^n)*(a + b*x^n)*(c + d*x^n)^3,x)$

[Out]  $(A*a*c^3*x*(e*x)^m)/(m+1) + (d^2*x*x^{(4*n)}*(e*x)^m*(A*b*d + B*a*d + 3*B*b*c)*(4*m + 11*n + 33*m*n + 82*m*n^2 + 33*m^2*n + 61*m*n^3 + 11*m^3*n + 6*m^2 + 4*m^3 + m^4 + 41*n^2 + 61*n^3 + 30*n^4 + 41*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (c*x*x^{(2*n)}*(e*x)^m*(3*A*a*d^2 + B*b*c^2 + 3*A*b*c*d + 3*B*a*c*d)*(4*m + 13*n + 39*m*n + 118*m*n^2 + 39*m^2*n + 107*m*n^3 + 13*m^3*n + 6*m^2 + 4*m^3 + m^4 + 59*n^2 + 107*n^3 + 60*n^4 + 59*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (d*x*x^{(3*n)}*(e*x)^m*(A*a*d^2 + 3*B*b*c^2 + 3*A*b*c*d + 3*B*a*c*d)*(4*m + 12*n + 36*m*n + 98*m*n^2 + 36*m^2*n + 78*m*n^3 + 12*m^3*n + 6*m^2 + 4*m^3 + m^4 + 49*n^2 + 78*n^3 + 40*n^4 + 49*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (c^2*x*x^n*(e*x)^m*(3*A*a*d + A*b*c + B*a*c)*(4*m + 14*n + 42*m*n + 142*m*n^2 + 42*m^2*n + 154*m*n^3 + 14*m^3*n + 6*m^2 + 4*m^3 + m^4 + 71*n^2 + 154*n^3 + 120*n^4 + 71*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1) + (B*b*d^3*x*x^{(5*n)}*(e*x)^m*(4*m + 10*n + 30*m*n + 70*m*n^2 + 30*m^2*n + 50*m*n^3 + 10*m^3*n + 6*m^2 + 4*m^3 + m^4 + 35*n^2 + 50*n^3 + 24*n^4 + 35*m^2*n^2 + 1))/(5*m + 15*n + 60*m*n + 255*m*n^2 + 90*m^2*n + 450*m*n^3 + 60*m^3*n + 274*m*n^4 + 15*m^4*n + 10*m^2 + 10*m^3 + 5*m^4 + m^5 + 85*n^2 + 225*n^3 + 274*n^4 + 120*n^5 + 255*m^2*n^2 + 225*m^2*n^3 + 85*m^3*n^2 + 1)$

### 3.18 $\int (ex)^m (A + Bx^n) (c + dx^n)^3 dx$

**Optimal.** Leaf size=137

$$\frac{c^2(Bc + 3Ad)x^{1+n}(ex)^m}{1+m+n} + \frac{3cd(Bc + Ad)x^{1+2n}(ex)^m}{1+m+2n} + \frac{d^2(3Bc + Ad)x^{1+3n}(ex)^m}{1+m+3n} + \frac{Bd^3x^{1+4n}(ex)^m}{1+m+4n} + \frac{Ac^3(ex)^m}{e(1+m)}$$

[Out]  $c^2*(3*A*d+B*c)*x^{(1+n)}*(e*x)^m/(1+m+n)+3*c*d*(A*d+B*c)*x^{(1+2*n)}*(e*x)^m/(1+m+2*n)+d^2*(A*d+3*B*c)*x^{(1+3*n)}*(e*x)^m/(1+m+3*n)+B*d^3*x^{(1+4*n)}*(e*x)^m/(1+m+4*n)+A*c^3*(e*x)^{(1+m)}/e/(1+m)$

**Rubi [A]**

time = 0.08, antiderivative size = 137, normalized size of antiderivative = 1.00, number of steps used = 10, number of rules used = 3, integrand size = 22,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.136$ ,

Rules used = {459, 20, 30}

$$\frac{c^2x^{n+1}(ex)^m(3Ad + Bc)}{m+n+1} + \frac{d^2x^{3n+1}(ex)^m(Ad + 3Bc)}{m+3n+1} + \frac{3cdx^{2n+1}(ex)^m(Ad + Bc)}{m+2n+1} + \frac{Ac^3(ex)^{m+1}}{e(m+1)} + \frac{Bd^3x^{4n+1}(ex)^m}{m+4n+1}$$

Antiderivative was successfully verified.

[In] Int[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

[Out]  $(c^2*(B*c + 3*A*d)*x^{(1+n)}*(e*x)^m/(1+m+n) + (3*c*d*(B*c + A*d)*x^{(1+2*n)}*(e*x)^m/(1+m+2*n) + (d^2*(3*B*c + A*d)*x^{(1+3*n)}*(e*x)^m/(1+m+3*n) + (B*d^3*x^{(1+4*n)}*(e*x)^m/(1+m+4*n) + (A*c^3*(e*x)^{(1+m)})/(e*(1+m)))$

**Rule 20**

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

**Rule 30**

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

**Rule 459**

Int[((e\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_), x\_Symbol] := Int[ExpandIntegrand[(e\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && IGtQ[p, 0] && IGtQ[q, 0]

Rubi steps



$$\begin{aligned}
\int (ex)^m (A + Bx^n) (c + dx^n)^3 dx &= \int (Ac^3(ex)^m + c^2(Bc + 3Ad)x^n(ex)^m + 3cd(Bc + Ad)x^{2n}(ex)^m + d^2(Bc + Ad)x^{3n}(ex)^m) dx \\
&= \frac{Ac^3(ex)^{1+m}}{e(1+m)} + (Bd^3) \int x^{4n}(ex)^m dx + (3cd(Bc + Ad)) \int x^{2n}(ex)^m dx + (d^2(Bc + Ad)) \int x^{3n}(ex)^m dx \\
&= \frac{Ac^3(ex)^{1+m}}{e(1+m)} + (Bd^3 x^{-m}(ex)^m) \int x^{m+4n} dx + (3cd(Bc + Ad)x^{-m}(ex)^m) \int x^{m+2n} dx + (d^2(Bc + Ad)x^{-m}(ex)^m) \int x^{m+n} dx \\
&= \frac{c^2(Bc + 3Ad)x^{1+n}(ex)^m}{1+m+n} + \frac{3cd(Bc + Ad)x^{1+2n}(ex)^m}{1+m+2n} + \frac{d^2(3Bc + Ad)x^{1+3n}(ex)^m}{1+m+3n} + \frac{Bd^3 x^{1+4n}(ex)^m}{1+m+4n}
\end{aligned}$$

**Mathematica [A]**

time = 0.15, size = 106, normalized size = 0.77

$$x(ex)^m \left( \frac{Ac^3}{1+m} + \frac{c^2(Bc + 3Ad)x^n}{1+m+n} + \frac{3cd(Bc + Ad)x^{2n}}{1+m+2n} + \frac{d^2(3Bc + Ad)x^{3n}}{1+m+3n} + \frac{Bd^3 x^{4n}}{1+m+4n} \right)$$

Antiderivative was successfully verified.

**[In]** Integrate[(e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3,x]

**[Out]** x\*(e\*x)^m\*((A\*c^3)/(1+m) + (c^2\*(B\*c + 3\*A\*d)\*x^n)/(1+m+n) + (3\*c\*d\*(B\*c + A\*d)\*x^(2\*n))/(1+m+2\*n) + (d^2\*(3\*B\*c + A\*d)\*x^(3\*n))/(1+m+3\*n) + (B\*d^3\*x^(4\*n))/(1+m+4\*n))

**Maple [C]** Result contains higher order function than in optimal. Order 9 vs. order 3.

time = 0.36, size = 1609, normalized size = 11.74

method	result	size
risch	Expression too large to display	1609

Verification of antiderivative is not currently implemented for this CAS.

**[In]** int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3,x,method=\_RETURNVERBOSE)

**[Out]** x\*(4\*A\*d^3\*(x^n)^3\*m+8\*A\*d^3\*n^3\*(x^n)^3+156\*A\*c^2\*d\*m\*n^2\*x^n+72\*A\*c\*d^2\*m\*n\*(x^n)^2+57\*B\*c^2\*d\*m^2\*n^2\*(x^n)^2+24\*A\*c\*d^2\*(x^n)^2\*n+27\*B\*c^3\*m\*n\*x^n+12\*B\*c^2\*d\*(x^n)^2\*m+6\*A\*d^3\*m^2\*(x^n)^3+14\*A\*d^3\*n^2\*(x^n)^3+36\*B\*c^2\*d\*m\*n^3\*(x^n)^2+72\*B\*c^2\*d\*m\*n\*(x^n)^2+B\*c^3\*m^4\*x^n+4\*m\*B\*d^3\*(x^n)^4+24\*B\*c^3\*n^3\*x^n+6\*B\*c^3\*m^2\*x^n+26\*B\*c^3\*n^2\*x^n+81\*A\*c^2\*d\*m\*n\*x^n+63\*B\*c\*d^2\*m^2\*n\*(x^n)^3+84\*B\*c\*d^2\*m\*n^2\*(x^n)^3+27\*A\*c^2\*d\*m^3\*n\*x^n+36\*A\*c\*d^2\*m\*n^3\*(x^n)^2+24\*B\*c^2\*d\*m^3\*n\*(x^n)^2+3\*(x^n)^2\*A\*c\*d^2+3\*(x^n)^2\*B\*c^2\*d+6\*B\*d^3\*(x^n)^4\*n+3\*A\*c^2\*d\*x^n+12\*A\*c\*d^2\*m^3\*(x^n)^2+36\*A\*c\*d^2\*n^3\*(x^n)^2+21\*A\*d^3\*m\*n\*(x^n)^3+9\*B\*c^3\*m^3\*n\*x^n+26\*B\*c^3\*m^2\*n^2\*x^n+24\*B\*c^3\*m\*n^3\*x^n+12\*B\*c^2\*d\*m^3\*(x^n)^2+24\*B\*c^2\*d\*(x^n)^2\*n+70\*A\*c^3\*m\*n^2+78\*A\*c^2\*d\*m^2\*

$$\begin{aligned} & n^2 x^n + 72 A c^2 d m n^3 x^n + 72 A c d^2 m^2 n (x^n)^2 + 114 A c d^2 m n^2 (x^n)^2 + 72 B c^2 d m^2 n (x^n)^2 + 114 B c^2 d m n^2 (x^n)^2 + 63 B c d^2 m n (x^n)^3 + 81 A c^2 d m^2 n x^n + B c^3 x^n + 4 B c^3 x^n m + 9 B c^3 x^n n + A c^3 + A c^3 m^4 + 24 A c^3 n^4 + 4 A c^3 m^3 + 50 A c^3 n^3 + 6 A c^3 m^2 + 35 A c^3 n^2 + 6 B d^3 m^2 (x^n)^4 + 11 B d^3 n^2 (x^n)^4 + A d^3 (x^n)^3 + 24 A c d^2 m^3 n (x^n)^2 + 57 A c d^2 m^2 n^2 (x^n)^2 + 4 A c^3 m + 10 A c^3 n + A d^3 m^4 (x^n)^3 + 4 B d^3 m^3 (x^n)^4 + 6 B d^3 n^3 (x^n)^4 + 4 A d^3 m^3 (x^n)^3 + B d^3 (x^n)^4 + 3 (x^n)^3 B c d^2 + 30 A c^3 m n + 10 A c^3 m^3 n + 35 A c^3 m^2 n^2 + 50 A c^3 m n^3 + 30 A c^3 m^2 n + 8 A d^3 m n^3 (x^n)^3 + 3 B c d^2 m^4 (x^n)^3 + 18 B d^3 m^2 n (x^n)^4 + 22 B d^3 m n^2 (x^n)^4 + 12 B c d^2 m^3 (x^n)^3 + 24 B c d^2 n^3 (x^n)^3 + 18 B d^3 m n (x^n)^4 + 3 A c^2 d m^4 x^n + 14 A d^3 m^2 n^2 (x^n)^3 + 12 A c^2 d x^n m + 27 A c^2 d x^n n + 6 B d^3 m^3 n (x^n)^4 + 11 B d^3 m^2 n^2 (x^n)^4 + 6 B d^3 m n^3 (x^n)^4 + 7 A d^3 m^3 n (x^n)^3 + 24 B c d^2 m n^3 (x^n)^3 + 7 A d^3 (x^n)^3 n + 4 B c^3 m^3 x^n + B d^3 m^4 (x^n)^4 + 21 B c d^2 m^3 n (x^n)^3 + 42 B c d^2 m^2 n^2 (x^n)^3 + 57 B c^2 d n^2 (x^n)^2 + 12 B c d^2 (x^n)^3 m + 21 B c d^2 (x^n)^3 n + 18 A c^2 d m^2 x^n + 78 A c^2 d n^2 x^n + 12 A c d^2 (x^n)^2 m + 36 B c^2 d n^3 (x^n)^2 + 18 B c d^2 m^2 (x^n)^3 + 42 B c d^2 n^2 (x^n)^3 + 12 A c^2 d m^3 x^n + 72 A c^2 d n^3 x^n + 18 A c d^2 m^2 (x^n)^2 + 57 A c d^2 n^2 (x^n)^2 + 27 B c^3 m^2 n x^n + 52 B c^3 m n^2 x^n + 18 B c^2 d m^2 (x^n)^2 + 3 A c d^2 m^4 (x^n)^2 + 21 A d^3 m^2 n (x^n)^3 + 28 A d^3 m n^2 (x^n)^3 + 3 B c^2 d m^4 (x^n)^2 / (1+m) / (1+m+n) / (1+m+2n) / (1+m+3n) / (1+m+4n) * exp(1/2*m*(-I*Pi*csgn(I*e*x)^3 + I*Pi*csgn(I*e*x)^2*csgn(I*e) + I*Pi*csgn(I*e*x)^2*csgn(I*x) - I*Pi*csgn(I*e*x)*csgn(I*e)*csgn(I*x) + 2*ln(e) + 2*ln(x))) \end{aligned}$$

**Maxima** [A]

time = 0.35, size = 205, normalized size = 1.50

$$\frac{(x e)^{m+1} A c^3 e^{-1}}{m+1} + \frac{B d^3 x e^{(m \log(x) + 4 n \log(x) + m)}}{m+4 n+1} + \frac{3 B c d^2 x e^{(m \log(x) + 3 n \log(x) + m)}}{m+3 n+1} + \frac{A d^3 x e^{(m \log(x) + 3 n \log(x) + m)}}{m+3 n+1} + \frac{3 B c^2 d x e^{(m \log(x) + 2 n \log(x) + m)}}{m+2 n+1} + \frac{3 A c d^2 x e^{(m \log(x) + 2 n \log(x) + m)}}{m+2 n+1} + \frac{B c^3 x e^{(m \log(x) + n \log(x) + m)}}{m+n+1} + \frac{3 A c^2 d x e^{(m \log(x) + n \log(x) + m)}}{m+n+1}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="maxima")

[Out] (x\*e)^(m + 1)\*A\*c^3\*e^(-1)/(m + 1) + B\*d^3\*x\*e^(m\*log(x) + 4\*n\*log(x) + m)/(m + 4\*n + 1) + 3\*B\*c\*d^2\*x\*e^(m\*log(x) + 3\*n\*log(x) + m)/(m + 3\*n + 1) + A\*d^3\*x\*e^(m\*log(x) + 3\*n\*log(x) + m)/(m + 3\*n + 1) + 3\*B\*c^2\*d\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + 3\*A\*c\*d^2\*x\*e^(m\*log(x) + 2\*n\*log(x) + m)/(m + 2\*n + 1) + B\*c^3\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1) + 3\*A\*c^2\*d\*x\*e^(m\*log(x) + n\*log(x) + m)/(m + n + 1)

**Fricas** [B] Leaf count of result is larger than twice the leaf count of optimal. 1089 vs. 2(141) = 282.

time = 1.00, size = 1089, normalized size = 7.95

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3,x, algorithm="fricas")

[Out] ((B\*d^3\*m^4 + 4\*B\*d^3\*m^3 + 6\*B\*d^3\*m^2 + 4\*B\*d^3\*m + B\*d^3 + 6\*(B\*d^3\*m + B\*d^3)\*n^3 + 11\*(B\*d^3\*m^2 + 2\*B\*d^3\*m + B\*d^3)\*n^2 + 6\*(B\*d^3\*m^3 + 3\*B\*d^3\*m^2 + 3\*B\*d^3\*m + B\*d^3)\*n)\*x\*x^(4\*n)\*e^(m\*log(x) + m) + ((3\*B\*c\*d^2 + A\*d^3)\*m^4 + 3\*B\*c\*d^2 + A\*d^3 + 4\*(3\*B\*c\*d^2 + A\*d^3)\*m^3 + 8\*(3\*B\*c\*d^2 + A\*d^3 + (3\*B\*c\*d^2 + A\*d^3)\*m)\*n^3 + 6\*(3\*B\*c\*d^2 + A\*d^3)\*m^2 + 14\*(3\*B\*c\*d^2 + A\*d^3 + (3\*B\*c\*d^2 + A\*d^3)\*m^2 + 2\*(3\*B\*c\*d^2 + A\*d^3)\*m)\*n^2 + 4\*(3\*B\*c\*d^2 + A\*d^3)\*m + 7\*(3\*B\*c\*d^2 + A\*d^3 + (3\*B\*c\*d^2 + A\*d^3)\*m^3 + 3\*(3\*B\*c\*d^2 + A\*d^3)\*m^2 + 3\*(3\*B\*c\*d^2 + A\*d^3)\*m)\*n)\*x\*x^(3\*n)\*e^(m\*log(x) + m) + 3\*((B\*c^2\*d + A\*c\*d^2)\*m^4 + B\*c^2\*d + A\*c\*d^2 + 4\*(B\*c^2\*d + A\*c\*d^2)\*m^3 + 12\*(B\*c^2\*d + A\*c\*d^2 + (B\*c^2\*d + A\*c\*d^2)\*m)\*n^3 + 6\*(B\*c^2\*d + A\*c\*d^2)\*m^2 + 19\*(B\*c^2\*d + A\*c\*d^2 + (B\*c^2\*d + A\*c\*d^2)\*m^2 + 2\*(B\*c^2\*d + A\*c\*d^2)\*m)\*n^2 + 4\*(B\*c^2\*d + A\*c\*d^2)\*m + 8\*(B\*c^2\*d + A\*c\*d^2 + (B\*c^2\*d + A\*c\*d^2)\*m^3 + 3\*(B\*c^2\*d + A\*c\*d^2)\*m^2 + 3\*(B\*c^2\*d + A\*c\*d^2)\*m)\*n)\*x\*x^(2\*n)\*e^(m\*log(x) + m) + ((B\*c^3 + 3\*A\*c^2\*d)\*m^4 + B\*c^3 + 3\*A\*c^2\*d + 4\*(B\*c^3 + 3\*A\*c^2\*d)\*m^3 + 24\*(B\*c^3 + 3\*A\*c^2\*d + (B\*c^3 + 3\*A\*c^2\*d)\*m)\*n^3 + 6\*(B\*c^3 + 3\*A\*c^2\*d)\*m^2 + 26\*(B\*c^3 + 3\*A\*c^2\*d + (B\*c^3 + 3\*A\*c^2\*d)\*m^2 + 2\*(B\*c^3 + 3\*A\*c^2\*d)\*m)\*n^2 + 4\*(B\*c^3 + 3\*A\*c^2\*d)\*m + 9\*(B\*c^3 + 3\*A\*c^2\*d + (B\*c^3 + 3\*A\*c^2\*d)\*m^3 + 3\*(B\*c^3 + 3\*A\*c^2\*d)\*m^2 + 3\*(B\*c^3 + 3\*A\*c^2\*d)\*m)\*n)\*x\*x^n\*e^(m\*log(x) + m) + (A\*c^3\*m^4 + 24\*A\*c^3\*n^4 + 4\*A\*c^3\*m^3 + 6\*A\*c^3\*m^2 + 4\*A\*c^3\*m + A\*c^3 + 50\*(A\*c^3\*m + A\*c^3)\*n^3 + 35\*(A\*c^3\*m^2 + 2\*A\*c^3\*m + A\*c^3)\*n^2 + 10\*(A\*c^3\*m^3 + 3\*A\*c^3\*m^2 + 3\*A\*c^3\*m + A\*c^3)\*n)\*x\*e^(m\*log(x) + m)/(m^5 + 24\*(m + 1)\*n^4 + 5\*m^4 + 50\*(m^2 + 2\*m + 1)\*n^3 + 10\*m^3 + 35\*(m^3 + 3\*m^2 + 3\*m + 1)\*n^2 + 10\*m^2 + 10\*(m^4 + 4\*m^3 + 6\*m^2 + 4\*m + 1)\*n + 5\*m + 1)

**Sympy** [B] Leaf count of result is larger than twice the leaf count of optimal. 16521 vs.  $\frac{2(128)}{2} = 256$ .

time = 76.54, size = 16521, normalized size = 120.59

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*3,x)

[Out] Piecewise(((A + B)\*(c + d)\*\*3\*log(x)/e, Eq(m, -1) & Eq(n, 0)), ((A\*c\*\*3\*log(x) + 3\*A\*c\*\*2\*d\*x\*\*n/n + 3\*A\*c\*d\*\*2\*x\*\*(2\*n)/(2\*n) + A\*d\*\*3\*x\*\*(3\*n)/(3\*n) + B\*c\*\*3\*x\*\*n/n + 3\*B\*c\*\*2\*d\*x\*\*(2\*n)/(2\*n) + B\*c\*d\*\*2\*x\*\*(3\*n)/n + B\*d\*\*3\*x\*\*(4\*n)/(4\*n))/e, Eq(m, -1)), (A\*c\*\*3\*Piecewise((-1/(4\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 3\*A\*c\*\*2\*d\*Piecewise((-x\*\*n/(3\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 3\*A\*c\*d\*\*2\*Piecewise((-x\*\*(2\*n)/(2\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + A\*d\*\*3\*Piecewise((-x\*\*(3\*n)/(n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + B\*c\*\*3\*Piecewise((-x\*\*n/(3\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 3\*B\*c\*\*2\*d\*Piecewise((-x\*\*(2\*n)/(2\*n\*(e\*x)\*\*(4\*n)), Ne(n, 0)), (log(x), True))/e + 3\*B\*c\*d\*\*2\*Piecewise((-

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x**(3*n)/(n*(e*x)**(4*n)), Ne(n, 0)), (log(x), True))/e + B*d**3*Piecewise(
(0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(4*n), Abs(x) < 1), (-log(1/
x)/e**(4*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(4*
n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(4*n), True))/e, Eq(m, -4*n
- 1)), (A*c**3*Piecewise((-1/(3*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), True))
/e + 3*A*c**2*d*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0)), (log(x), Tr
ue))/e + 3*A*c*d**2*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(n, 0)), (log(
x), True))/e + A*d**3*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)
/e**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1), (-meijerg(((),
(1, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)
/e**(3*n), True))/e + B*c**3*Piecewise((-x**n/(2*n*(e*x)**(3*n)), Ne(n, 0))
, (log(x), True))/e + 3*B*c**2*d*Piecewise((-x**(2*n)/(n*(e*x)**(3*n)), Ne(
n, 0)), (log(x), True))/e + 3*B*c*d**2*Piecewise((0, (Abs(x) < 1) & (1/Abs(
x) < 1)), (log(x)/e**(3*n), Abs(x) < 1), (-log(1/x)/e**(3*n), 1/Abs(x) < 1)
, (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**(3*n) + meijerg(((1, 1), ()),
((), (0, 0)), x)/e**(3*n), True))/e + B*d**3*Piecewise((x**(4*n)/(n*(e*x)*
*(3*n)), Ne(n, 0)), (log(x), True))/e, Eq(m, -3*n - 1)), (A*c**3*Piecewise(
(-1/(2*n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + 3*A*c**2*d*Piecewise
((-x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + 3*A*c*d**2*Piecawi
se((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n), Abs(x) < 1), (-log
(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), ()), x)/e**
(2*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n), True))/e + A*d**3*
Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + B*c**3
*Piecewise((-x**n/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), True))/e + 3*B*c**2
*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)/e**(2*n), Abs(x) <
1), (-log(1/x)/e**(2*n), 1/Abs(x) < 1), (-meijerg(((), (1, 1)), ((0, 0), (
)), x)/e**(2*n) + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**(2*n), True))/e
+ 3*B*c*d**2*Piecewise((x**(3*n)/(n*(e*x)**(2*n)), Ne(n, 0)), (log(x), Tru
e))/e + B*d**3*Piecewise((x**(4*n)/(2*n*(e*x)**(2*n)), Ne(n, 0)), (log(x),
True))/e, Eq(m, -2*n - 1)), (A*c**3*Piecewise((-1/(n*(e*x)**n), Ne(n, 0)),
(log(x), True))/e + 3*A*c**2*d*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1))
, (log(x)/e**n, Abs(x) < 1), (-log(1/x)/e**n, 1/Abs(x) < 1), (-meijerg(((),
(1, 1)), ((0, 0), ()), x)/e**n + meijerg(((1, 1), ()), (((), (0, 0)), x)/e*
*n, True))/e + 3*A*c*d**2*Piecewise((x**(2*n)/(n*(e*x)**n), Ne(n, 0)), (log
(x), True))/e + A*d**3*Piecewise((x**(3*n)/(2*n*(e*x)**n), Ne(n, 0)), (log(
x), True))/e + B*c**3*Piecewise((0, (Abs(x) < 1) & (1/Abs(x) < 1)), (log(x)
/e**n, Abs(x) < 1), (-log(1/x)/e**n, 1/Abs(x) < 1), (-meijerg(((), (1, 1)),
((0, 0), ()), x)/e**n + meijerg(((1, 1), ()), (((), (0, 0)), x)/e**n, True)
)/e + 3*B*c**2*d*Piecewise((x**(2*n)/(n*(e*x)**n), Ne(n, 0)), (log(x), True
))/e + 3*B*c*d**2*Piecewise((x**(3*n)/(2*n*(e*x)**n), Ne(n, 0)), (log(x), T
rue))/e + B*d**3*Piecewise((x**(4*n)/(3*n*(e*x)**n), Ne(n, 0)), (log(x), Tr
ue))/e, Eq(m, -n - 1)), (A*c**3*m**4*x*(e*x)**m/(m**5 + 10*m**4*n + 5*m**4
+ 35*m**3*n**2 + 40*m**3*n + 10*m**3 + 50*m**2*n**3 + 105*m**2*n**2 + 60*m*
*2*n + 10*m**2 + 24*m*n**4 + 100*m*n**3 + 105*m*n**2 + 40*m*n + 5*m + 24*n*
*4 + 50*n**3 + 35*n**2 + 10*n + 1) + 10*A*c**3*m**3*n*x*(e*x)**m/(m**5 + 10

```

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*m**4*n + 5*m**4 + 35*m**3*n**2 + 40*m**3*n + 10*m**3 + 50*m**2*n**3 + 105*
m**2*n**2 + 60*m**2*n + 10*m**2 + 24*m*n**4 + 100*m*n**3 + 105*m*n**2 + 40*
m*n + 5*m + 24*n**4 + 50*n**3 + 35*n**2 + 10*n + 1) + 4*A*c**3*m**3*x*(e*x)
**m/(m**5 + 10*m**4*n + 5*m**4 + 35*m**3*n**2 + 40*m**3*n + 10*m**3 + 50*m
**2*n**3 + 105*m**2*n**2 + 60*m**2*n + 10*m**2 + 24*m*n**4 + 100*m*n**3 + 10
5*m*n**2 + 40*m*n + 5*m + 24*n**4 + 50*n**3 + 35*n**2 + 10*n + 1) + 35*A*c*
**3*m**2*n**2*x*(e*x)**m/(m**5 + 10*m**4*n + 5*m**4 + 35*m**3*n**2 + 40*m**3
*n + 10*m**3 + 50*m**2*n**3 + 105*m**2*n**2 + 60*m**2*n + 10*m**2 + 24*m*n
**4 + 100*m*n**3 + 105*m*n**2 + 40*m*n + 5*m + 24*n**4 + 50*n**3 + 35*n**2 +
10*n + 1) + 30*A*c**3*m**2*n*x*(e*x)**m/(m**5 + 10*m**4*n + 5*m**4 + 35*m
**3*n**2 + 40*m**3*n + 10*m**3 + 50*m**2*n**3 + 105*m**2*n**2 + 60*m**2*n +
10*m**2 + 24*m*n**4 + 100*m*n**3 + 105*m*n**2 + ...

```

**Giac** [B] Leaf count of result is larger than twice the leaf count of optimal. 2278 vs. 2(141) = 282.

time = 1.89, size = 2278, normalized size = 16.63

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^3,x, algorithm="giac")
```

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[Out] (B*d^3*m^4*x*x^m*x^(4*n)*e^m + 6*B*d^3*m^3*n*x*x^m*x^(4*n)*e^m + 11*B*d^3*m
^2*n^2*x*x^m*x^(4*n)*e^m + 6*B*d^3*m*n^3*x*x^m*x^(4*n)*e^m + 3*B*c*d^2*m^4
*x*x^m*x^(3*n)*e^m + A*d^3*m^4*x*x^m*x^(3*n)*e^m + 21*B*c*d^2*m^3*n*x*x^m*x
^(3*n)*e^m + 7*A*d^3*m^3*n*x*x^m*x^(3*n)*e^m + 42*B*c*d^2*m^2*n^2*x*x^m*x^(3
*n)*e^m + 14*A*d^3*m^2*n^2*x*x^m*x^(3*n)*e^m + 24*B*c*d^2*m*n^3*x*x^m*x^(3*
n)*e^m + 8*A*d^3*m*n^3*x*x^m*x^(3*n)*e^m + 3*B*c^2*d*m^4*x*x^m*x^(2*n)*e^m
+ 3*A*c*d^2*m^4*x*x^m*x^(2*n)*e^m + 24*B*c^2*d*m^3*n*x*x^m*x^(2*n)*e^m + 24
*A*c*d^2*m^3*n*x*x^m*x^(2*n)*e^m + 57*B*c^2*d*m^2*n^2*x*x^m*x^(2*n)*e^m + 5
7*A*c*d^2*m^2*n^2*x*x^m*x^(2*n)*e^m + 36*B*c^2*d*m*n^3*x*x^m*x^(2*n)*e^m +
36*A*c*d^2*m*n^3*x*x^m*x^(2*n)*e^m + B*c^3*m^4*x*x^m*x^n*e^m + 3*A*c^2*d*m^
4*x*x^m*x^n*e^m + 9*B*c^3*m^3*n*x*x^m*x^n*e^m + 27*A*c^2*d*m^3*n*x*x^m*x^n*
e^m + 26*B*c^3*m^2*n^2*x*x^m*x^n*e^m + 78*A*c^2*d*m^2*n^2*x*x^m*x^n*e^m + 2
4*B*c^3*m*n^3*x*x^m*x^n*e^m + 72*A*c^2*d*m*n^3*x*x^m*x^n*e^m + A*c^3*m^4*x*
x^m*e^m + 10*A*c^3*m^3*n*x*x^m*e^m + 35*A*c^3*m^2*n^2*x*x^m*e^m + 50*A*c^3*
m*n^3*x*x^m*e^m + 24*A*c^3*n^4*x*x^m*e^m + 4*B*d^3*m^3*x*x^m*x^(4*n)*e^m +
18*B*d^3*m^2*n*x*x^m*x^(4*n)*e^m + 22*B*d^3*m*n^2*x*x^m*x^(4*n)*e^m + 6*B*d
^3*n^3*x*x^m*x^(4*n)*e^m + 12*B*c*d^2*m^3*x*x^m*x^(3*n)*e^m + 4*A*d^3*m^3*x
*x^m*x^(3*n)*e^m + 63*B*c*d^2*m^2*n*x*x^m*x^(3*n)*e^m + 21*A*d^3*m^2*n*x*x^
m*x^(3*n)*e^m + 84*B*c*d^2*m*n^2*x*x^m*x^(3*n)*e^m + 28*A*d^3*m*n^2*x*x^m*x
^(3*n)*e^m + 24*B*c*d^2*n^3*x*x^m*x^(3*n)*e^m + 8*A*d^3*n^3*x*x^m*x^(3*n)*e
^m + 12*B*c^2*d*m^3*x*x^m*x^(2*n)*e^m + 12*A*c*d^2*m^3*x*x^m*x^(2*n)*e^m +
72*B*c^2*d*m^2*n*x*x^m*x^(2*n)*e^m + 72*A*c*d^2*m^2*n*x*x^m*x^(2*n)*e^m + 1
14*B*c^2*d*m*n^2*x*x^m*x^(2*n)*e^m + 114*A*c*d^2*m*n^2*x*x^m*x^(2*n)*e^m +

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$$\begin{aligned}
& 36*B*c^2*d^n^3*x*x^m*x^(2*n)*e^m + 36*A*c*d^2*n^3*x*x^m*x^(2*n)*e^m + 4*B*c \\
& ^3*m^3*x*x^m*x^n*e^m + 12*A*c^2*d*m^3*x*x^m*x^n*e^m + 27*B*c^3*m^2*n*x*x^m* \\
& x^n*e^m + 81*A*c^2*d*m^2*n*x*x^m*x^n*e^m + 52*B*c^3*m*n^2*x*x^m*x^n*e^m + 1 \\
& 56*A*c^2*d*m*n^2*x*x^m*x^n*e^m + 24*B*c^3*n^3*x*x^m*x^n*e^m + 72*A*c^2*d*n^ \\
& 3*x*x^m*x^n*e^m + 4*A*c^3*m^3*x*x^m*e^m + 30*A*c^3*m^2*n*x*x^m*e^m + 70*A*c \\
& ^3*m*n^2*x*x^m*e^m + 50*A*c^3*n^3*x*x^m*e^m + 6*B*d^3*m^2*x*x^m*x^(4*n)*e^m \\
& + 18*B*d^3*m*n*x*x^m*x^(4*n)*e^m + 11*B*d^3*n^2*x*x^m*x^(4*n)*e^m + 18*B*c \\
& *d^2*m^2*x*x^m*x^(3*n)*e^m + 6*A*d^3*m^2*x*x^m*x^(3*n)*e^m + 63*B*c*d^2*m*n \\
& *x*x^m*x^(3*n)*e^m + 21*A*d^3*m*n*x*x^m*x^(3*n)*e^m + 42*B*c*d^2*n^2*x*x^m* \\
& x^(3*n)*e^m + 14*A*d^3*n^2*x*x^m*x^(3*n)*e^m + 18*B*c^2*d*m^2*x*x^m*x^(2*n) \\
& *e^m + 18*A*c*d^2*m^2*x*x^m*x^(2*n)*e^m + 72*B*c^2*d*m*n*x*x^m*x^(2*n)*e^m \\
& + 72*A*c*d^2*m*n*x*x^m*x^(2*n)*e^m + 57*B*c^2*d*n^2*x*x^m*x^(2*n)*e^m + 57* \\
& A*c*d^2*n^2*x*x^m*x^(2*n)*e^m + 6*B*c^3*m^2*x*x^m*x^n*e^m + 18*A*c^2*d*m^2* \\
& x*x^m*x^n*e^m + 27*B*c^3*m*n*x*x^m*x^n*e^m + 81*A*c^2*d*m*n*x*x^m*x^n*e^m + \\
& 26*B*c^3*n^2*x*x^m*x^n*e^m + 78*A*c^2*d*n^2*x*x^m*x^n*e^m + 6*A*c^3*m^2*x* \\
& x^m*e^m + 30*A*c^3*m*n*x*x^m*e^m + 35*A*c^3*n^2*x*x^m*e^m + 4*B*d^3*m*x*x^m \\
& *x^(4*n)*e^m + 6*B*d^3*n*x*x^m*x^(4*n)*e^m + 12*B*c*d^2*m*x*x^m*x^(3*n)*e^m \\
& + 4*A*d^3*m*x*x^m*x^(3*n)*e^m + 21*B*c*d^2*n*x*x^m*x^(3*n)*e^m + 7*A*d^3*n \\
& *x*x^m*x^(3*n)*e^m + 12*B*c^2*d*m*x*x^m*x^(2*n)*e^m + 12*A*c*d^2*m*x*x^m*x^ \\
& (2*n)*e^m + 24*B*c^2*d*n*x*x^m*x^(2*n)*e^m + 24*A*c*d^2*n*x*x^m*x^(2*n)*e^m \\
& + 4*B*c^3*m*x*x^m*x^n*e^m + 12*A*c^2*d*m*x*x^m*x^n*e^m + 9*B*c^3*n*x*x^m*x \\
& ^n*e^m + 27*A*c^2*d*n*x*x^m*x^n*e^m + 4*A*c^3*m*x*x^m*e^m + 10*A*c^3*n*x*x^ \\
& m*e^m + B*d^3*x*x^m*x^(4*n)*e^m + 3*B*c*d^2*x*x^m*x^(3*n)*e^m + A*d^3*x*x^m \\
& *x^(3*n)*e^m + 3*B*c^2*d*x*x^m*x^(2*n)*e^m + 3*A*c*d^2*x*x^m*x^(2*n)*e^m + \\
& B*c^3*x*x^m*x^n*e^m + 3*A*c^2*d*x*x^m*x^n*e^m + A*c^3*x*x^m*e^m)/(m^5 + 10* \\
& m^4*n + 35*m^3*n^2 + 50*m^2*n^3 + 24*m*n^4 + 5*m^4 + 40*m^3*n + 105*m^2*n^2 \\
& + 100*m*n^3 + 24*n^4 + 10*m^3 + 60*m^2*n + 105*m*n^2 + 50*n^3 + 10*m^2 + 4 \\
& 0*m*n + 35*n^2 + 5*m + 10*n + 1)
\end{aligned}$$

Mupad [B]

time = 5.31, size = 563, normalized size = 4.11

$\frac{d}{dx} \int (e^x)^m (A + Bx^n)(c + dx^n)^3 dx = (e^x)^m (A + Bx^n)(c + dx^n)^3$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3,x)

[Out] (A\*c^3\*x\*(e\*x)^m)/(m + 1) + (d^2\*x\*x^(3\*n)\*(e\*x)^m\*(A\*d + 3\*B\*c)\*(3\*m + 7\*n + 14\*m\*n + 14\*m\*n^2 + 7\*m^2\*n + 3\*m^2 + m^3 + 14\*n^2 + 8\*n^3 + 1))/(4\*m + 10\*n + 30\*m\*n + 70\*m\*n^2 + 30\*m^2\*n + 50\*m\*n^3 + 10\*m^3\*n + 6\*m^2 + 4\*m^3 + m^4 + 35\*n^2 + 50\*n^3 + 24\*n^4 + 35\*m^2\*n^2 + 1) + (c^2\*x\*x^n\*(e\*x)^m\*(3\*A\*d + B\*c)\*(3\*m + 9\*n + 18\*m\*n + 26\*m\*n^2 + 9\*m^2\*n + 3\*m^2 + m^3 + 26\*n^2 + 24\*n^3 + 1))/(4\*m + 10\*n + 30\*m\*n + 70\*m\*n^2 + 30\*m^2\*n + 50\*m\*n^3 + 10\*m^3\*n + 6\*m^2 + 4\*m^3 + m^4 + 35\*n^2 + 50\*n^3 + 24\*n^4 + 35\*m^2\*n^2 + 1) + (B\*d^3\*x\*x^(4\*n)\*(e\*x)^m\*(3\*m + 6\*n + 12\*m\*n + 11\*m\*n^2 + 6\*m^2\*n + 3\*m^2 + m

$$\begin{aligned} & \left( m^3 + 11n^2 + 6n^3 + 1 \right) / \left( 4m + 10n + 30mn + 70m^2n + 30m^2n + 50m \right. \\ & \left. n^3 + 10m^3n + 6m^2 + 4m^3 + m^4 + 35n^2 + 50n^3 + 24n^4 + 35m^2n \right. \\ & \left. ^2 + 1 \right) + \left( 3cdx^2(e^x)^m(A^d + B^c) \left( 3m + 8n + 16mn + 19m^2n \right. \right. \\ & \left. \left. + 8m^2n + 3m^2 + m^3 + 19n^2 + 12n^3 + 1 \right) \right) / \left( 4m + 10n + 30mn + 7 \right. \\ & \left. 0m^2n + 30m^2n + 50mn^3 + 10m^3n + 6m^2 + 4m^3 + m^4 + 35n^2 + 5 \right. \\ & \left. 0n^3 + 24n^4 + 35m^2n^2 + 1 \right) \end{aligned}$$

$$3.19 \quad \int \frac{(ex)^m (A+Bx^n)(c+dx^n)^3}{a+bx^n} dx$$

**Optimal.** Leaf size=270

$$\frac{d(a^2Bd^2 + 3b^2c(Bc + Ad) - abd(3Bc + Ad))x^{1+n}(ex)^m}{b^3(1+m+n)} + \frac{d^2(3bBc + Abd - aBd)x^{1+2n}(ex)^m}{b^2(1+m+2n)} + \frac{Bd^3x^{1+3n}(ex)^m}{b(1+m+3n)}$$

[Out]  $d*(a^2*B*d^2+3*b^2*c*(A*d+B*c)-a*b*d*(A*d+3*B*c))*x^{(1+n)}*(e*x)^m/b^3/(1+m+n)+d^2*(A*b*d-B*a*d+3*B*b*c)*x^{(1+2*n)}*(e*x)^m/b^2/(1+m+2*n)+B*d^3*x^{(1+3*n)}*(e*x)^m/b/(1+m+3*n)-(a^3*B*d^3+3*a*b^2*c*d*(A*d+B*c)-a^2*b*d^2*(A*d+3*B*c)-b^3*c^2*(3*A*d+B*c))*(e*x)^{(1+m)}/b^4/e/(1+m)+(A*b-B*a)*(-a*d+b*c)^3*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/a/b^4/e/(1+m)$

**Rubi [A]**

time = 0.26, antiderivative size = 270, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.129$ , Rules used = {584, 20, 30, 371}

$$\frac{dx^{m+1}(ex)^m(a^2Bd^2 - abd(Ad+3Bc) + 3b^2c(Ad+Bc))}{b^{m+1}(m+n+1)} - \frac{(ex)^{m+1}(a^3Bd^3 - a^2bd^2(Ad+3Bc) + 3ab^2c(Ad+Bc) + b^3(-c^2)(3Ad+Bc))}{b^{m+1}(m+1)} + \frac{(ex)^{m+1}(Ab-aD)(bc-ad)^3 {}_2F_1(1, \frac{m+1}{n}, \frac{m+n+1}{n}, -\frac{bx^n}{a})}{ab^m c(m+1)} + \frac{d^2 x^{2m+1}(ex)^m(-aBd+Abd+3bBc)}{b^{m+2n+1}} + \frac{Bd^3 x^{3m+1}(ex)^m}{b^{m+3n+1}}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3)/(a + b\*x^n), x]

[Out]  $(d*(a^2*B*d^2 + 3*b^2*c*(B*c + A*d) - a*b*d*(3*B*c + A*d))*x^{(1+n)}*(e*x)^m/(b^3*c*(1+m+n)) + (d^2*(3*b*B*c + A*b*d - a*B*d)*x^{(1+2*n)}*(e*x)^m/(b^2*(1+m+2*n)) + (B*d^3*x^{(1+3*n)}*(e*x)^m)/(b*(1+m+3*n)) - ((a^3*B*d^3 + 3*a*b^2*c*d*(B*c + A*d) - a^2*b*d^2*(3*B*c + A*d) - b^3*c^2*(B*c + 3*A*d))*(e*x)^{(1+m)}/(b^4*e*(1+m)) + ((A*b - a*B)*(b*c - a*d)^3*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((b*x^n)/a)])/(a*b^4*e*(1+m))$

**Rule 20**

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_.)\*((b\_.)\*(v\_))^(n\_.), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

**Rule 30**

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && N eQ[m, -1]

**Rule 371**

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1



, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

### Rule 584

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_.)\*((e\_) + (f\_.)\*(x\_)^(n\_))^(r\_.), x\_Symbol] :> Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)(c + dx^n)^3}{a + bx^n} dx &= \int \left( \frac{(-a^3 Bd^3 - 3ab^2 cd(Bc + Ad) + a^2 bd^2(3Bc + Ad) + b^3 c^2(Bc + 3Ad))}{b^4} \right. \\ &= -\frac{(a^3 Bd^3 + 3ab^2 cd(Bc + Ad) - a^2 bd^2(3Bc + Ad) - b^3 c^2(Bc + 3Ad))}{b^4 e(1 + m)} \\ &= -\frac{(a^3 Bd^3 + 3ab^2 cd(Bc + Ad) - a^2 bd^2(3Bc + Ad) - b^3 c^2(Bc + 3Ad))}{b^4 e(1 + m)} \\ &= \frac{d(a^2 Bd^2 + 3b^2 c(Bc + Ad) - abd(3Bc + Ad)) x^{1+n} (ex)^m}{b^3(1 + m + n)} + \frac{d^2(3bBc + 3ad^2)}{b^3(1 + m + n)} \end{aligned}$$

### Mathematica [A]

time = 0.59, size = 212, normalized size = 0.79

$$x(ex)^m \left( -\frac{(-Ab + aB)(-bc + ad)^3}{ab^4(1 + m)} + \frac{Ac^3}{a + am} + \frac{d(a^2 Bd^2 + 3b^2 c(Bc + Ad) - abd(3Bc + Ad)) x^n}{b^3(1 + m + n)} + \frac{d^2(3bBc + Abd - aBd)x^{2n}}{b^2(1 + m + 2n)} + \frac{Bd^2 x^{3n}}{b + bm + 3bn} + \frac{(-Ab + aB)(-bc + ad)^3 {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bc^n}{a}\right)}{ab^4(1 + m)} \right)$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3)/(a + b\*x^n), x]

[Out] x\*(e\*x)^m\*(-(((-(A\*b) + a\*B)\*(-b\*c) + a\*d)^3)/(a\*b^4\*(1 + m))) + (A\*c^3)/(a + a\*m) + (d\*(a^2\*B\*d^2 + 3\*b^2\*c\*(B\*c + A\*d) - a\*b\*d\*(3\*B\*c + A\*d))\*x^n)/(b^3\*(1 + m + n)) + (d^2\*(3\*b\*B\*c + A\*b\*d - a\*B\*d)\*x^(2\*n))/(b^2\*(1 + m + 2\*n)) + (B\*d^3\*x^(3\*n))/(b + b\*m + 3\*b\*n) + (((-(A\*b) + a\*B)\*(-b\*c) + a\*d)^3\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)])/(a\*b^4\*(1 + m))

### Maple [F]

time = 0.10, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)(c + dx^n)^3}{a + bx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A+B*x^n)*(c+d*x^n)^3/(a+b*x^n),x)$

[Out]  $\text{int}((e*x)^m*(A+B*x^n)*(c+d*x^n)^3/(a+b*x^n),x)$

**Maxima** [F]

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e*x)^m*(A+B*x^n)*(c+d*x^n)^3/(a+b*x^n),x, \text{algorithm}="maxima")$

[Out]  $((b^4*c^3*e^m - 3*a*b^3*c^2*d*e^m + 3*a^2*b^2*c*d^2*e^m - a^3*b*d^3*e^m)*A - (a*b^3*c^3*e^m - 3*a^2*b^2*c^2*d*e^m + 3*a^3*b*c*d^2*e^m - a^4*d^3*e^m)*B) * \text{integrate}(x^m/(b^5*x^n + a*b^4), x) + ((m^3*e^m + 3*m^2*(n + 1)*e^m + (2*n^2 + 6*n + 3)*m*e^m + (2*n^2 + 3*n + 1)*e^m)*B*b^3*d^3*x*e^{(m*\log(x) + 3*n*\log(x))} + ((3*(m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*b^3*c^2*d - 3*(m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a*b^2*c*d^2 + (m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a^2*b*d^3)*A + ((m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*b^3*c^3 - 3*(m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a*b^2*c^2*d + 3*(m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a^2*b*c*d^2 - (m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a^3*d^3)*B)*x*x^m + ((m^3*e^m + m^2*(4*n + 3)*e^m + (3*n^2 + 8*n + 3)*m*e^m + (3*n^2 + 4*n + 1)*e^m)*A*b^3*d^3 + (3*(m^3*e^m + m^2*(4*n + 3)*e^m + (3*n^2 + 8*n + 3)*m*e^m + (3*n^2 + 4*n + 1)*e^m)*b^3*c*d^2 - (m^3*e^m + m^2*(4*n + 3)*e^m + (3*n^2 + 8*n + 3)*m*e^m + (3*n^2 + 4*n + 1)*e^m)*a*b^2*d^3)*B)*x*e^{(m*\log(x) + 2*n*\log(x))} + ((3*(m^3*e^m + m^2*(5*n + 3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*b^3*c*d^2 - (m^3*e^m + m^2*(5*n + 3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*a*b^2*d^3)*A + (3*(m^3*e^m + m^2*(5*n + 3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*b^3*c^2*d - 3*(m^3*e^m + m^2*(5*n + 3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*a*b^2*c*d^2 + (m^3*e^m + m^2*(5*n + 3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*a^2*b*d^3)*B)*x*e^{(m*\log(x) + n*\log(x))}/((m^4 + 2*m^3*(3*n + 2) + (11*n^2 + 18*n + 6)*m^2 + 6*n^3 + 2*(3*n^3 + 11*n^2 + 9*n + 2)*m + 11*n^2 + 6*n + 1)*b^4)$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^3/(a+b*x^n),x, algorithm="fricas")
```

```
[Out] integral((B*d^3*x^(4*n) + A*c^3 + (3*B*c*d^2 + A*d^3)*x^(3*n) + 3*(B*c^2*d
+ A*c*d^2)*x^(2*n) + (B*c^3 + 3*A*c^2*d)*x^n)*(x*e)^m/(b*x^n + a), x)
```

**Sympy** [C] Result contains complex when optimal does not.

time = 23.38, size = 1503, normalized size = 5.57

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(A+B*x**n)*(c+d*x**n)**3/(a+b*x**n),x)
```

```
[Out] A*c**3*e**m*m*x*x**m*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1/n)*gamma
(m/n + 1/n)/(a*n**2*gamma(m/n + 1 + 1/n)) + A*c**3*e**m*m*x*x**m*lerchphi(b*x
**n*exp_polar(I*pi)/a, 1, m/n + 1/n)*gamma(m/n + 1/n)/(a*n**2*gamma(m/n + 1
+ 1/n)) + 3*A*c**2*d*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a,
1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + 3*A
*c**2*d*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/
n)*gamma(m/n + 1 + 1/n)/(a*n*gamma(m/n + 2 + 1/n)) + 3*A*c**2*d*e**m*m*x*x**m
*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 +
1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + 3*A*c*d**2*e**m*m*x*x**m*x**(2*n)*lerc
hphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n*
**2*gamma(m/n + 3 + 1/n)) + 6*A*c*d**2*e**m*m*x*x**m*x**(2*n)*lerchphi(b*x**n*
exp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n*gamma(m/n +
3 + 1/n)) + 3*A*c*d**2*e**m*m*x*x**m*x**(2*n)*lerchphi(b*x**n*exp_polar(I*pi)
/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n**2*gamma(m/n + 3 + 1/n)) +
A*d**3*e**m*m*x*x**m*x**(3*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 3
+ 1/n)*gamma(m/n + 3 + 1/n)/(a*n**2*gamma(m/n + 4 + 1/n)) + 3*A*d**3*e**m*
*x*x**m*x**(3*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 3 + 1/n)*gamma(
m/n + 3 + 1/n)/(a*n*gamma(m/n + 4 + 1/n)) + A*d**3*e**m*m*x*x**m*x**(3*n)*ler
chphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 3 + 1/n)*gamma(m/n + 3 + 1/n)/(a*n
**2*gamma(m/n + 4 + 1/n)) + B*c**3*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_p
olar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n**2*gamma(m/n + 2
+ 1/n)) + B*c**3*e**m*m*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n
+ 1 + 1/n)*gamma(m/n + 1 + 1/n)/(a*n*gamma(m/n + 2 + 1/n)) + B*c**3*e**m*m*
*x*x**m*x**n*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 1 + 1/n)*gamma(m/n +
1 + 1/n)/(a*n**2*gamma(m/n + 2 + 1/n)) + 3*B*c**2*d*e**m*m*x*x**m*x**(2*n)
*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/
(a*n**2*gamma(m/n + 3 + 1/n)) + 6*B*c**2*d*e**m*m*x*x**m*x**(2*n)*lerchphi(b*
x**n*exp_polar(I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n*gamma(m
/n + 3 + 1/n)) + 3*B*c**2*d*e**m*m*x*x**m*x**(2*n)*lerchphi(b*x**n*exp_polar(
I*pi)/a, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(a*n**2*gamma(m/n + 3 + 1/n
)) + 3*B*c*d**2*e**m*m*x*x**m*x**(3*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1
```

```
, m/n + 3 + 1/n)*gamma(m/n + 3 + 1/n)/(a*n**2*gamma(m/n + 4 + 1/n)) + 9*B*c
*d**2*e**m*x*x**m*x**(3*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 3 +
1/n)*gamma(m/n + 3 + 1/n)/(a*n*gamma(m/n + 4 + 1/n)) + 3*B*c*d**2*e**m*x*x*
*m*x**(3*n)*lerchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 3 + 1/n)*gamma(m/n
+ 3 + 1/n)/(a*n**2*gamma(m/n + 4 + 1/n)) + B*d**3*e**m*m*x*x**m*x**(4*n)*le
rchphi(b*x**n*exp_polar(I*pi)/a, 1, m/n + 4 + 1/n)*gamma(m/n + 4 + 1/n)/(a*
n**2*gamma(m/n + 5 + 1/n)) + 4*B*d**3*e**m*x*x**m*x**(4*n)*lerchphi(b*x**n*
exp_polar(I*pi)/a, 1, m/n + 4 + 1/n)*gamma(m/n + 4 + 1/n)/(a*n*gamma(m/n +
5 + 1/n)) + B*d**3*e**m*x*x**m*x**(4*n)*lerchphi(b*x**n*exp_polar(I*pi)/a,
1, m/n + 4 + 1/n)*gamma(m/n + 4 + 1/n)/(a*n**2*gamma(m/n + 5 + 1/n))
```

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)*(c+d*x^n)^3/(a+b*x^n),x, algorithm="giac")
```

```
[Out] integrate((B*x^n + A)*(d*x^n + c)^3*(x*e)^m/(b*x^n + a), x)
```

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)^3}{a + bx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(((e*x)^m*(A + B*x^n)*(c + d*x^n)^3)/(a + b*x^n),x)
```

```
[Out] int(((e*x)^m*(A + B*x^n)*(c + d*x^n)^3)/(a + b*x^n), x)
```

$$3.20 \quad \int \frac{(ex)^m (A+Bx^n)(c+dx^n)^3}{(a+bx^n)^2} dx$$

**Optimal.** Leaf size=394

$$\frac{d^2(Ab(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+2n) - ad(1+m+3n)))x^{1+n}(ex)^m}{ab^3n(1+m+n)} - \frac{d^3(Ab(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+2n) - ad(1+m+3n)))x^{1+n}(ex)^m}{ab^3n(1+m+n)}$$

[Out]  $-d^2(A*b*(3*b*c*(1+m+n)-a*d*(1+m+2*n))-a*B*(3*b*c*(1+m+2*n)-a*d*(1+m+3*n))$   
 $) * x^{(1+n)} * (e*x)^m / a / b^3 / n / (1+m+n) - d^3(A*b*(1+m+2*n)-a*B*(1+m+3*n)) * x^{(1+2*n)}$   
 $* (e*x)^m / a / b^2 / n / (1+m+2*n) - d*(A*b*(3*b^2*c^2*(1+m)-3*a*b*c*d*(1+m+n)+a^2*d^2*(1+m+2*n))$   
 $- a*B*(3*b^2*c^2*(1+m+n)-3*a*b*c*d*(1+m+2*n)+a^2*d^2*(1+m+3*n)) * (e*x)^{(1+m)} / a / b^4 / e / (1+m) / n + (A*b-B*a) * (e*x)^{(1+m)} * (c+d*x^n)^3 / a / b / e / n / (a$   
 $+b*x^n) - (-a*d+b*c)^2 * (A*b*(b*c*(1+m-n)-a*d*(1+m+2*n))-a*B*(b*c*(1+m)-a*d*(1+m+3*n))) * (e*x)^{(1+m)} * \text{hypergeom}([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a) / a^2 / b^4 / e / (1+m) / n$

**Rubi** [A]

time = 0.66, antiderivative size = 389, normalized size of antiderivative = 0.99, number of steps used = 8, number of rules used = 5, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.161$ , Rules used = {608, 584, 20, 30, 371}

(a^2\*x^m\*(b\*c - a\*d)^2\*F1[1, (3\*b\*c\*(1+m+n) - a\*d\*(1+m+2\*n)) - a\*B\*(3\*b\*c\*(1+m+2\*n) - a\*d\*(1+m+3\*n)) / (a\*b^3\*n\*(1+m+n)) - (d^3\*(A\*b\*(1+m+2\*n) - a\*B\*(1+m+3\*n)) / (b\*(1+m+2\*n)) \* x^(1+2\*n) \* (e\*x)^m) / (a\*b\*n) - (d\*(A\*b\*(3\*b^2\*c^2\*(1+m) - 3\*a\*b\*c\*d\*(1+m+n) + a^2\*d^2\*(1+m+2\*n)) - a\*B\*(3\*b^2\*c^2\*(1+m+n) - 3\*a\*b\*c\*d\*(1+m+2\*n) + a^2\*d^2\*(1+m+3\*n))) \* (e\*x)^(1+m) / (a\*b^4\*e\*(1+m)\*n) + ((A\*b - a\*B) \* (e\*x)^(1+m) \* (c + d\*x^n)^3) / (a\*b\*e\*n\*(a + b\*x^n)) - ((b\*c - a\*d)^2 \* (A\*b\*(b\*c\*(1+m-n) - a\*d\*(1+m+2\*n)) - a\*B\*(b\*c\*(1+m) - a\*d\*(1+m+3\*n))) \* (e\*x)^(1+m) \* Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(b\*x^n/a)] / (a^2\*b^4\*e\*(1+m)\*n)

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3)/(a + b\*x^n)^2,x]

[Out]  $-((d^2(A*b*(3*b*c*(1+m+n) - a*d*(1+m+2*n)) - a*B*(3*b*c*(1+m+2*n) - a*d*(1+m+3*n))) * x^{(1+n)} * (e*x)^m) / (a*b^3*n*(1+m+n)) - (d^3(A - (a*B*(1+m+3*n)) / (b*(1+m+2*n))) * x^{(1+2*n)} * (e*x)^m) / (a*b*n) - (d*(A*b*(3*b^2*c^2*(1+m) - 3*a*b*c*d*(1+m+n) + a^2*d^2*(1+m+2*n)) - a*B*(3*b^2*c^2*(1+m+n) - 3*a*b*c*d*(1+m+2*n) + a^2*d^2*(1+m+3*n))) * (e*x)^{(1+m)} / (a*b^4*e*(1+m)*n) + ((A*b - a*B) * (e*x)^{(1+m)} * (c + d*x^n)^3) / (a*b*e*n*(a + b*x^n)) - ((b*c - a*d)^2 * (A*b*(b*c*(1+m-n) - a*d*(1+m+2*n)) - a*B*(b*c*(1+m) - a*d*(1+m+3*n))) * (e*x)^{(1+m)} * Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(b*x^n/a)] / (a^2*b^4*e*(1+m)*n)$

**Rule 20**

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_)\*((b\_.)\*(v\_))^(n\_), x\_Symbol] :> Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

**Rule 30**

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && NeQ[m, -1]

### Rule 371

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p \* ((c\*x)^(m + 1)/(c\*(m + 1))) \* Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

### Rule 584

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_))^(r\_), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

### Rule 608

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_)), x\_Symbol] := Simp[(-b\*e - a\*f)\*(g\*x)^(m + 1)\*(a + b\*x^n)^(p + 1)\*((c + d\*x^n)^q/(a\*b\*g\*n\*(p + 1))), x] + Dist[1/(a\*b\*n\*(p + 1)), Int[(g\*x)^m\*(a + b\*x^n)^(p + 1)\*(c + d\*x^n)^(q - 1)\*Simp[c\*(b\*e\*n\*(p + 1) + (b\*e - a\*f)\*(m + 1) + d\*(b\*e\*n\*(p + 1) + (b\*e - a\*f)\*(m + n\*q + 1))\*x^n, x], x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b\*c - a\*d, b\*e - a\*f])

### Rubi steps

$$\begin{aligned}
 \int \frac{(ex)^m (A + Bx^n) (c + dx^n)^3}{(a + bx^n)^2} dx &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)^3}{aben (a + bx^n)} - \int \frac{(ex)^m (c + dx^n)^2 (-c(aB(1+m) - Ab(1+m-n)) + d(a + bx^n))}{a + bx^n} dx \\
 &= \frac{(Ab - aB)(ex)^{1+m} (c + dx^n)^3}{aben (a + bx^n)} - \int \left( \frac{d(Ab(3b^2c^2(1+m) - 3abcd(1+m+n) + a^2d^2(1+m+n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n))}{ab^4e(1+m+n)} \right) dx \\
 &= \frac{d(Ab(3b^2c^2(1+m) - 3abcd(1+m+n) + a^2d^2(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n))}{ab^4e(1+m+n)} \\
 &= \frac{d(Ab(3b^2c^2(1+m) - 3abcd(1+m+n) + a^2d^2(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n))}{ab^4e(1+m+n)} \\
 &= \frac{d^2(Ab(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n)) - aB(3bc(1+m+n) - ad(1+m+2n))}{ab^3n(1+m+n)}
 \end{aligned}$$

**Mathematica [A]**

time = 2.18, size = 345, normalized size = 0.88

$$\frac{x(ex)^m \left( \frac{b^2 d^2 (A b c - B c d)}{m(m+1)x^2} + a^2 B d^2 \left( \frac{3}{1+m} + \frac{a}{m+1 b x^n} \right) + a b d^2 \left( A d \left( -\frac{2}{1+m} - \frac{a}{m+1 b x^n} \right) + B \left( -\frac{6c}{1+m} - \frac{2d a^2}{1+m+n} - \frac{3c d}{m+1 b x^n} \right) \right) + b^2 d \left( A d \left( \frac{d a^2}{1+m+n} + 3c \left( \frac{1}{1+m} + \frac{a}{m+1 b x^n} \right) \right) + B \left( \frac{3 b d a^2}{1+m+n} + \frac{d^2 a^2}{1+m+2n} + 3c^2 \left( \frac{1}{1+m} + \frac{a}{m+1 b x^n} \right) \right) \right) - \frac{(b c - a d)^2 (A b c (1+m-n) - a d (1+m+2n)) + B (-b c (1+m) + a d (1+m+3n)) {}_2F_1 \left( 1, \frac{3 a^2 d^2 (A b c - B c d)}{m(m+1)x^2} \right)}{a^2 (1+m)n}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3)/(a + b\*x^n)^2,x]

[Out]  $(x*(e*x)^m*((b^3*c^2*(A*b*c - a*B*c - 3*a*A*d))/(a*n*(a + b*x^n)) + a^2*B*d^3*(3/(1 + m) + a/(a*n + b*n*x^n)) + a*b*d^2*(A*d*(-2/(1 + m) - a/(a*n + b*n*x^n)) + B*((-6*c)/(1 + m) - (2*d*x^n)/(1 + m + n) - (3*a*c)/(a*n + b*n*x^n))) + b^2*d*(A*d*((d*x^n)/(1 + m + n) + 3*c*((1 + m)^(-1) + a/(a*n + b*n*x^n))) + B*((3*c*d*x^n)/(1 + m + n) + (d^2*x^(2*n))/(1 + m + 2*n) + 3*c^2*((1 + m)^(-1) + a/(a*n + b*n*x^n)))) - ((b*c - a*d)^2*(A*b*(b*c*(1 + m - n) - a*d*(1 + m + 2*n)) + a*B*(-(b*c*(1 + m)) + a*d*(1 + m + 3*n)))*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(b*x^n)/a])/a^2*(1 + m)*n)/b^4$

**Maple [F]**

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)(c + dx^n)^3}{(a + bx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3/(a+b\*x^n)^2,x)

[Out] int((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3/(a+b\*x^n)^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3/(a+b\*x^n)^2,x, algorithm="maxima")

[Out]  $-(((m*e^m - (n - 1)*e^m)*b^4*c^3 - 3*(m*e^m + e^m)*a*b^3*c^2*d + 3*(m*e^m + (n + 1)*e^m)*a^2*b^2*c*d^2 - (m*e^m + (2*n + 1)*e^m)*a^3*b*d^3)*A - ((m*e^m + e^m)*a*b^3*c^3 - 3*(m*e^m + (n + 1)*e^m)*a^2*b^2*c^2*d + 3*(m*e^m + (2*n + 1)*e^m)*a^3*b*c*d^2 - (m*e^m + (3*n + 1)*e^m)*a^4*d^3)*B)*integrate(x^m/(a*b^5*n*x^n + a^2*b^4*n), x) + ((m^2*n*e^m + (n^2 + 2*n)*m*e^m + (n^2 + n)*e^m)*B*a*b^3*d^3*x*e^(m*log(x) + 3*n*log(x)) + (((m^3*e^m + 3*m^2*(n + 1)*e^m + (2*n^2 + 6*n + 3)*m*e^m + (2*n^2 + 3*n + 1)*e^m)*b^4*c^3 - 3*(m^3*e^m + 3*m^2*(n + 1)*e^m + (2*n^2 + 6*n + 3)*m*e^m + (2*n^2 + 3*n + 1)*e^m)*a*b^3*c^2*d + 3*(m^3*e^m + m^2*(4*n + 3)*e^m + (5*n^2 + 8*n + 3)*m*e^m + (2*n$

$$\begin{aligned} &^3 + 5n^2 + 4n + 1)e^m)a^2b^2cd^2 - (m^3e^m + m^2(5n + 3)e^m + ( \\ &8n^2 + 10n + 3)m^2e^m + (4n^3 + 8n^2 + 5n + 1)e^m)a^3bd^3)A - ((m \\ &^3e^m + 3m^2(n + 1)e^m + (2n^2 + 6n + 3)m^2e^m + (2n^2 + 3n + 1)e^ \\ &m)a^3c^3 - 3(m^3e^m + m^2(4n + 3)e^m + (5n^2 + 8n + 3)m^2e^m + ( \\ &2n^3 + 5n^2 + 4n + 1)e^m)a^2b^2c^2d + 3(m^3e^m + m^2(5n + 3)e^ \\ &m + (8n^2 + 10n + 3)m^2e^m + (4n^3 + 8n^2 + 5n + 1)e^m)a^3b^2cd^2 - \\ &(m^3e^m + 3m^2(2n + 1)e^m + (11n^2 + 12n + 3)m^2e^m + (6n^3 + 11n \\ &^2 + 6n + 1)e^m)a^4d^3)B)xx^m + ((m^2ne^m + 2(n^2 + n)m^2e^m + (2 \\ &n^2 + n)e^m)Aa^3bd^3 + (3(m^2ne^m + 2(n^2 + n)m^2e^m + (2n^2 + n \\ &)e^m)a^3cd^2 - (m^2ne^m + (3n^2 + 2n)m^2e^m + (3n^2 + n)e^m)a^2 \\ &b^2d^3)B)xe^{(m \log(x) + 2n \log(x))} + ((3(m^2ne^m + (3n^2 + 2n) \\ &m^2e^m + (2n^3 + 3n^2 + n)e^m)a^3cd^2 - (m^2ne^m + 2(2n^2 + n)m \\ &^2e^m + (4n^3 + 4n^2 + n)e^m)a^2b^2d^3)A + (3(m^2ne^m + (3n^2 + 2 \\ &n)m^2e^m + (2n^3 + 3n^2 + n)e^m)a^3c^2d - 3(m^2ne^m + 2(2n^2 \\ &+ n)m^2e^m + (4n^3 + 4n^2 + n)e^m)a^2b^2cd^2 + (m^2ne^m + (5n^2 + \\ &2n)m^2e^m + (6n^3 + 5n^2 + n)e^m)a^3bd^3)B)xe^{(m \log(x) + n \log(x))} \\ &)/((m^3n + 3(n^2 + n)m^2 + 2n^3 + (2n^3 + 6n^2 + 3n)m + 3n^2 + \\ &n)a^5x^n + (m^3n + 3(n^2 + n)m^2 + 2n^3 + (2n^3 + 6n^2 + 3n)m + \\ &3n^2 + n)a^2b^4) \end{aligned}$$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3/(a+b\*x^n)^2,x, algorithm="fricas")

[Out] integral((B\*d^3\*x^(4\*n) + A\*c^3 + (3\*B\*c\*d^2 + A\*d^3)\*x^(3\*n) + 3\*(B\*c^2\*d + A\*c\*d^2)\*x^(2\*n) + (B\*c^3 + 3\*A\*c^2\*d)\*x^n)\*(x\*e)^m/(b^2\*x^(2\*n) + 2\*a\*b\*x^n + a^2), x)

**Sympy** [F(-2)]

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*3/(a+b\*x\*\*n)\*\*2,x)

[Out] Exception raised: HeuristicGCDFailed >> no luck

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate



Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)\*(c+d\*x^n)^3/(a+b\*x^n)^2,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(d\*x^n + c)^3\*(x\*e)^m/(b\*x^n + a)^2, x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (c + dx^n)^3}{(a + bx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3)/(a + b\*x^n)^2,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(c + d\*x^n)^3)/(a + b\*x^n)^2, x)

$$3.21 \quad \int \frac{(ex)^m (a+bx^n)^4 (A+Bx^n)}{c+dx^n} dx$$

**Optimal.** Leaf size=380

$$\frac{b(4a^3Bd^3 - b^3c^2(Bc - Ad) + 4ab^2cd(Bc - Ad) - 6a^2bd^2(Bc - Ad)) x^{1+n} (ex)^m}{d^4(1+m+n)} + \frac{b^2(6a^2Bd^2 + b^2c(Bc - Ad))}{d^3(1+m)}$$

[Out]  $b*(4*a^3*B*d^3 - b^3*c^2*(-A*d+B*c) + 4*a*b^2*c*d*(-A*d+B*c) - 6*a^2*b*d^2*(-A*d+B*c))*x^{(1+n)}*(e*x)^m/d^4/(1+m+n) + b^2*(6*a^2*B*d^2 + b^2*c*(Bc - Ad) - 4*a*b*d*(-A*d+B*c))*x^{(1+2*n)}*(e*x)^m/d^3/(1+m+2*n) - b^3*(-A*b*d - 4*B*a*d + B*b*c)*x^{(1+3*n)}*(e*x)^m/d^2/(1+m+3*n) + b^4*B*x^{(1+4*n)}*(e*x)^m/d/(1+m+4*n) + (a^4*B*d^4 + b^4*c^3*(-A*d+B*c) - 4*a*b^3*c^2*d*(-A*d+B*c) + 6*a^2*b^2*c*d^2*(-A*d+B*c) - 4*a^3*b*d^3*(-A*d+B*c))*(e*x)^{(1+m)}/d^5/e/(1+m) - (-a*d+b*c)^4*(-A*d+B*c)*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c/d^5/e/(1+m)$

**Rubi [A]**

time = 0.41, antiderivative size = 380, normalized size of antiderivative = 1.00, number of steps used = 11, number of rules used = 4, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.129$ , Rules used = {584, 20, 30, 371}

$$\frac{b^2 e^{m+1} (a^2 B d^2 - 4 a b d c - A d) + b^2 c (B c - A d)}{d^2 (m+2n+1)} + \frac{b^{m+1} (a^2 B d^2 - 4 a^2 b d^2 (B c - A d) + 4 a b^2 d (B c - A d) + b^2 c^2 (B c - A d))}{d^2 (m+n+1)} + \frac{(e x)^{m+1} (a^2 B d^2 - 4 a^2 b d^2 (B c - A d) + 6 a^2 b^2 d^2 (B c - A d) - 4 a b^3 d^2 (B c - A d) + b^2 c^2 (B c - A d))}{d^2 (m+1)} - \frac{b^2 e^{m+1} (a x)^m (-4 a B d - A b d + b^2 c)}{d^2 (m+3n+1)} - \frac{(e x)^{m+1} (b c - a d)^m (B c - A d) F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{d x^n}{c}\right)}{c d^2 (m+1)} + \frac{b^2 B e^{m+1} (e x)^m}{d^2 (m+4n+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)^4\*(A + B\*x^n))/(c + d\*x^n), x]

[Out]  $(b*(4*a^3*B*d^3 - b^3*c^2*(B*c - A*d) + 4*a*b^2*c*d*(B*c - A*d) - 6*a^2*b*d^2*(B*c - A*d))*x^{(1+n)}*(e*x)^m/(d^4*(1+m+n)) + (b^2*(6*a^2*B*d^2 + b^2*c*(B*c - A*d) - 4*a*b*d*(B*c - A*d))*x^{(1+2*n)}*(e*x)^m/(d^3*(1+m+2*n)) - (b^3*(b*B*c - A*b*d - 4*a*B*d)*x^{(1+3*n)}*(e*x)^m/(d^2*(1+m+3*n)) + (b^4*B*x^{(1+4*n)}*(e*x)^m)/(d*(1+m+4*n)) + ((a^4*B*d^4 + b^4*c^3*(B*c - A*d) - 4*a*b^3*c^2*d*(B*c - A*d) + 6*a^2*b^2*c*d^2*(B*c - A*d) - 4*a^3*b*d^3*(B*c - A*d))*(e*x)^{(1+m)}/(d^5*e*(1+m)) - ((b*c - a*d)^4*(B*c - A*d)*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(d*x^n/c)])/(c*d^5*e*(1+m))$

**Rule 20**

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_)\*((b\_.)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

**Rule 30**

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]



**Maple [F]**

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^4 (A + Bx^n)}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^4\*(A+B\*x^n)/(c+d\*x^n),x)

[Out] int((e\*x)^m\*(a+b\*x^n)^4\*(A+B\*x^n)/(c+d\*x^n),x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^4\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="maxima")

[Out] ((b^4\*c^4\*d\*e^m - 4\*a\*b^3\*c^3\*d^2\*e^m + 6\*a^2\*b^2\*c^2\*d^3\*e^m - 4\*a^3\*b\*c\*d^4\*e^m + a^4\*d^5\*e^m)\*A - (b^4\*c^5\*e^m - 4\*a\*b^3\*c^4\*d\*e^m + 6\*a^2\*b^2\*c^3\*d^2\*e^m - 4\*a^3\*b\*c^2\*d^3\*e^m + a^4\*c\*d^4\*e^m)\*B)\*integrate(x^m/(d^6\*x^n + c\*d^5), x) + ((m^4\*e^m + 2\*m^3\*(3\*n + 2)\*e^m + (11\*n^2 + 18\*n + 6)\*m^2\*e^m + 2\*(3\*n^3 + 11\*n^2 + 9\*n + 2)\*m\*e^m + (6\*n^3 + 11\*n^2 + 6\*n + 1)\*e^m)\*B\*b^4\*d^4\*x\*e^(m\*log(x) + 4\*n\*log(x)) - (((m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*b^4\*c^3\*d - 4\*(m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*a\*b^3\*c^2\*d^2 + 6\*(m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*a^2\*b^2\*c\*d^3 - 4\*(m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*a^3\*b\*d^4)\*A - ((m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*b^4\*c^4 - 4\*(m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*a\*b^3\*c^3\*d + 6\*(m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*a^2\*b^2\*c^2\*d^2 - 4\*(m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*a^3\*b\*c\*d^3 + (m^4\*e^m + 2\*m^3\*(5\*n + 2)\*e^m + (35\*n^2 + 30\*n + 6)\*m^2\*e^m + 2\*(25\*n^3 + 35\*n^2 + 15\*n + 2)\*m\*e^m + (24\*n^4 + 50\*n^3 + 35\*n^2 + 10\*n + 1)\*e^m)\*a^4\*d^4)\*B)\*x\*x^m + ((m^4\*e^m + m^3\*(7\*n + 4)\*e^m + (14\*n^2 + 21\*n + 6)\*m^2\*e^m + (8\*n^3 + 28\*n^2 + 21\*n

$$\begin{aligned}
& + 4)m^4e^m + (8n^3 + 14n^2 + 7n + 1)e^m)A^4b^4d^4 - ((m^4e^m + m^3(7n + 4)e^m + (14n^2 + 21n + 6)m^2e^m + (8n^3 + 28n^2 + 21n + 4)m^2e^m + (8n^3 + 14n^2 + 7n + 1)e^m)b^4c^3d^3 - 4(m^4e^m + m^3(7n + 4)e^m + (14n^2 + 21n + 6)m^2e^m + (8n^3 + 28n^2 + 21n + 4)m^2e^m + (8n^3 + 14n^2 + 7n + 1)e^m)a^3b^3d^4)B)xe^{(m\log(x) + 3n\log(x))} - \\
& ((m^4e^m + 4m^3(2n + 1)e^m + (19n^2 + 24n + 6)m^2e^m + 2(6n^3 + 19n^2 + 12n + 2)m^2e^m + (12n^3 + 19n^2 + 8n + 1)e^m)b^4c^3d^3 - 4(m^4e^m + 4m^3(2n + 1)e^m + (19n^2 + 24n + 6)m^2e^m + 2(6n^3 + 19n^2 + 12n + 2)m^2e^m + (12n^3 + 19n^2 + 8n + 1)e^m)a^3b^3d^4)A - ( \\
& (m^4e^m + 4m^3(2n + 1)e^m + (19n^2 + 24n + 6)m^2e^m + 2(6n^3 + 19n^2 + 12n + 2)m^2e^m + (12n^3 + 19n^2 + 8n + 1)e^m)b^4c^2d^2 - 4(m^4e^m + 4m^3(2n + 1)e^m + (19n^2 + 24n + 6)m^2e^m + 2(6n^3 + 19n^2 + 12n + 2)m^2e^m + (12n^3 + 19n^2 + 8n + 1)e^m)a^3b^3c^3d^3 + 6(m^4e^m + 4m^3(2n + 1)e^m + (19n^2 + 24n + 6)m^2e^m + 2(6n^3 + 19n^2 + 12n + 2)m^2e^m + (12n^3 + 19n^2 + 8n + 1)e^m)a^2b^2d^4)B) \\
& xe^{(m\log(x) + 2n\log(x))} + ((m^4e^m + m^3(9n + 4)e^m + (26n^2 + 27n + 6)m^2e^m + (24n^3 + 52n^2 + 27n + 4)m^2e^m + (24n^3 + 26n^2 + 9n + 1)e^m)b^4c^2d^2 - 4(m^4e^m + m^3(9n + 4)e^m + (26n^2 + 27n + 6)m^2e^m + (24n^3 + 52n^2 + 27n + 4)m^2e^m + (24n^3 + 26n^2 + 9n + 1)e^m)a^3b^3c^3d^3 + 6(m^4e^m + m^3(9n + 4)e^m + (26n^2 + 27n + 6)m^2e^m + (24n^3 + 52n^2 + 27n + 4)m^2e^m + (24n^3 + 26n^2 + 9n + 1)e^m)b^4c^3d^3 - 4(m^4e^m + m^3(9n + 4)e^m + (26n^2 + 27n + 6)m^2e^m + (24n^3 + 52n^2 + 27n + 4)m^2e^m + (24n^3 + 26n^2 + 9n + 1)e^m)a^3b^3c^2d^2 + 6(m^4e^m + m^3(9n + 4)e^m + (26n^2 + 27n + 6)m^2e^m + (24n^3 + 52n^2 + 27n + 4)m^2e^m + (24n^3 + 26n^2 + 9n + 1)e^m)a^2b^2c^3d^3 - 4(m^4e^m + m^3(9n + 4)e^m + (26n^2 + 27n + 6)m^2e^m + (24n^3 + 52n^2 + 27n + 4)m^2e^m + (24n^3 + 26n^2 + 9n + 1)e^m)a^3b^3d^4)B)xe^{(m\log(x) + n\log(x))})/(m^5 + 5m^4(2n + 1) + 5(7n^2 + 8n + 2)m^3 + 24n^4 + 5(10n^3 + 21n^2 + 12n + 2)m^2 + 50n^3 + (24n^4 + 100n^3 + 105n^2 + 40n + 5)m + 35n^2 + 10n + 1)d^5)
\end{aligned}$$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^4\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="fricas")

[Out] integral((B\*b^4\*x^(5\*n) + A\*a^4 + (4\*B\*a\*b^3 + A\*b^4)\*x^(4\*n) + 2\*(3\*B\*a^2\*b^2 + 2\*A\*a\*b^3)\*x^(3\*n) + 2\*(2\*B\*a^3\*b + 3\*A\*a^2\*b^2)\*x^(2\*n) + (B\*a^4 + 4\*A\*a^3\*b)\*x^n)\*(x\*e)^m/(d\*x^n + c), x)

**Sympy** [C] Result contains complex when optimal does not.

time = 44.64, size = 1921, normalized size = 5.06

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*4\*(A+B\*x\*\*n)/(c+d\*x\*\*n),x)

[Out]  $A*a^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1/n)*\text{gamma}(m/n + 1/n)/(c^{n+2}*\text{gamma}(m/n + 1 + 1/n)) + A*a^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1/n)*\text{gamma}(m/n + 1/n)/(c^{n+2}*\text{gamma}(m/n + 1 + 1/n)) + 4*A*a^{3}*b*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1 + 1/n)*\text{gamma}(m/n + 1 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 2 + 1/n)) + 4*A*a^{3}*b*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1 + 1/n)*\text{gamma}(m/n + 1 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 2 + 1/n)) + 4*A*a^{3}*b*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1 + 1/n)*\text{gamma}(m/n + 1 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 2 + 1/n)) + 6*A*a^{2}*b^{2}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 2 + 1/n)*\text{gamma}(m/n + 2 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 3 + 1/n)) + 12*A*a^{2}*b^{2}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 2 + 1/n)*\text{gamma}(m/n + 2 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 3 + 1/n)) + 6*A*a^{2}*b^{2}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 2 + 1/n)*\text{gamma}(m/n + 2 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 3 + 1/n)) + 4*A*a*b^{3}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 3 + 1/n)*\text{gamma}(m/n + 3 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 4 + 1/n)) + 12*A*a*b^{3}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 3 + 1/n)*\text{gamma}(m/n + 3 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 4 + 1/n)) + 4*A*a*b^{3}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 3 + 1/n)*\text{gamma}(m/n + 3 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 4 + 1/n)) + A*b^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 4 + 1/n)*\text{gamma}(m/n + 4 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 5 + 1/n)) + 4*A*b^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 4 + 1/n)*\text{gamma}(m/n + 4 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 5 + 1/n)) + A*b^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 4 + 1/n)*\text{gamma}(m/n + 4 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 5 + 1/n)) + B*a^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1 + 1/n)*\text{gamma}(m/n + 1 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 2 + 1/n)) + B*a^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1 + 1/n)*\text{gamma}(m/n + 1 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 2 + 1/n)) + B*a^{4}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 1 + 1/n)*\text{gamma}(m/n + 1 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 2 + 1/n)) + 4*B*a^{3}*b*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 2 + 1/n)*\text{gamma}(m/n + 2 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 3 + 1/n)) + 8*B*a^{3}*b*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 2 + 1/n)*\text{gamma}(m/n + 2 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 3 + 1/n)) + 4*B*a^{3}*b*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 2 + 1/n)*\text{gamma}(m/n + 2 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 3 + 1/n)) + 6*B*a^{2}*b^{2}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 3 + 1/n)*\text{gamma}(m/n + 3 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 4 + 1/n)) + 18*B*a^{2}*b^{2}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 3 + 1/n)*\text{gamma}(m/n + 3 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 4 + 1/n)) + 18*B*a^{2}*b^{2}*e^{m*x}*\text{lerchphi}(d*x^{n+1}/c, 1, m/n + 3 + 1/n)*\text{gamma}(m/n + 3 + 1/n)/(c^{n+2}*\text{gamma}(m/n + 4 + 1/n))$

```

**(3*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 3 + 1/n)*gamma(m/n + 3
+ 1/n)/(c*n*gamma(m/n + 4 + 1/n)) + 6*B*a**2*b**2*e**m*x*x**m*x**(3*n)*lerc
hphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 3 + 1/n)*gamma(m/n + 3 + 1/n)/(c*n*
*2*gamma(m/n + 4 + 1/n)) + 4*B*a*b**3*e**m*m*x*x**m*x**(4*n)*lerchphi(d*x**
n*exp_polar(I*pi)/c, 1, m/n + 4 + 1/n)*gamma(m/n + 4 + 1/n)/(c*n**2*gamma(m
/n + 5 + 1/n)) + 16*B*a*b**3*e**m*x*x**m*x**(4*n)*lerchphi(d*x**n*exp_polar
(I*pi)/c, 1, m/n + 4 + 1/n)*gamma(m/n + 4 + 1/n)/(c*n*gamma(m/n + 5 + 1/n))
+ 4*B*a*b**3*e**m*x*x**m*x**(4*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/
n + 4 + 1/n)*gamma(m/n + 4 + 1/n)/(c*n**2*gamma(m/n + 5 + 1/n)) + B*b**4*e
**m*m*x*x**m*x**(5*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 5 + 1/n)*g
amma(m/n + 5 + 1/n)/(c*n**2*gamma(m/n + 6 + 1/n)) + 5*B*b**4*e**m*x*x**m*x*
*(5*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 5 + 1/n)*gamma(m/n + 5 +
1/n)/(c*n*gamma(m/n + 6 + 1/n)) + B*b**4*e**m*x*x**m*x**(5*n)*lerchphi(d*x
**n*exp_polar(I*pi)/c, 1, m/n + 5 + 1/n)*gamma(m/n + 5 + 1/n)/(c*n**2*gamma
(m/n + 6 + 1/n))

```

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^4\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^4\*(x\*e)^m/(d\*x^n + c), x)

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^4}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^4)/(c + d\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^4)/(c + d\*x^n), x)

$$3.22 \quad \int \frac{(ex)^m (a+bx^n)^3 (A+Bx^n)}{c+dx^n} dx$$

**Optimal.** Leaf size=272

$$\frac{b(3a^2Bd^2 + b^2c(Bc - Ad) - 3abd(Bc - Ad))x^{1+n}(ex)^m}{d^3(1+m+n)} - \frac{b^2(bBc - Abd - 3aBd)x^{1+2n}(ex)^m}{d^2(1+m+2n)} + \frac{b^3Bx^{1+3n}(ex)^m}{d(1+m+3n)}$$

[Out]  $b*(3*a^2*B*d^2+b^2*c*(-A*d+B*c)-3*a*b*d*(-A*d+B*c))*x^{(1+n)}*(e*x)^m/d^3/(1+m+n)-b^2*(-A*b*d-3*B*a*d+B*b*c)*x^{(1+2*n)}*(e*x)^m/d^2/(1+m+2*n)+b^3*B*x^{(1+3*n)}*(e*x)^m/d/(1+m+3*n)+(a^3*B*d^3-b^3*c^2*(-A*d+B*c)+3*a*b^2*c*d*(-A*d+B*c)-3*a^2*b*d^2*(-A*d+B*c))*(e*x)^{(1+m)}/d^4/e/(1+m)+(-a*d+b*c)^3*(-A*d+B*c)*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c/d^4/e/(1+m)$

**Rubi [A]**

time = 0.27, antiderivative size = 272, normalized size of antiderivative = 1.00, number of steps used = 9, number of rules used = 4, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.129$ , Rules used = {584, 20, 30, 371}

$$\frac{bx^{n+1}(ex)^m(3a^2Bd^2-3abd(Bc-Ad)+b^2c(Bc-Ad))}{d^4(m+n+1)} + \frac{(ex)^{m+1}(a^3Bd^3-3a^2bd^2(Bc-Ad)+3ab^2cd(Bc-Ad)+b^3(-c^2)(Bc-Ad))}{d^4e(m+1)} - \frac{b^2x^{2n+1}(ex)^m(-3aBd-Abd+bBc)}{d^2(m+2n+1)} + \frac{(ex)^{m+1}(bc-ad)^2(Bc-Ad)}{cd^4e(m+1)} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+1}{n}; -\frac{dx^n}{c}\right) + \frac{b^3Bx^{3n+1}(ex)^m}{d(m+3n+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n))/(c + d\*x^n), x]

[Out]  $(b*(3*a^2*B*d^2 + b^2*c*(B*c - A*d) - 3*a*b*d*(B*c - A*d))*x^{(1+n)}*(e*x)^m)/(d^3*(1+m+n)) - (b^2*(b*B*c - A*b*d - 3*a*B*d)*x^{(1+2*n)}*(e*x)^m)/(d^2*(1+m+2*n)) + (b^3*B*x^{(1+3*n)}*(e*x)^m)/(d*(1+m+3*n)) + ((a^3*B*d^3 - b^3*c^2*(B*c - A*d) + 3*a*b^2*c*d*(B*c - A*d) - 3*a^2*b*d^2*(B*c - A*d))*(e*x)^{(1+m)})/(d^4*e*(1+m)) + ((b*c - a*d)^3*(B*c - A*d)*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)]/(c*d^4*e*(1+m))$

Rule 20

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_.)\*((b\_.)\*(v\_))^(n\_.), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

Rule 30

Int[(x\_)^(m\_.), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && N eQ[m, -1]

Rule 371

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1



, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

### Rule 584

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_.) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_.) + (d\_.)\*(x\_)^(n\_))^(q\_.)\*((e\_.) + (f\_.)\*(x\_)^(n\_))^(r\_.), x\_Symbol] := Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*(c + d\*x^n)^q\*(e + f\*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (a + bx^n)^3 (A + Bx^n)}{c + dx^n} dx &= \int \left( \frac{(a^3 B d^3 - b^3 c^2 (Bc - Ad) + 3ab^2 cd (Bc - Ad) - 3a^2 b d^2 (Bc - Ad))}{d^4} \right. \\ &= \frac{(a^3 B d^3 - b^3 c^2 (Bc - Ad) + 3ab^2 cd (Bc - Ad) - 3a^2 b d^2 (Bc - Ad)) (ex)^m}{d^4 e (1 + m)} \\ &= \frac{(a^3 B d^3 - b^3 c^2 (Bc - Ad) + 3ab^2 cd (Bc - Ad) - 3a^2 b d^2 (Bc - Ad)) (ex)^m}{d^4 e (1 + m)} \\ &= \frac{b(3a^2 B d^2 + b^2 c (Bc - Ad) - 3abd (Bc - Ad)) x^{1+n} (ex)^m}{d^3 (1 + m + n)} - \frac{b^2 (bBc - a^2 d)}{d^3 (1 + m + n)} \end{aligned}$$

### Mathematica [A]

time = 0.62, size = 213, normalized size = 0.78

$$x(ex)^m \left( -\frac{(bc-ad)^3(Bc-Ad)}{cd^4(1+m)} + \frac{a^3 A}{c+cm} + \frac{b(3a^2 B d^2 + b^2 c(Bc-Ad) + 3abd(-Bc+Ad))x^n}{d^3(1+m+n)} + \frac{b^2(-bBc+Abd+3aBd)x^{2n}}{d^2(1+m+2n)} + \frac{b^3 B x^{3n}}{d+dm+3dn} + \frac{(bc-ad)^3(Bc-Ad)}{cd^4(1+m)} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right) \right)$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n))/(c + d\*x^n), x]

[Out] x\*(e\*x)^m\*(-(((b\*c - a\*d)^3\*(B\*c - A\*d))/(c\*d^4\*(1 + m))) + (a^3\*A)/(c + c\*m) + (b\*(3\*a^2\*B\*d^2 + b^2\*c\*(B\*c - A\*d) + 3\*a\*b\*d\*(-(B\*c) + A\*d))\*x^n)/(d^3\*(1 + m + n)) + (b^2\*(-(b\*B\*c) + A\*b\*d + 3\*a\*B\*d)\*x^(2\*n))/(d^2\*(1 + m + 2\*n)) + (b^3\*B\*x^(3\*n))/(d + d\*m + 3\*d\*n) + ((b\*c - a\*d)^3\*(B\*c - A\*d)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)]/(c\*d^4\*(1 + m)))

### Maple [F]

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^3 (A + Bx^n)}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(a+b*x^n)^3*(A+B*x^n)/(c+d*x^n), x)$

[Out]  $\text{int}((e*x)^m*(a+b*x^n)^3*(A+B*x^n)/(c+d*x^n), x)$

**Maxima** [F]

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e*x)^m*(a+b*x^n)^3*(A+B*x^n)/(c+d*x^n), x, \text{algorithm}="maxima")$

[Out]  $-(b^3*c^3*d*e^m - 3*a*b^2*c^2*d^2*e^m + 3*a^2*b*c*d^3*e^m - a^3*d^4*e^m)*A - (b^3*c^4*e^m - 3*a*b^2*c^3*d*e^m + 3*a^2*b*c^2*d^2*e^m - a^3*c*d^3*e^m)*B*\text{integrate}(x^m/(d^5*x^n + c*d^4), x) + ((m^3*e^m + 3*m^2*(n+1)*e^m + (2*n^2 + 6*n + 3)*m*e^m + (2*n^2 + 3*n + 1)*e^m)*B*b^3*d^3*x*e^{(m*\log(x) + 3*n*\log(x))} + (((m^3*e^m + 3*m^2*(2*n+1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*b^3*c^2*d - 3*(m^3*e^m + 3*m^2*(2*n+1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a*b^2*c*d^2 + 3*(m^3*e^m + 3*m^2*(2*n+1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a^2*b*d^3)*A - ((m^3*e^m + 3*m^2*(2*n+1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*b^3*c^3 - 3*(m^3*e^m + 3*m^2*(2*n+1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a*b^2*c^2*d + 3*(m^3*e^m + 3*m^2*(2*n+1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a^2*b*c*d^2 - (m^3*e^m + 3*m^2*(2*n+1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*a*b^2*d^3)*B)*x*x^m + ((m^3*e^m + m^2*(4*n+3)*e^m + (3*n^2 + 8*n + 3)*m*e^m + (3*n^2 + 4*n + 1)*e^m)*A*b^3*d^3 - ((m^3*e^m + m^2*(4*n+3)*e^m + (3*n^2 + 8*n + 3)*m*e^m + (3*n^2 + 4*n + 1)*e^m)*b^3*c*d^2 - 3*(m^3*e^m + m^2*(4*n+3)*e^m + (3*n^2 + 8*n + 3)*m*e^m + (3*n^2 + 4*n + 1)*e^m)*a*b^2*d^3)*B)*x*e^{(m*\log(x) + 2*n*\log(x))} - (((m^3*e^m + m^2*(5*n+3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*b^3*c*d^2 - 3*(m^3*e^m + m^2*(5*n+3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*a*b^2*d^3)*A - ((m^3*e^m + m^2*(5*n+3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*b^3*c^2*d - 3*(m^3*e^m + m^2*(5*n+3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*a*b^2*c*d^2 + 3*(m^3*e^m + m^2*(5*n+3)*e^m + (6*n^2 + 10*n + 3)*m*e^m + (6*n^2 + 5*n + 1)*e^m)*a^2*b*d^3)*B)*x*e^{(m*\log(x) + n*\log(x))}/((m^4 + 2*m^3*(3*n+2) + (11*n^2 + 18*n + 6)*m^2 + 6*n^3 + 2*(3*n^3 + 11*n^2 + 9*n + 2)*m + 11*n^2 + 6*n + 1)*d^4)$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="fricas")

[Out] integral((B\*b^3\*x^(4\*n) + A\*a^3 + (3\*B\*a\*b^2 + A\*b^3)\*x^(3\*n) + 3\*(B\*a^2\*b + A\*a\*b^2)\*x^(2\*n) + (B\*a^3 + 3\*A\*a^2\*b)\*x^n)\*(x\*e)^m/(d\*x^n + c), x)

**Sympy** [C] Result contains complex when optimal does not.

time = 23.44, size = 1503, normalized size = 5.53

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*3\*(A+B\*x\*\*n)/(c+d\*x\*\*n),x)

[Out] A\*a\*\*3\*e\*\*m\*m\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*n\*\*2\*gamma(m/n + 1 + 1/n)) + A\*a\*\*3\*e\*\*m\*m\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*n\*\*2\*gamma(m/n + 1 + 1/n)) + 3\*A\*a\*\*2\*b\*e\*\*m\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*\*2\*gamma(m/n + 2 + 1/n)) + 3\*A\*a\*\*2\*b\*e\*\*m\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*gamma(m/n + 2 + 1/n)) + 3\*A\*a\*\*2\*b\*e\*\*m\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*\*2\*gamma(m/n + 2 + 1/n)) + 3\*A\*a\*b\*\*2\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(2\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 2 + 1/n)\*gamma(m/n + 2 + 1/n)/(c\*n\*\*2\*gamma(m/n + 3 + 1/n)) + 6\*A\*a\*b\*\*2\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(2\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 2 + 1/n)\*gamma(m/n + 2 + 1/n)/(c\*n\*gamma(m/n + 3 + 1/n)) + 3\*A\*a\*b\*\*2\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(2\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 2 + 1/n)\*gamma(m/n + 2 + 1/n)/(c\*n\*\*2\*gamma(m/n + 3 + 1/n)) + A\*b\*\*3\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(3\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 3 + 1/n)\*gamma(m/n + 3 + 1/n)/(c\*n\*\*2\*gamma(m/n + 4 + 1/n)) + 3\*A\*b\*\*3\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(3\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 3 + 1/n)\*gamma(m/n + 3 + 1/n)/(c\*n\*gamma(m/n + 4 + 1/n)) + A\*b\*\*3\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(3\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 3 + 1/n)\*gamma(m/n + 3 + 1/n)/(c\*n\*\*2\*gamma(m/n + 4 + 1/n)) + B\*a\*\*3\*e\*\*m\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*\*2\*gamma(m/n + 2 + 1/n)) + B\*a\*\*3\*e\*\*m\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*gamma(m/n + 2 + 1/n)) + B\*a\*\*3\*e\*\*m\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*\*2\*gamma(m/n + 2 + 1/n)) + 3\*B\*a\*\*2\*b\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(2\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 2 + 1/n)\*gamma(m/n + 2 + 1/n)/(c\*n\*\*2\*gamma(m/n + 3 + 1/n)) + 6\*B\*a\*\*2\*b\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(2\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 2 + 1/n)\*gamma(m/n + 2 + 1/n)/(c\*n\*gamma(m/n + 3 + 1/n)) + 3\*B\*a\*\*2\*b\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(2\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 2 + 1/n)\*gamma(m/n + 2 + 1/n)/(c\*n\*\*2\*gamma(m/n + 3 + 1/n)) + 3\*B\*a\*b\*\*2\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(3\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 3 + 1/n)\*gamma(m/n + 3 + 1/n)/(c\*n\*\*2\*gamma(m/n + 4 + 1/n)) + 9\*B\*a\*b\*\*2\*e\*\*m\*m\*x\*x\*\*m\*x\*\*(3\*n)\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 3 +

$$\begin{aligned} & 1/n) * \text{gamma}(m/n + 3 + 1/n) / (c * n * \text{gamma}(m/n + 4 + 1/n)) + 3 * B * a * b^{**2} * e^{**m * x * x *} \\ & * m * x^{**3 * n} * \text{lerchphi}(d * x^{**n} * \text{exp\_polar}(I * \text{pi}) / c, 1, m/n + 3 + 1/n) * \text{gamma}(m/n \\ & + 3 + 1/n) / (c * n^{**2} * \text{gamma}(m/n + 4 + 1/n)) + B * b^{**3} * e^{**m * m * x * x * m * x^{**4 * n}} * \text{le} \\ & \text{rchphi}(d * x^{**n} * \text{exp\_polar}(I * \text{pi}) / c, 1, m/n + 4 + 1/n) * \text{gamma}(m/n + 4 + 1/n) / (c * \\ & n^{**2} * \text{gamma}(m/n + 5 + 1/n)) + 4 * B * b^{**3} * e^{**m * x * x * m * x^{**4 * n}} * \text{lerchphi}(d * x^{**n} * \\ & \text{exp\_polar}(I * \text{pi}) / c, 1, m/n + 4 + 1/n) * \text{gamma}(m/n + 4 + 1/n) / (c * n * \text{gamma}(m/n + \\ & 5 + 1/n)) + B * b^{**3} * e^{**m * x * x * m * x^{**4 * n}} * \text{lerchphi}(d * x^{**n} * \text{exp\_polar}(I * \text{pi}) / c, \\ & 1, m/n + 4 + 1/n) * \text{gamma}(m/n + 4 + 1/n) / (c * n^{**2} * \text{gamma}(m/n + 5 + 1/n)) \end{aligned}$$

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^3\*(x\*e)^m/(d\*x^n + c), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(e x)^m (A + B x^n) (a + b x^n)^3}{c + d x^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^3)/(c + d\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^3)/(c + d\*x^n), x)

$$3.23 \quad \int \frac{(ex)^m (a+bx^n)^2 (A+Bx^n)}{c+dx^n} dx$$

**Optimal.** Leaf size=187

$$\frac{b(bBc - Abd - 2aBd)x^{1+n}(ex)^m}{d^2(1+m+n)} + \frac{b^2 Bx^{1+2n}(ex)^m}{d(1+m+2n)} + \frac{(a^2 Bd^2 + b^2 c(Bc - Ad) - 2abd(Bc - Ad))(ex)^{1+m}}{d^3 e(1+m)}$$

[Out]  $-b*(-A*b*d-2*B*a*d+B*b*c)*x^{(1+n)}*(e*x)^m/d^2/(1+m+n)+b^2*B*x^{(1+2*n)}*(e*x)^m/d/(1+m+2*n)+(a^2*B*d^2+b^2*c*(B*c-A*d)-2*a*b*d*(B*c-A*d))*(e*x)^{(1+m)}/d^3/e/(1+m)-(-a*d+b*c)^2*(-A*d+B*c)*(e*x)^{(1+m)}*\text{hypergeom}([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c/d^3/e/(1+m)$

**Rubi** [A]

time = 0.17, antiderivative size = 187, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 4, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.129$ , Rules used = {584, 20, 30, 371}

$$\frac{(ex)^{m+1}(a^2 Bd^2 - 2abd(Bc - Ad) + b^2 c(Bc - Ad))}{d^3 e(m+1)} - \frac{(ex)^{m+1}(bc - ad)^2 (Bc - Ad) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right)}{cd^3 e(m+1)} - \frac{bx^{m+1}(ex)^m(-2aBd - Abd + bBc)}{d^2(m+n+1)} + \frac{b^2 Bx^{2n+1}(ex)^m}{d(m+2n+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n))/(c + d\*x^n), x]

[Out]  $-((b*(b*B*c - A*b*d - 2*a*B*d)*x^{(1+n)}*(e*x)^m)/(d^2*(1+m+n))) + (b^2*B*x^{(1+2*n)}*(e*x)^m)/(d*(1+m+2*n)) + ((a^2*B*d^2 + b^2*c*(B*c - A*d) - 2*a*b*d*(B*c - A*d))*(e*x)^{(1+m)})/(d^3*e*(1+m)) - ((b*c - a*d)^2*(B*c - A*d)*(e*x)^{(1+m)}*\text{Hypergeometric2F1}[1, (1+m)/n, (1+m+n)/n, -(d*x^n/c)])/(c*d^3*e*(1+m))$

Rule 20

Int[(u\_.)\*((a\_.)\*(v\_))^(m\_)\*((b\_.)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && N eQ[m, -1]

Rule 371

Int[((c\_.)\*(x\_))^(m\_)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILt Q[p, 0] || GtQ[a, 0])

Rule 584

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (a + bx^n)^2 (A + Bx^n)}{c + dx^n} dx &= \int \left( \frac{(a^2 B d^2 + b^2 c (Bc - Ad) - 2abd(Bc - Ad)) (ex)^m}{d^3} + \frac{b(-bBc + Abd)}{d} \right) dx \\ &= \frac{(a^2 B d^2 + b^2 c (Bc - Ad) - 2abd(Bc - Ad)) (ex)^{1+m}}{d^3 e (1+m)} + \frac{(b^2 B) \int x^{2n} (ex)^m dx}{d} \\ &= \frac{(a^2 B d^2 + b^2 c (Bc - Ad) - 2abd(Bc - Ad)) (ex)^{1+m}}{d^3 e (1+m)} - \frac{(bc - ad)^2 (Bc - Ad)}{d^2} \\ &= -\frac{b(bBc - Abd - 2aBd)x^{1+n} (ex)^m}{d^2 (1+m+n)} + \frac{b^2 B x^{1+2n} (ex)^m}{d(1+m+2n)} + \frac{(a^2 B d^2 + b^2 c (Bc - Ad)) (ex)^m}{d^3} \end{aligned}$$

**Mathematica [A]**

time = 0.33, size = 156, normalized size = 0.83

$$x(ex)^m \left( \frac{(bc - ad)^2 (Bc - Ad)}{cd^3 (1+m)} + \frac{a^2 A}{c + cm} + \frac{b(-bBc + Abd + 2aBd)x^n}{d^2 (1+m+n)} + \frac{b^2 B x^{2n}}{d + dm + 2dn} + \frac{(bc - ad)^2 (-Bc + Ad) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{cd^3 (1+m)} \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(a + b*x^n)^2*(A + B*x^n))/(c + d*x^n), x]
```

```
[Out] x*(e*x)^m*((b*c - a*d)^2*(B*c - A*d)/(c*d^3*(1 + m)) + (a^2*A)/(c + c*m) + (b*(-b*B*c) + A*b*d + 2*a*B*d)*x^n/(d^2*(1 + m + n)) + (b^2*B*x^(2*n))/(d + d*m + 2*d*n) + ((b*c - a*d)^2*(-(B*c) + A*d)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(d*x^n)/c])/(c*d^3*(1 + m)))
```

**Maple [F]**

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^2 (A + Bx^n)}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(a+b*x^n)^2*(A+B*x^n)/(c+d*x^n), x)
```

```
[Out] int((e*x)^m*(a+b*x^n)^2*(A+B*x^n)/(c+d*x^n), x)
```

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

**[In]** integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="maxima")

**[Out]**  $((b^2*c^2*d*e^m - 2*a*b*c*d^2*e^m + a^2*d^3*e^m)*A - (b^2*c^3*e^m - 2*a*b*c^2*d*e^m + a^2*c*d^2*e^m)*B)*\int(x^m/(d^4*x^n + c*d^3), x) + ((m^2*e^m + m*(n+2)*e^m + (n+1)*e^m)*B*b^2*d^2*x*e^{(m*\log(x) + 2*n*\log(x))} - ((m^2*e^m + m*(3*n+2)*e^m + (2*n^2+3*n+1)*e^m)*b^2*c*d - 2*(m^2*e^m + m*(3*n+2)*e^m + (2*n^2+3*n+1)*e^m)*a*b*d^2)*A - ((m^2*e^m + m*(3*n+2)*e^m + (2*n^2+3*n+1)*e^m)*b^2*c^2 - 2*(m^2*e^m + m*(3*n+2)*e^m + (2*n^2+3*n+1)*e^m)*a*b*c*d + (m^2*e^m + m*(3*n+2)*e^m + (2*n^2+3*n+1)*e^m)*a^2*d^2)*B)*x*x^m + ((m^2*e^m + 2*m*(n+1)*e^m + (2*n+1)*e^m)*A*b^2*d^2 - ((m^2*e^m + 2*m*(n+1)*e^m + (2*n+1)*e^m)*b^2*c*d - 2*(m^2*e^m + 2*m*(n+1)*e^m + (2*n+1)*e^m)*a*b*d^2)*B)*x*e^{(m*\log(x) + n*\log(x))}/((m^3 + 3*m^2*(n+1) + (2*n^2 + 6*n + 3)*m + 2*n^2 + 3*n + 1)*d^3)$

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

**[In]** integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="fricas")

**[Out]** integral((B\*b^2\*x^(3\*n) + A\*a^2 + (2\*B\*a\*b + A\*b^2)\*x^(2\*n) + (B\*a^2 + 2\*A\*a\*b)\*x^n)\*(x\*e)^m/(d\*x^n + c), x)

**Sympy [C]** Result contains complex when optimal does not.

time = 12.16, size = 1085, normalized size = 5.80

Verification of antiderivative is not currently implemented for this CAS.

**[In]** integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*2\*(A+B\*x\*\*n)/(c+d\*x\*\*n),x)

**[Out]**  $A*a**2*e**m*m*x*x**m*\text{lerchphi}(d*x**n*\text{exp\_polar}(I*\text{pi})/c, 1, m/n + 1/n)*\text{gamma}(m/n + 1/n)/(c*n**2*\text{gamma}(m/n + 1 + 1/n)) + A*a**2*e**m*x*x**m*\text{lerchphi}(d*x**n*\text{exp\_polar}(I*\text{pi})/c, 1, m/n + 1/n)*\text{gamma}(m/n + 1/n)/(c*n**2*\text{gamma}(m/n + 1 + 1/n)) + 2*A*a*b*e**m*m*x*x**m*x**n*\text{lerchphi}(d*x**n*\text{exp\_polar}(I*\text{pi})/c, 1, m/n + 1 + 1/n)*\text{gamma}(m/n + 1 + 1/n)/(c*n**2*\text{gamma}(m/n + 2 + 1/n)) + 2*A*a*b*e**m*x*x**m*x**n*\text{lerchphi}(d*x**n*\text{exp\_polar}(I*\text{pi})/c, 1, m/n + 1 + 1/n)*\text{gam}$

```

ma(m/n + 1 + 1/n)/(c*n*gamma(m/n + 2 + 1/n)) + 2*A*a*b*e**m*x*x**m*x**n*ler
chphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*n
**2*gamma(m/n + 2 + 1/n)) + A*b**2*e**m*m*x*x**m*x**(2*n)*lerchphi(d*x**n*e
xp_polar(I*pi)/c, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(c*n**2*gamma(m/n
+ 3 + 1/n)) + 2*A*b**2*e**m*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_polar(I*pi)
/c, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(c*n*gamma(m/n + 3 + 1/n)) + A*b
**2*e**m*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 2 + 1/
n)*gamma(m/n + 2 + 1/n)/(c*n**2*gamma(m/n + 3 + 1/n)) + B*a**2*e**m*m*x*x**
m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 +
1/n)/(c*n**2*gamma(m/n + 2 + 1/n)) + B*a**2*e**m*x*x**m*x**n*lerchphi(d*x*
*n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*n*gamma(m/n
+ 2 + 1/n)) + B*a**2*e**m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1
, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*n**2*gamma(m/n + 2 + 1/n)) + 2*B*a
*b*e**m*m*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 2 + 1
/n)*gamma(m/n + 2 + 1/n)/(c*n**2*gamma(m/n + 3 + 1/n)) + 4*B*a*b*e**m*x*x**
m*x**(2*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 2 + 1/n)*gamma(m/n +
2 + 1/n)/(c*n*gamma(m/n + 3 + 1/n)) + 2*B*a*b*e**m*x*x**m*x**(2*n)*lerchph
i(d*x**n*exp_polar(I*pi)/c, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(c*n**2*
gamma(m/n + 3 + 1/n)) + B*b**2*e**m*m*x*x**m*x**(3*n)*lerchphi(d*x**n*exp_p
olar(I*pi)/c, 1, m/n + 3 + 1/n)*gamma(m/n + 3 + 1/n)/(c*n**2*gamma(m/n + 4
+ 1/n)) + 3*B*b**2*e**m*x*x**m*x**(3*n)*lerchphi(d*x**n*exp_polar(I*pi)/c,
1, m/n + 3 + 1/n)*gamma(m/n + 3 + 1/n)/(c*n*gamma(m/n + 4 + 1/n)) + B*b**2*
e**m*x*x**m*x**(3*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 3 + 1/n)*g
amma(m/n + 3 + 1/n)/(c*n**2*gamma(m/n + 4 + 1/n))

```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^2\*(x\*e)^m/(d\*x^n + c), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^2}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^2)/(c + d\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^2)/(c + d\*x^n), x)



$$3.24 \quad \int \frac{(ex)^m (a+bx^n)(A+Bx^n)}{c+dx^n} dx$$

**Optimal.** Leaf size=122

$$\frac{bBx^{1+n}(ex)^m}{d(1+m+n)} - \frac{(bBc - Abd - aBd)(ex)^{1+m}}{d^2e(1+m)} + \frac{(bc - ad)(Bc - Ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{cd^2e(1+m)}$$

[Out] b\*B\*x^(1+n)\*(e\*x)^m/d/(1+m+n)-(-A\*b\*d-B\*a\*d+B\*b\*c)\*(e\*x)^(1+m)/d^2/e/(1+m)+(-a\*d+b\*c)\*(-A\*d+B\*c)\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d\*x^n/c)/c/d^2/e/(1+m)

**Rubi [A]**

time = 0.09, antiderivative size = 122, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 4, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.138$ , Rules used = {584, 20, 30, 371}

$$\frac{(ex)^{m+1}(bc - ad)(Bc - Ad) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right)}{cd^2e(m+1)} - \frac{(ex)^{m+1}(-aBd - Abd + bBc)}{d^2e(m+1)} + \frac{bBx^{n+1}(ex)^m}{d(m+n+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n))/(c + d\*x^n), x]

[Out] (b\*B\*x^(1 + n)\*(e\*x)^m)/(d\*(1 + m + n)) - ((b\*B\*c - A\*b\*d - a\*B\*d)\*(e\*x)^(1 + m))/(d^2\*e\*(1 + m)) + ((b\*c - a\*d)\*(B\*c - A\*d)\*(e\*x)^(1 + m)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)]/(c\*d^2\*e\*(1 + m))

Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 371

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 584

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (a + bx^n) (A + Bx^n)}{c + dx^n} dx &= \int \left( \frac{(-bBc + Abd + aBd)(ex)^m}{d^2} + \frac{bBx^n(ex)^m}{d} + \frac{(-bc + ad)(-Bc + Ad)}{d^2(c + dx^n)} \right) dx \\ &= -\frac{(bBc - Abd - aBd)(ex)^{1+m}}{d^2e(1+m)} + \frac{(bB) \int x^n(ex)^m dx}{d} + \frac{((bc - ad)(Bc - Ad))}{d^2} \\ &= -\frac{(bBc - Abd - aBd)(ex)^{1+m}}{d^2e(1+m)} + \frac{(bc - ad)(Bc - Ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}\right)}{cd^2e(1+m)} \\ &= \frac{bBx^{1+n}(ex)^m}{d(1+m+n)} - \frac{(bBc - Abd - aBd)(ex)^{1+m}}{d^2e(1+m)} + \frac{(bc - ad)(Bc - Ad)(ex)^{1+m}}{cd^2} \end{aligned}$$

**Mathematica [A]**

time = 0.18, size = 115, normalized size = 0.94

$$\frac{x(ex)^m (aAd^2(1+m+n) - (bc-ad)(Bc-Ad)(1+m+n) + bBcd(1+m)x^n + (bc-ad)(Bc-Ad)(1+m+n) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right))}{cd^2(1+m)(1+m+n)}$$

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(a + b*x^n)*(A + B*x^n))/(c + d*x^n), x]
```

```
[Out] (x*(e*x)^m*(a*A*d^2*(1 + m + n) - (b*c - a*d)*(B*c - A*d)*(1 + m + n) + b*B*c*d*(1 + m)*x^n + (b*c - a*d)*(B*c - A*d)*(1 + m + n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)])/(c*d^2*(1 + m)*(1 + m + n))
```

**Maple [F]**

time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n) (A + Bx^n)}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(a+b*x^n)*(A+B*x^n)/(c+d*x^n), x)
```

```
[Out] int((e*x)^m*(a+b*x^n)*(A+B*x^n)/(c+d*x^n), x)
```

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)*(A+B*x^n)/(c+d*x^n),x, algorithm="maxima")
```

```
[Out] -((b*c*d*e^m - a*d^2*e^m)*A - (b*c^2*e^m - a*c*d*e^m)*B)*integrate(x^m/(d^3
*x^n + c*d^2), x) + ((m*e^m + e^m)*B*b*d*x*e^(m*log(x) + n*log(x)) + ((m*e^
m + (n + 1)*e^m)*A*b*d - ((m*e^m + (n + 1)*e^m)*b*c - (m*e^m + (n + 1)*e^m)
*a*d)*B)*x*x^m)/((m^2 + m*(n + 2) + n + 1)*d^2)
```

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)*(A+B*x^n)/(c+d*x^n),x, algorithm="fricas")
```

```
[Out] integral((B*b*x^(2*n) + A*a + (B*a + A*b)*x^n)*(x*e)^m/(d*x^n + c), x)
```

**Sympy** [C] Result contains complex when optimal does not.

time = 6.25, size = 666, normalized size = 5.46

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)*(A+B*x**n)/(c+d*x**n),x)
```

```
[Out] A*a*e**m*m*x*x**m*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/
n + 1/n)/(c*n**2*gamma(m/n + 1 + 1/n)) + A*a*e**m*x*x**m*lerchphi(d*x**n*ex
p_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c*n**2*gamma(m/n + 1 + 1/n
)) + A*b*e**m*m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 +
1/n)*gamma(m/n + 1 + 1/n)/(c*n**2*gamma(m/n + 2 + 1/n)) + A*b*e**m*x*x**m*
x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1
/n)/(c*n*gamma(m/n + 2 + 1/n)) + A*b*e**m*x*x**m*x**n*lerchphi(d*x**n*exp_p
olar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*n**2*gamma(m/n + 2
+ 1/n)) + B*a*e**m*m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n
+ 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*n**2*gamma(m/n + 2 + 1/n)) + B*a*e**m*x*
x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n +
1 + 1/n)/(c*n*gamma(m/n + 2 + 1/n)) + B*a*e**m*x*x**m*x**n*lerchphi(d*x**n*
exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*n**2*gamma(m/n
+ 2 + 1/n)) + B*b*e**m*m*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_polar(I*pi)/c
, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n)/(c*n**2*gamma(m/n + 3 + 1/n)) + 2*
B*b*e**m*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 2 + 1/
n)*gamma(m/n + 2 + 1/n)/(c*n*gamma(m/n + 3 + 1/n)) + B*b*e**m*x*x**m*x**(2*
n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 2 + 1/n)*gamma(m/n + 2 + 1/n
)/(c*n**2*gamma(m/n + 3 + 1/n))
```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)\*(x\*e)^m/(d\*x^n + c), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(e x)^m (A + B x^n) (a + b x^n)}{c + d x^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n))/(c + d\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n))/(c + d\*x^n), x)

$$3.25 \quad \int \frac{(ex)^m (A+Bx^n)}{c+dx^n} dx$$

**Optimal.** Leaf size=78

$$\frac{B(ex)^{1+m}}{de(1+m)} - \frac{(Bc - Ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{cde(1+m)}$$

[Out] B\*(e\*x)^(1+m)/d/e/(1+m)-(-A\*d+B\*c)\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d\*x^n/c)/c/d/e/(1+m)

**Rubi** [A]

time = 0.03, antiderivative size = 78, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$ ,

Rules used = {470, 371}

$$\frac{B(ex)^{m+1}}{de(m+1)} - \frac{(ex)^{m+1}(Bc - Ad) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right)}{cde(m+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n))/(c + d\*x^n), x]

[Out] (B\*(e\*x)^(1 + m))/(d\*e\*(1 + m)) - ((B\*c - A\*d)\*(e\*x)^(1 + m)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)]/(c\*d\*e\*(1 + m))

Rule 371

Int[((c\_.)\*(x\_)^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_.))^(p\_), x\_Symbol] :> Simp[a^p\*((c\*x)^(m + 1)/(c\*(m + 1)))\*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 470

Int[((e\_.)\*(x\_)^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_.))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_.)), x\_Symbol] :> Simp[d\*(e\*x)^(m + 1)\*((a + b\*x^n)^(p + 1)/(b\*e\*(m + n\*(p + 1) + 1))), x] - Dist[(a\*d\*(m + 1) - b\*c\*(m + n\*(p + 1) + 1))/(b\*(m + n\*(p + 1) + 1)), Int[(e\*x)^m\*(a + b\*x^n)^p, x], x] /; FreeQ[{a, b, c, d, e, m, n, p}, x] && NeQ[b\*c - a\*d, 0] && NeQ[m + n\*(p + 1) + 1, 0]

Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A+Bx^n)}{c+dx^n} dx &= \frac{B(ex)^{1+m}}{de(1+m)} - \frac{(Bc(1+m) - Ad(1+m)) \int \frac{(ex)^m}{c+dx^n} dx}{d(1+m)} \\ &= \frac{B(ex)^{1+m}}{de(1+m)} - \frac{(Bc - Ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{cde(1+m)} \end{aligned}$$

**Mathematica [A]**

time = 0.09, size = 59, normalized size = 0.76

$$\frac{x(ex)^m (-Bc + (Bc - Ad) {}_2F_1(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}))}{cd(1+m)}$$

Antiderivative was successfully verified.

`[In] Integrate[((e*x)^m*(A + B*x^n))/(c + d*x^n), x]``[Out] -((x*(e*x)^m*(-(B*c) + (B*c - A*d)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(d*x^n)/c]))/(c*d*(1 + m))`**Maple [F]**

time = 0.09, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

`[In] int((e*x)^m*(A+B*x^n)/(c+d*x^n), x)``[Out] int((e*x)^m*(A+B*x^n)/(c+d*x^n), x)`**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

`[In] integrate((e*x)^m*(A+B*x^n)/(c+d*x^n), x, algorithm="maxima")``[Out] -(B*c*e^m - A*d*e^m)*integrate(x^m/(d^2*x^n + c*d), x) + B*x*e^(m*log(x) + m)/(d*(m + 1))`**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

`[In] integrate((e*x)^m*(A+B*x^n)/(c+d*x^n), x, algorithm="fricas")``[Out] integral((B*x^n + A)*(x*e)^m/(d*x^n + c), x)`**Sympy [C] Result contains complex when optimal does not.**

time = 2.00, size = 284, normalized size = 3.64

$$\frac{Ae^m m x x^m \Phi\left(\frac{dx^n}{c}, 1, \frac{m}{n} + \frac{1}{n}\right) \Gamma\left(\frac{m}{n} + \frac{1}{n}\right)}{cn^2 \Gamma\left(\frac{m}{n} + 1 + \frac{1}{n}\right)} + \frac{Ae^m x x^m \Phi\left(\frac{dx^n}{c}, 1, \frac{m}{n} + \frac{1}{n}\right) \Gamma\left(\frac{m}{n} + \frac{1}{n}\right)}{cn^2 \Gamma\left(\frac{m}{n} + 1 + \frac{1}{n}\right)} + \frac{Be^m m x x^m \Phi\left(\frac{dx^n}{c}, 1, \frac{m}{n} + 1 + \frac{1}{n}\right) \Gamma\left(\frac{m}{n} + 1 + \frac{1}{n}\right)}{cn^2 \Gamma\left(\frac{m}{n} + 2 + \frac{1}{n}\right)} + \frac{Be^m x x^m \Phi\left(\frac{dx^n}{c}, 1, \frac{m}{n} + 1 + \frac{1}{n}\right) \Gamma\left(\frac{m}{n} + 1 + \frac{1}{n}\right)}{cn \Gamma\left(\frac{m}{n} + 2 + \frac{1}{n}\right)} + \frac{Be^m x x^m \Phi\left(\frac{dx^n}{c}, 1, \frac{m}{n} + 1 + \frac{1}{n}\right) \Gamma\left(\frac{m}{n} + 1 + \frac{1}{n}\right)}{cn^2 \Gamma\left(\frac{m}{n} + 2 + \frac{1}{n}\right)}$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)/(c+d\*x\*\*n),x)

[Out] A\*e\*\*m\*m\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*n\*\*2\*gamma(m/n + 1 + 1/n)) + A\*e\*\*m\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*n\*\*2\*gamma(m/n + 1 + 1/n)) + B\*e\*\*m\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*\*2\*gamma(m/n + 2 + 1/n)) + B\*e\*\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*\*2\*gamma(m/n + 2 + 1/n)) + B\*e\*\*m\*x\*x\*\*m\*x\*\*n\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1 + 1/n)\*gamma(m/n + 1 + 1/n)/(c\*n\*\*2\*gamma(m/n + 2 + 1/n))

Giac [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(x\*e)^m/(d\*x^n + c), x)

Mupad [F]

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(ex)^m (A + Bx^n)}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/(c + d\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/(c + d\*x^n), x)

### 3.26 $\int \frac{(ex)^m(A+Bx^n)}{(a+bx^n)(c+dx^n)} dx$

**Optimal.** Leaf size=127

$$\frac{(Ab - aB)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{a(bc - ad)e(1+m)} + \frac{(Bc - Ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{c(bc - ad)e(1+m)}$$

[Out] (A\*b-B\*a)\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b\*x^n/a)/a/(-a\*d+b\*c)/e/(1+m)+(-A\*d+B\*c)\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d\*x^n/c)/c/(-a\*d+b\*c)/e/(1+m)

**Rubi [A]**

time = 0.09, antiderivative size = 127, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 2, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.065$ , Rules used = {611, 371}

$$\frac{(ex)^{m+1}(Ab - aB) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{bx^n}{a}\right)}{ae(m+1)(bc - ad)} + \frac{(ex)^{m+1}(Bc - Ad) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right)}{ce(m+1)(bc - ad)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)\*(c + d\*x^n)), x]

[Out] ((A\*b - a\*B)\*(e\*x)^(1+m)\*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(b\*x^n/a)]/(a\*(b\*c - a\*d)\*e\*(1+m)) + ((B\*c - A\*d)\*(e\*x)^(1+m)\*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d\*x^n)/c)]/(c\*(b\*c - a\*d)\*e\*(1+m))

Rule 371

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 611

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((e\_) + (f\_.)\*(x\_)^(n\_)))/((c\_) + (d\_.)\*(x\_)^(n\_)), x\_Symbol] :> Int[ExpandIntegrand[(g\*x)^m\*(a + b\*x^n)^p\*((e + f\*x^n)/(c + d\*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x]

Rubi steps



$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)(c + dx^n)} dx &= \int \left( \frac{(Ab - aB)(ex)^m}{(bc - ad)(a + bx^n)} + \frac{(Bc - Ad)(ex)^m}{(bc - ad)(c + dx^n)} \right) dx \\ &= \frac{(Ab - aB) \int \frac{(ex)^m}{a + bx^n} dx}{bc - ad} + \frac{(Bc - Ad) \int \frac{(ex)^m}{c + dx^n} dx}{bc - ad} \\ &= \frac{(Ab - aB)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{a(bc - ad)e(1+m)} + \frac{(Bc - Ad)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{c(bc - ad)e(1+m)} \end{aligned}$$

**Mathematica [A]**

time = 0.19, size = 102, normalized size = 0.80

$$\frac{x(ex)^m \left( (-Abc + aBc) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right) + a(-Bc + Ad) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right) \right)}{ac(-bc + ad)(1+m)}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)\*(c + d\*x^n)),x]

[Out] (x\*(e\*x)^m\*((-(A\*b\*c) + a\*B\*c)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)] + a\*(-(B\*c) + A\*d)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)])/(a\*c\*(-(b\*c) + a\*d)\*(1 + m))

**Maple [F]**

time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)(c + dx^n)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n),x)

[Out] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n),x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n),x, algorithm="maxima")

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)\*(d\*x^n + c)), x)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n),x, algorithm="fricas")

[Out] integral((B\*x^n + A)\*(x\*e)^m/(b\*d\*x^(2\*n) + a\*c + (b\*c + a\*d)\*x^n), x)

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)/(a+b\*x\*\*n)/(c+d\*x\*\*n),x)

[Out] Exception raised: HeuristicGCDFailed >> no luck

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)\*(d\*x^n + c)), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(e x)^m (A + B x^n)}{(a + b x^n) (c + d x^n)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)\*(c + d\*x^n)),x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)\*(c + d\*x^n)), x)

$$3.27 \quad \int \frac{(ex)^m (A+Bx^n)}{(a+bx^n)^2 (c+dx^n)} dx$$

**Optimal.** Leaf size=212

$$\frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en(a + bx^n)} + \frac{(Ab(ad(1 + m - 2n) - bc(1 + m - n)) + aB(bc(1 + m) - ad(1 + m - n)))(ex)^{1+m}}{a^2(bc - ad)^2 e(1 + m)n}$$

[Out] (A\*b-B\*a)\*(e\*x)^(1+m)/a/(-a\*d+b\*c)/e/n/(a+b\*x^n)+(A\*b\*(a\*d\*(1+m-2\*n)-b\*c\*(1+m-n))+a\*B\*(b\*c\*(1+m)-a\*d\*(1+m-n))\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b\*x^n/a)/a^2/(-a\*d+b\*c)^2/e/(1+m)/n-d\*(-A\*d+B\*c)\*(e\*x)^(1+m)\*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d\*x^n/c)/c/(-a\*d+b\*c)^2/e/(1+m)

**Rubi** [A]

time = 0.35, antiderivative size = 212, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {609, 611, 371}

$$\frac{(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{bx^n}{a}\right) (Ab(ad(m-2n+1) - bc(m-n+1)) + aB(bc(m+1) - ad(m-n+1)))}{a^2 e(m+1)n(bc-ad)^2} - \frac{d(ex)^{m+1} (Bc - Ad) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right)}{ce(m+1)(bc-ad)^2} + \frac{(ex)^{m+1} (Ab - aB)}{aen(bc-ad)(a+bx^n)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)),x]

[Out] ((A\*b - a\*B)\*(e\*x)^(1 + m))/(a\*(b\*c - a\*d)\*e\*n\*(a + b\*x^n)) + ((A\*b\*(a\*d\*(1 + m - 2\*n) - b\*c\*(1 + m - n)) + a\*B\*(b\*c\*(1 + m) - a\*d\*(1 + m - n)))\*(e\*x)^(1 + m)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)]/(a^2\*(b\*c - a\*d)^2\*e\*(1 + m)\*n) - (d\*(B\*c - A\*d)\*(e\*x)^(1 + m)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)]/(c\*(b\*c - a\*d)^2\*e\*(1 + m))

Rule 371

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m + 1)/(c\*(m + 1)))\*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 609

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_.)\*(x\_)^(n\_)), x\_Symbol] := Simp[(-b\*e - a\*f)\*(g\*x)^(m + 1)\*(a + b\*x^n)^(p + 1)\*((c + d\*x^n)^(q + 1)/(a\*g\*n\*(b\*c - a\*d)\*(p + 1))), x] + Dist[1/(a\*n\*(b\*c - a\*d)\*(p + 1)), Int[(g\*x)^m\*(a + b\*x^n)^(p + 1)\*(c + d\*x^n)^q\*Simp[c\*(b\*e - a\*f)\*(m + 1) + e\*n\*(b\*c - a\*d)\*(p + 1) + d\*(b\*e - a\*f)\*(m + n\*(p + q + 2) + 1)\*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, q}, x] && LtQ[p, -1]

## Rule 611

```
Int[(((g_)*(x_)^(m_))*((a_) + (b_)*(x_)^(n_))^(p_))*((e_) + (f_)*(x_)^(n_)))/((c_) + (d_)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x]
```

## Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)} dx &= \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n)} - \frac{\int \frac{(ex)^m (-aBc(1+m) + Abc(1+m-n) + aAdn + (Ab - aB)d(1+m-n)x^n)}{(a+bx^n)(c+dx^n)} dx}{a(bc - ad)n} \\ &= \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n)} - \frac{\int \left( \frac{(-Ab(ad(1+m-2n) - bc(1+m-n)) - aB(bc(1+m) - ad(1+m-n))}{(bc-ad)(a+bx^n)} \right) dx}{a(bc - ad)n} \\ &= \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n)} - \frac{(d(Bc - Ad)) \int \frac{(ex)^m}{c+dx^n} dx}{(bc - ad)^2} + \frac{(Ab(ad(1+m-2n) - bc(1+m-n)) - aB(bc(1+m) - ad(1+m-n)))}{a(bc - ad)n} \\ &= \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n)} + \frac{(Ab(ad(1+m-2n) - bc(1+m-n)) + aB(bc(1+m) - ad(1+m-n)))}{a^2(bc - ad)^2} \end{aligned}$$

**Mathematica** [A]

time = 0.36, size = 177, normalized size = 0.83

$$\frac{x(ex)^m \left( \frac{(-Ab+aB)(-bc+ad)}{an(a+bx^n)} - \frac{(Ab(-ad(1+m-2n)+bc(1+m-n))+aB(-bc(1+m)+ad(1+m-n))}{a^2(1+m)n} {}_2F_1\left(1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{bx^n}{a}\right) + \frac{d(-Bc+Ad)}{c(1+m)} {}_2F_1\left(1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{dx^n}{c}\right) \right)}{(bc - ad)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(A + B*x^n))/((a + b*x^n)^2*(c + d*x^n)), x]
```

```
[Out] (x*(e*x)^m*(((-(A*b) + a*B)*(-(b*c) + a*d))/(a*n*(a + b*x^n)) - ((A*b*(-(a*d*(1 + m - 2*n)) + b*c*(1 + m - n)) + a*B*(-(b*c*(1 + m)) + a*d*(1 + m - n)))*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(b*x^n)/a]))/(a^2*(1 + m)*n) + (d*(-(B*c) + A*d)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(d*x^n)/c]))/(c*(1 + m)))/(b*c - a*d)^2
```

**Maple** [F]

time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(A+B*x^n)/(a+b*x^n)^2/(c+d*x^n), x)
```

[Out]  $\int (e^x)^m (A+Bx^n) / (a+bx^n)^2 / (c+dx^n), x$

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(A+B*x^n)/(a+b*x^n)^2/(c+d*x^n),x, algorithm="maxima")`

[Out]  $-(B*a*e^m - A*b*e^m)*x*x^m/(a^2*b*c^n - a^3*d^n + (a*b^2*c^n - a^2*b*d^n)*x^n) - (((m*e^m - (n-1)*e^m)*b^2*c - (m*e^m - (2*n-1)*e^m)*a*b*d)*A - ((m*e^m + e^m)*a*b*c - (m*e^m - (n-1)*e^m)*a^2*d)*B)*\int(x^m/(a^2*b^2*c^2*n - 2*a^3*b*c*d*n + a^4*d^2*n + (a*b^3*c^2*n - 2*a^2*b^2*c*d*n + a^3*b*d^2*n)*x^n), x) - (B*c*d*e^m - A*d^2*e^m)*\int(x^m/(b^2*c^3 - 2*a*b*c^2*d + a^2*c*d^2 + (b^2*c^2*d - 2*a*b*c*d^2 + a^2*d^3)*x^n), x)$

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(A+B*x^n)/(a+b*x^n)^2/(c+d*x^n),x, algorithm="fricas")`

[Out]  $\int (B*x^n + A)*(x*e)^m / (b^2*d*x^{3*n} + a^2*c + (b^2*c + 2*a*b*d)*x^{2*n} + (2*a*b*c + a^2*d)*x^n), x$

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)**m*(A+B*x**n)/(a+b*x**n)**2/(c+d*x**n),x)`

[Out] Exception raised: HeuristicGCDFailed >> no luck

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] `integrate((e*x)^m*(A+B*x^n)/(a+b*x^n)^2/(c+d*x^n),x, algorithm="giac")`

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)^2\*(d\*x^n + c)), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)), x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)), x)

$$3.28 \quad \int \frac{(ex)^m(A+Bx^n)}{(a+bx^n)^3(c+dx^n)} dx$$

**Optimal.** Leaf size=407

$$\frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en(a + bx^n)^2} + \frac{(Ab(ad(1 + m - 4n) - bc(1 + m - 2n)) + aB(bc(1 + m) - ad(1 + m - 2n)))(e)}{2a^2(bc - ad)^2en^2(a + bx^n)}$$

[Out]  $1/2*(A*b-B*a)*(e*x)^{(1+m)}/a/(-a*d+b*c)/e/n/(a+b*x^n)^2+1/2*(A*b*(a*d*(1+m-4*n)-b*c*(1+m-2*n))+a*B*(b*c*(1+m)-a*d*(1+m-2*n))*(e*x)^{(1+m)}/a^2/(-a*d+b*c)^2/e/n^2/(a+b*x^n)+1/2*(a*B*(2*a*b*c*d*(1+m)*(1+m-2*n)-b^2*c^2*(1+m)*(1+m-n)-a^2*d^2*(1+m^2+m*(2-3*n)-3*n+2*n^2))+A*b*(b^2*c^2*(1+m^2+m*(2-3*n)-3*n+2*n^2)-2*a*b*c*d*(1+m^2+m*(2-4*n)-4*n+3*n^2)+a^2*d^2*(1+m^2+m*(2-5*n)-5*n+6*n^2))*(e*x)^{(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/a^3/(-a*d+b*c)^3/e/(1+m)/n^2+d^2*(-A*d+B*c)*(e*x)^{(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c/(-a*d+b*c)^3/e/(1+m)}$

**Rubi [A]**

time = 0.81, antiderivative size = 407, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {609, 611, 371}

$(ex)^m(A(ad(m-4n+1)-bc(m-2n+1))+aB(bc(m+1)-ad(m-2n+1)))/2a(bc-ad)^2en(a+bx^n)^2 + (ex)^m(A(b(ad(m+1+m-4n)-bc(m-2n)))+aB(bc(m+1)-ad(m-2n)))/a^2(bc-ad)^2en^2(a+bx^n)^2 + (ex)^m(aB(2abc*d(m+1+m-2n)-b^2c^2(m+1+m-n)-a^2d^2(m^2+m(2-3n)-3n+2n^2))+A*b(b^2c^2(m^2+m(2-3n)-3n+2n^2)-2abc*d(m^2+m(2-4n)-4n+3n^2)+a^2d^2(m^2+m(2-5n)-5n+6n^2)))/a^3(bc-ad)^3en^2(a+bx^n)^3 + (ex)^m(d^2(-A*d+B*c)*(e*x)^{(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)}/c/(-a*d+b*c)^3en^2(a+bx^n)^3$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^3\*(c + d\*x^n)),x]

[Out]  $((A*b - a*B)*(e*x)^{(1 + m)}/(2*a*(b*c - a*d)*e*n*(a + b*x^n)^2) + ((A*b*(a*d*(1 + m - 4*n) - b*c*(1 + m - 2*n)) + a*B*(b*c*(1 + m) - a*d*(1 + m - 2*n)))*(e*x)^{(1 + m)}/(2*a^2*(b*c - a*d)^2*e*n^2*(a + b*x^n)) + ((a*B*(2*a*b*c*d*(1 + m)*(1 + m - 2*n) - b^2*c^2*(1 + m)*(1 + m - n) - a^2*d^2*(1 + m^2 + m*(2 - 3*n) - 3*n + 2*n^2)) + A*b*(b^2*c^2*(1 + m^2 + m*(2 - 3*n) - 3*n + 2*n^2) - 2*a*b*c*d*(1 + m^2 + m*(2 - 4*n) - 4*n + 3*n^2) + a^2*d^2*(1 + m^2 + m*(2 - 5*n) - 5*n + 6*n^2)))*(e*x)^{(1 + m)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)]}/(2*a^3*(b*c - a*d)^3*e*(1 + m)*n^2) + (d^2*(B*c - A*d)*(e*x)^{(1 + m)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(d*x^n/c)]}/(c*(b*c - a*d)^3*e*(1 + m))$

**Rule 371**

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

**Rule 609**

```
Int[((g_)*(x_))^(m_)*((a_) + (b_)*(x_)^(n_))^(p_)*((c_) + (d_)*(x_)^(n_))^(q_)*((e_) + (f_)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^(q + 1)/(a*g*n*(b*c - a*d)*(p + 1))], x] + Dist[1/(a*n*(b*c - a*d)*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^q*Simp[c*(b*e - a*f)*(m + 1) + e*n*(b*c - a*d)*(p + 1) + d*(b*e - a*f)*(m + n*(p + q + 2) + 1)*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, q}, x] && LtQ[p, -1]
```

### Rule 611

```
Int[(((g_)*(x_))^(m_)*((a_) + (b_)*(x_)^(n_))^(p_)*((e_) + (f_)*(x_)^(n_)))/((c_) + (d_)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x]
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^3 (c + dx^n)} dx &= \frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en (a + bx^n)^2} - \frac{\int \frac{(ex)^m (-aBc(1+m) + Abc(1+m-2n) + 2aAdn + (Ab - aB)d(1+m-n))}{(a+bx^n)^2(c+dx^n)} dx}{2a(bc - ad)n} \\ &= \frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en (a + bx^n)^2} + \frac{(Ab(ad(1 + m - 4n) - bc(1 + m - 2n)) + aB(bc(1 + m - 2n) - ad(1 + m - 2n)))}{2a^2(bc - ad)^2 en^2 (a + bx^n)} \\ &= \frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en (a + bx^n)^2} + \frac{(Ab(ad(1 + m - 4n) - bc(1 + m - 2n)) + aB(bc(1 + m - 2n) - ad(1 + m - 2n)))}{2a^2(bc - ad)^2 en^2 (a + bx^n)} \\ &= \frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en (a + bx^n)^2} + \frac{(Ab(ad(1 + m - 4n) - bc(1 + m - 2n)) + aB(bc(1 + m - 2n) - ad(1 + m - 2n)))}{2a^2(bc - ad)^2 en^2 (a + bx^n)} \\ &= \frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en (a + bx^n)^2} + \frac{(Ab(ad(1 + m - 4n) - bc(1 + m - 2n)) + aB(bc(1 + m - 2n) - ad(1 + m - 2n)))}{2a^2(bc - ad)^2 en^2 (a + bx^n)} \end{aligned}$$

### Mathematica [A]

time = 1.21, size = 402, normalized size = 0.99

```
Integrate[((e*x)^m*(A + B*x^n))/((a + b*x^n)^3*(c + d*x^n)), x]
```

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(A + B*x^n))/((a + b*x^n)^3*(c + d*x^n)), x]
```

```
[Out] (x*(e*x)^m*(a*c*(b*c - a*d)*(1 + m)*(a^3*B*d*(1 + m - 3*n) + A*b^3*c*(1 + m - 2*n)*x^n + a*b^2*(A*c*(1 + m - 3*n) - B*c*(1 + m)*x^n - A*d*(1 + m - 4*n)*x^n) - a^2*b*(A*d*(1 + m - 5*n) + B*c*(1 + m - n) - B*d*(1 + m - 2*n)*x^n)
```



)) - c\*(-(a\*B\*(-2\*a\*b\*c\*d\*(1 + m)\*(1 + m - 2\*n) + b^2\*c^2\*(1 + m)\*(1 + m - n) + a^2\*d^2\*(1 + m^2 + m\*(2 - 3\*n) - 3\*n + 2\*n^2))) + A\*b\*(b^2\*c^2\*(1 + m^2 + m\*(2 - 3\*n) - 3\*n + 2\*n^2) - 2\*a\*b\*c\*d\*(1 + m^2 + m\*(2 - 4\*n) - 4\*n + 3\*n^2) + a^2\*d^2\*(1 + m^2 + m\*(2 - 5\*n) - 5\*n + 6\*n^2)))\*(a + b\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)] + 2\*a^3\*d^2\*(-(B\*c + A\*d)\*n^2\*(a + b\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)])))/(2\*a^3\*c\*(-(b\*c) + a\*d)^3\*(1 + m)\*n^2\*(a + b\*x^n)^2)

**Maple [F]**

time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^3 (c + dx^n)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n), x)

[Out] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n), x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n), x, algorithm="maxima")

[Out] -(((m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*b^3\*c^2 - 2\*(m^2\*e^m - 2\*m\*(2\*n - 1)\*e^m + (3\*n^2 - 4\*n + 1)\*e^m)\*a\*b^2\*c\*d + (m^2\*e^m - m\*(5\*n - 2)\*e^m + (6\*n^2 - 5\*n + 1)\*e^m)\*a^2\*b\*d^2)\*A - ((m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a\*b^2\*c^2 - 2\*(m^2\*e^m - 2\*m\*(n - 1)\*e^m - (2\*n - 1)\*e^m)\*a^2\*b\*c\*d + (m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*a^3\*d^2)\*B)\*integrate(-1/2\*x^m/(a^3\*b^3\*c^3\*n^2 - 3\*a^4\*b^2\*c^2\*d\*n^2 + 3\*a^5\*b\*c\*d^2\*n^2 - a^6\*d^3\*n^2 + (a^2\*b^4\*c^3\*n^2 - 3\*a^3\*b^3\*c^2\*d\*n^2 + 3\*a^4\*b^2\*c\*d^2\*n^2 - a^5\*b\*d^3\*n^2)\*x^n), x) - (B\*c\*d^2\*e^m - A\*d^3\*e^m)\*integrate(-x^m/(b^3\*c^4 - 3\*a\*b^2\*c^3\*d + 3\*a^2\*b\*c^2\*d^2 - a^3\*c\*d^3 + (b^3\*c^3\*d - 3\*a\*b^2\*c^2\*d^2 + 3\*a^2\*b\*c\*d^3 - a^3\*d^4)\*x^n), x) - 1/2\*(((m\*e^m - (3\*n - 1)\*e^m)\*a\*b^2\*c - (m\*e^m - (5\*n - 1)\*e^m)\*a^2\*b\*d)\*A - ((m\*e^m - (n - 1)\*e^m)\*a^2\*b\*c - (m\*e^m - (3\*n - 1)\*e^m)\*a^3\*d)\*B)\*x\*x^m + (((m\*e^m - (2\*n - 1)\*e^m)\*b^3\*c - (m\*e^m - (4\*n - 1)\*e^m)\*a\*b^2\*d)\*A - ((m\*e^m + e^m)\*a\*b^2\*c - (m\*e^m - (2\*n - 1)\*e^m)\*a^2\*b\*d)\*B)\*x\*e^(m\*log(x) + n\*log(x)))/(a^4\*b^2\*c^2\*n^2 - 2\*a^5\*b\*c\*d\*n^2 + a^6\*d^2\*n^2 + (a^2\*b^4\*c^2\*n^2 - 2\*a^3\*b^3\*c\*d\*n^2 + a^4\*b^2\*d^2\*n^2)\*x^(2\*n) + 2\*(a^3\*b^3\*c^2\*n^2 - 2\*a^4\*b^2\*c\*d\*n^2 + a^5\*b\*d^2\*n^2)\*x^n)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n),x, algorithm="fricas")

[Out] integral((B\*x^n + A)\*(x\*e)^m/(b^3\*d\*x^(4\*n) + a^3\*c + (b^3\*c + 3\*a\*b^2\*d)\*x^(3\*n) + 3\*(a\*b^2\*c + a^2\*b\*d)\*x^(2\*n) + (3\*a^2\*b\*c + a^3\*d)\*x^n), x)

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)/(a+b\*x\*\*n)\*\*3/(c+d\*x\*\*n),x)

[Out] Exception raised: HeuristicGCDFailed >> no luck

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)^3\*(d\*x^n + c)), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^3 (c + dx^n)} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^3\*(c + d\*x^n)),x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^3\*(c + d\*x^n)), x)

$$3.29 \quad \int \frac{(ex)^m (a+bx^n)^3 (A+Bx^n)}{(c+dx^n)^2} dx$$

**Optimal.** Leaf size=386

$$\frac{b^2(3ad(Ad(1+m+n) - Bc(1+m+2n)) - bc(Ad(1+m+2n) - Bc(1+m+3n)))x^{1+n}(ex)^m}{cd^3n(1+m+n)} - \frac{b^3(Ad(1+m+n) - Bc(1+m+2n))}{cd^3n(1+m+n)}$$

```
[Out] -b^2*(3*a*d*(A*d*(1+m+n)-B*c*(1+m+2*n))-b*c*(A*d*(1+m+2*n)-B*c*(1+m+3*n)))*
x^(1+n)*(e*x)^m/c/d^3/n/(1+m+n)-b^3*(A*d*(1+m+2*n)-B*c*(1+m+3*n))*x^(1+2*n)
*(e*x)^m/c/d^2/n/(1+m+2*n)-b*(3*a^2*d^2*(A*d*(1+m)-B*c*(1+m+n))-3*a*b*c*d*(
A*d*(1+m+n)-B*c*(1+m+2*n))+b^2*c^2*(A*d*(1+m+2*n)-B*c*(1+m+3*n)))*(e*x)^(1+
m)/c/d^4/e/(1+m)/n-(A*d+B*c)*(e*x)^(1+m)*(a+b*x^n)^3/c/d/e/n/(c+d*x^n)+(-a
*d+b*c)^2*(a*d*(B*c*(1+m)-A*d*(1+m-n))+b*c*(A*d*(1+m+2*n)-B*c*(1+m+3*n)))*(
e*x)^(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^2/d^4/e/(1+m)/n
```

**Rubi [A]**

time = 0.74, antiderivative size = 381, normalized size of antiderivative = 0.99, number of steps used = 8, number of rules used = 5, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.161$ ,

Rules used = {608, 584, 20, 30, 371}

$\frac{((ex)^m (3a^2d^2(Ad(1+m) - Bc(1+m+n)) - 3ab^2cd(Ad(1+m+n) - Bc(1+m+2n)) - b^3(Ad(1+m+n) - Bc(1+m+2n)))x^{1+n}(ex)^m}{cd^3n(1+m+n)} - \frac{b^3(Ad(1+m+n) - Bc(1+m+2n))}{cd^3n(1+m+n)}$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n))/(c + d\*x^n)^2,x]

```
[Out] -((b^2*(3*a*d*(A*d*(1 + m + n) - B*c*(1 + m + 2*n)) - b*c*(A*d*(1 + m + 2*n)
) - B*c*(1 + m + 3*n)))*x^(1 + n)*(e*x)^m)/(c*d^3*n*(1 + m + n)) - (b^3*(A
- (B*c*(1 + m + 3*n))/(d*(1 + m + 2*n)))*x^(1 + 2*n)*(e*x)^m)/(c*d*n) - (b
*(3*a^2*d^2*(A*d*(1 + m) - B*c*(1 + m + n)) - 3*a*b*c*d*(A*d*(1 + m + n) -
B*c*(1 + m + 2*n)) + b^2*c^2*(A*d*(1 + m + 2*n) - B*c*(1 + m + 3*n)))*(e*x)
^(1 + m))/(c*d^4*e*(1 + m)*n) - ((B*c - A*d)*(e*x)^(1 + m)*(a + b*x^n)^3)/(
c*d*e*n*(c + d*x^n)) + ((b*c - a*d)^2*(a*d*(B*c*(1 + m) - A*d*(1 + m - n))
+ b*c*(A*d*(1 + m + 2*n) - B*c*(1 + m + 3*n)))*(e*x)^(1 + m)*Hypergeometric
2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)]/(c^2*d^4*e*(1 + m)*n)
```

**Rule 20**

```
Int[(u_.)*((a_.)*(v_))^(m_.)*((b_.)*(v_))^(n_), x_Symbol] := Dist[b^IntPart[
n]*((b*v)^FracPart[n]/(a^IntPart[n]*(a*v)^FracPart[n])), Int[u*(a*v)^(m + n
), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !
IntegerQ[m + n]
```

**Rule 30**

```
Int[(x_)^(m_.), x_Symbol] := Simp[x^(m + 1)/(m + 1), x] /; FreeQ[m, x] && N
eQ[m, -1]
```

Rule 371

```
Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[a^p
*((c*x)^(m + 1)/(c*(m + 1))]*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1
, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILt
Q[p, 0] || GtQ[a, 0])
```

Rule 584

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n
_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[
(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c
, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

Rule 608

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_
))^(q_.)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(
m + 1)*(a + b*x^n)^(p + 1)*(c + d*x^n)^q/(a*b*g*n*(p + 1)), x] + Dist[1/(
a*b*n*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^(q - 1)*Simp[c*
(b*e*n*(p + 1) + (b*e - a*f)*(m + 1)) + d*(b*e*n*(p + 1) + (b*e - a*f)*(m +
n*q + 1))*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[
p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b*c - a*d, b*e - a*f])
```

Rubi steps

$$\begin{aligned}
\int \frac{(ex)^m (a + bx^n)^3 (A + Bx^n)}{(c + dx^n)^2} dx &= -\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^3}{cde n (c + dx^n)} - \frac{\int \frac{(ex)^m (a + bx^n)^2 (-a(Bc(1+m) - Ad(1+m-n))}{c + dx^n} dx}{cdn} \\
&= -\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^3}{cde n (c + dx^n)} - \frac{\int \left( \frac{b(3a^2 d^2 (Ad(1+m) - Bc(1+m+n)) - 3abcd(A + Bx^n))}{c + dx^n} \right) dx}{cdn} \\
&= -\frac{b(3a^2 d^2 (Ad(1+m) - Bc(1+m+n)) - 3abcd(Ad(1+m+n) - Bc)}{cd^4 e (1 + m + n)} \\
&= -\frac{b(3a^2 d^2 (Ad(1+m) - Bc(1+m+n)) - 3abcd(Ad(1+m+n) - Bc)}{cd^4 e (1 + m + n)} \\
&= -\frac{b^2 (3ad(Ad(1+m+n) - Bc(1+m+2n)) - bc(Ad(1+m+2n) - Bc)}{cd^3 n (1 + m + n)}
\end{aligned}$$

Mathematica [A]

time = 1.96, size = 365, normalized size = 0.95

$$\frac{x^{m+1} \left( \frac{3a^2 b^2 (-Ad(1+m) + Bc(1+m+n) + Bdnx^2)}{d^2 (1+m)(c+dx^n)} - \frac{a^2 Bc - c^2 Ad}{c^2 dn + cd^2 n^2} + \frac{3a^2 d (Ad(\frac{1}{n} + \frac{m}{n+1}) + B(-\frac{1}{n} + \frac{1}{n+1} + \frac{1}{n+2} - \frac{m}{n+1}))}{d^2} + \frac{B^2 (Ad(-\frac{1}{n} + \frac{1}{n+1} - \frac{m}{n+1})) + B(\frac{1}{n} - \frac{1}{n+1} + \frac{1}{n+2} + \frac{m}{n+1})}{d^2} - \frac{(bc - ad)^2 (ad(-Bc(1+m) + Ad(1+m-n)) + bc(-Ad(1+m+2n) + Bc(1+m+3n))) {}_2F_1(1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{dx^n}{c})}{c^2 d^2 (1+m)n} \right)}{cd^3 n (1+m+n)}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)^3\*(A + B\*x^n))/(c + d\*x^n)^2,x]

[Out]  $x*(e*x)^m*((3*a^2*b*(-(A*d*(1+m)) + B*c*(1+m+n) + B*d*n*x^n))/(d^2*(1+m)*n*(c+d*x^n)) - (a^3*B*c - a^3*A*d)/(c^2*d*n + c*d^2*n*x^n) + (3*a*b^2*(A*d*((1+m)^{-1}) + c/(c*n + d*n*x^n)) + B*((-2*c)/(1+m) + (d*x^n)/(1+m+n) - c^2/(c*n + d*n*x^n)))/d^3 + (b^3*(A*d*((-2*c)/(1+m) + (d*x^n)/(1+m+n) - c^2/(c*n + d*n*x^n)) + B*((3*c^2)/(1+m) - (2*c*d*x^n)/(1+m+n) + (d^2*x^{2*n})/(1+m+2*n) + c^3/(c*n + d*n*x^n)))/d^4 - ((b*c - a*d)^2*(a*d*(-(B*c*(1+m)) + A*d*(1+m-n)) + b*c*(-(A*d*(1+m+2*n)) + B*c*(1+m+3*n)))*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(d*x^n)/c])/((c^2*d^4*(1+m)*n))$

Maple [F]

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^3 (A + Bx^n)}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)/(c+d\*x^n)^2,x)

[Out] int((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)/(c+d\*x^n)^2,x)

Maxima [F]

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^3\*(A+B\*x^n)/(c+d\*x^n)^2,x, algorithm="maxima")

[Out]  $((m*e^m + (2*n + 1)*e^m)*b^3*c^3*d - 3*(m*e^m + (n + 1)*e^m)*a*b^2*c^2*d^2 + 3*(m*e^m + e^m)*a^2*b*c*d^3 - (m*e^m - (n - 1)*e^m)*a^3*d^4)*A - ((m*e^m + (3*n + 1)*e^m)*b^3*c^4 - 3*(m*e^m + (2*n + 1)*e^m)*a*b^2*c^3*d + 3*(m*e^m + (n + 1)*e^m)*a^2*b*c^2*d^2 - (m*e^m + e^m)*a^3*c*d^3)*B)*integrate(x^m/(c*d^5*n*x^n + c^2*d^4*n), x) + ((m^2*n*e^m + (n^2 + 2*n)*m*e^m + (n^2 + n)*e^m)*B*b^3*c*d^3*x*e^{(m*log(x) + 3*n*log(x))} - ((m^3*e^m + m^2*(5*n + 3)*e^m + (8*n^2 + 10*n + 3)*m*e^m + (4*n^3 + 8*n^2 + 5*n + 1)*e^m)*b^3*c^3*d - 3*(m^3*e^m + m^2*(4*n + 3)*e^m + (5*n^2 + 8*n + 3)*m*e^m + (2*n^3 + 5*n^2 + 4*n + 1)*e^m)*a*b^2*c^2*d^2 + 3*(m^3*e^m + 3*m^2*(n + 1)*e^m + (2*n^2 + 6*n + 3)*m*e^m + (2*n^2 + 3*n + 1)*e^m)*a^2*b*c*d^3 - (m^3*e^m + 3*m^2*(n + 1)*e^m + (2*n^2 + 6*n + 3)*m*e^m + (2*n^2 + 3*n + 1)*e^m)*a^3*d^4)*A - ((m^3*e^m + 3*m^2*(2*n + 1)*e^m + (11*n^2 + 12*n + 3)*m*e^m + (6*n^3 + 11*n^2 + 6*n + 1)*e^m)*b^3*c^4 - 3*(m^3*e^m + m^2*(5*n + 3)*e^m + (8*n^2 + 10*n + 3$

```

)*m*e^m + (4*n^3 + 8*n^2 + 5*n + 1)*e^m)*a*b^2*c^3*d + 3*(m^3*e^m + m^2*(4*
n + 3)*e^m + (5*n^2 + 8*n + 3)*m*e^m + (2*n^3 + 5*n^2 + 4*n + 1)*e^m)*a^2*b
*c^2*d^2 - (m^3*e^m + 3*m^2*(n + 1)*e^m + (2*n^2 + 6*n + 3)*m*e^m + (2*n^2
+ 3*n + 1)*e^m)*a^3*c*d^3)*B)*x*x^m + ((m^2*n*e^m + 2*(n^2 + n)*m*e^m + (2*
n^2 + n)*e^m)*A*b^3*c*d^3 - ((m^2*n*e^m + (3*n^2 + 2*n)*m*e^m + (3*n^2 + n)
*e^m)*b^3*c^2*d^2 - 3*(m^2*n*e^m + 2*(n^2 + n)*m*e^m + (2*n^2 + n)*e^m)*a*b
^2*c*d^3)*B)*x*e^(m*log(x) + 2*n*log(x)) - (((m^2*n*e^m + 2*(2*n^2 + n)*m*e
^m + (4*n^3 + 4*n^2 + n)*e^m)*b^3*c^2*d^2 - 3*(m^2*n*e^m + (3*n^2 + 2*n)*m*
e^m + (2*n^3 + 3*n^2 + n)*e^m)*a*b^2*c*d^3)*A - ((m^2*n*e^m + (5*n^2 + 2*n)
*m*e^m + (6*n^3 + 5*n^2 + n)*e^m)*b^3*c^3*d - 3*(m^2*n*e^m + 2*(2*n^2 + n)*
m*e^m + (4*n^3 + 4*n^2 + n)*e^m)*a*b^2*c^2*d^2 + 3*(m^2*n*e^m + (3*n^2 + 2*
n)*m*e^m + (2*n^3 + 3*n^2 + n)*e^m)*a^2*b*c*d^3)*B)*x*e^(m*log(x) + n*log(x
)))/((m^3*n + 3*(n^2 + n)*m^2 + 2*n^3 + (2*n^3 + 6*n^2 + 3*n)*m + 3*n^2 + n
)*c*d^5*x^n + (m^3*n + 3*(n^2 + n)*m^2 + 2*n^3 + (2*n^3 + 6*n^2 + 3*n)*m +
3*n^2 + n)*c^2*d^4)

```

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="fricas")
```

```
[Out] integral((B*b^3*x^(4*n) + A*a^3 + (3*B*a*b^2 + A*b^3)*x^(3*n) + 3*(B*a^2*b
+ A*a*b^2)*x^(2*n) + (B*a^3 + 3*A*a^2*b)*x^n)*(x*e)^m/(d^2*x^(2*n) + 2*c*d*
x^n + c^2), x)

```

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)**3*(A+B*x**n)/(c+d*x**n)**2,x)
```

```
[Out] Exception raised: HeuristicGCDFailed >> no luck

```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^3*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="giac")
```

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^3\*(x\*e)^m/(d\*x^n + c)^2, x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^3}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^3)/(c + d\*x^n)^2,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^3)/(c + d\*x^n)^2, x)

$$3.30 \quad \int \frac{(ex)^m (a+bx^n)^2 (A+Bx^n)}{(c+dx^n)^2} dx$$

**Optimal.** Leaf size=267

$$\frac{b^2(Ad(1+m+n) - Bc(1+m+2n))x^{1+n}(ex)^m}{cd^2n(1+m+n)} - \frac{b(2ad(Ad(1+m) - Bc(1+m+n)) - bc(Ad(1+m+n) - Bc(1+m+2n)))}{cd^3e(1+m)n}$$

[Out]  $-b^2(A*d*(1+m+n)-B*c*(1+m+2*n))*x^{(1+n)}*(e*x)^m/c/d^2/n/(1+m+n)-b*(2*a*d*(A*d*(1+m)-B*c*(1+m+n))-b*c*(A*d*(1+m+n)-B*c*(1+m+2*n)))*(e*x)^{(1+m)}/c/d^3/e/(1+m)/n-(-A*d+B*c)*(e*x)^{(1+m)}*(a+b*x^n)^2/c/d/e/n/(c+d*x^n)-(-a*d+b*c)*(a*d*(B*c*(1+m)-A*d*(1+m-n))+b*c*(A*d*(1+m+n)-B*c*(1+m+2*n)))*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^2/d^3/e/(1+m)/n$

**Rubi [A]**

time = 0.45, antiderivative size = 267, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.161$ , Rules used = {608, 584, 20, 30, 371}

$$\frac{(ex)^{m+1}(bc-ad)_2F_1\left(1, \frac{m+1}{n}, \frac{m+1+n}{n}, -\frac{dx^n}{c}\right) (ad(Bc(m+1) - Ad(m-n+1)) + bc(Ad(m+n+1) - Bc(m+2n+1)))}{c^2d^2e(m+1)n} - \frac{b(ex)^{m+1}(2ad(Ad(m+1) - Bc(m+n+1)) - bc(Ad(m+n+1) - Bc(m+2n+1)))}{cd^2e(m+1)n} - \frac{(ex)^{m+1}(a+bx^n)^2(Bc-Ad)}{cd^2e(m+1)n} - \frac{b^2x^{m+1}(ex)^m(Ad(m+n+1) - Bc(m+2n+1))}{cd^2e(m+n+1)n}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n))/(c + d\*x^n)^2,x]

[Out]  $-((b^2(A*d*(1+m+n) - B*c*(1+m+2*n))*x^{(1+n)}*(e*x)^m)/(c*d^2*n*(1+m+n)) - (b*(2*a*d*(A*d*(1+m) - B*c*(1+m+n)) - b*c*(A*d*(1+m+n) - B*c*(1+m+2*n)))*(e*x)^{(1+m)}/(c*d^3*e*(1+m)*n) - ((B*c - A*d)*(e*x)^{(1+m)}*(a + b*x^n)^2)/(c*d*e*n*(c + d*x^n)) - ((b*c - a*d)*(a*d*(B*c*(1+m) - A*d*(1+m-n)) + b*c*(A*d*(1+m+n) - B*c*(1+m+2*n)))*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)])/ (c^2*d^3*e*(1+m)*n)$

Rule 20

Int[(u\_)\*((a\_)\*(v\_))^(m\_)\*((b\_)\*(v\_))^(n\_), x\_Symbol] := Dist[b^IntPart[n]\*((b\*v)^FracPart[n]/(a^IntPart[n]\*(a\*v)^FracPart[n])), Int[u\*(a\*v)^(m+n), x], x] /; FreeQ[{a, b, m, n}, x] && !IntegerQ[m] && !IntegerQ[n] && !IntegerQ[m+n]

Rule 30

Int[(x\_)^(m\_), x\_Symbol] := Simp[x^(m+1)/(m+1), x] /; FreeQ[m, x] && NeQ[m, -1]

Rule 371



```
Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[a^p
*((c*x)^(m + 1)/(c*(m + 1)))*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1
, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILt
Q[p, 0] || GtQ[a, 0])
```

### Rule 584

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n
_))^(q_.)*((e_) + (f_.)*(x_)^(n_))^(r_.), x_Symbol] := Int[ExpandIntegrand[
(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(e + f*x^n)^r, x], x] /; FreeQ[{a, b, c
, d, e, f, g, m, n}, x] && IGtQ[p, -2] && IGtQ[q, 0] && IGtQ[r, 0]
```

### Rule 608

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n
_))^(q_.)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(
m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^q/(a*b*g*n*(p + 1))), x] + Dist[1/(
a*b*n*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^(q - 1)*Simp[c*
(b*e*n*(p + 1) + (b*e - a*f)*(m + 1)) + d*(b*e*n*(p + 1) + (b*e - a*f)*(m +
n*q + 1))*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[
p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b*c - a*d, b*e - a*f])
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (a + bx^n)^2 (A + Bx^n)}{(c + dx^n)^2} dx &= -\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^2}{c d e n (c + dx^n)} - \frac{\int \frac{(ex)^m (a + bx^n)^{-a(Bc(1+m) - Ad(1+m-n))}}{c + dx^n} c d n}{c d n} \\ &= -\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^2}{c d e n (c + dx^n)} - \frac{\int \left( \frac{b(2ad(Ad(1+m) - Bc(1+m+n)) - bc(Ad(1+m+n) - Bc(1+m+n))}{d^2} \right)}{c d e n (c + dx^n)} \\ &= -\frac{b(2ad(Ad(1+m) - Bc(1+m+n)) - bc(Ad(1+m+n) - Bc(1+m+n))}{c d^3 e (1+m)n} \\ &= -\frac{b(2ad(Ad(1+m) - Bc(1+m+n)) - bc(Ad(1+m+n) - Bc(1+m+n))}{c d^3 e (1+m)n} \\ &= -\frac{b^2(Ad(1+m+n) - Bc(1+m+2n))x^{1+n}(ex)^m}{c d^2 n (1+m+n)} - \frac{b(2ad(Ad(1+m+n) - Bc(1+m+n))}{c d^2 n (1+m+n)} \end{aligned}$$

### Mathematica [A]

time = 0.82, size = 249, normalized size = 0.93

$$x(ex)^m \left( \frac{2ab(-Ad(1+m) + Bc(1+m+n) + Bdnx^n)}{d^2(1+m)n(c+dx^n)} - \frac{a^2Bc - a^2Ad}{c^2dn + cd^2nx^n} + \frac{b^2 \left( Ad \left( \frac{1}{1+m} + \frac{c}{a+dx^n} \right) + B \left( -\frac{2c}{1+m} + \frac{d^2}{1+m^2n} - \frac{c^2}{a+dx^n} \right) \right)}{d^3} + \frac{(bc - ad)(ad(-Bc(1+m) + Ad(1+m-n)) + bc(-Ad(1+m+n) + Bc(1+m+2n))) {}_2F_1 \left( 1, \frac{1+m}{n}; \frac{1+m+n}{c}; -\frac{d^2}{c} \right)}{c^2 d^2 (1+m)n} \right)$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n))/(c + d\*x^n)^2,x]

[Out] x\*(e\*x)^m\*((2\*a\*b\*(-(A\*d\*(1 + m)) + B\*c\*(1 + m + n) + B\*d\*n\*x^n))/(d^2\*(1 + m)\*n\*(c + d\*x^n)) - (a^2\*B\*c - a^2\*A\*d)/(c^2\*d\*n + c\*d^2\*n\*x^n) + (b^2\*(A\*d\*((1 + m)^(-1) + c/(c\*n + d\*n\*x^n)) + B\*((-2\*c)/(1 + m) + (d\*x^n)/(1 + m + n) - c^2/(c\*n + d\*n\*x^n))))/d^3 + ((b\*c - a\*d)\*(a\*d\*(-(B\*c\*(1 + m)) + A\*d\*(1 + m - n)) + b\*c\*(-(A\*d\*(1 + m + n)) + B\*c\*(1 + m + 2\*n)))\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)]/(c^2\*d^3\*(1 + m)\*n))

**Maple** [F]

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^2 (A + Bx^n)}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n)^2,x)

[Out] int((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n)^2,x)

**Maxima** [F]

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n)^2,x, algorithm="maxima")

[Out] -(((m\*e^m + (n + 1)\*e^m)\*b^2\*c^2\*d - 2\*(m\*e^m + e^m)\*a\*b\*c\*d^2 + (m\*e^m - (n - 1)\*e^m)\*a^2\*d^3)\*A - ((m\*e^m + (2\*n + 1)\*e^m)\*b^2\*c^3 - 2\*(m\*e^m + (n + 1)\*e^m)\*a\*b\*c^2\*d + (m\*e^m + e^m)\*a^2\*c\*d^2)\*B)\*integrate(x^m/(c\*d^4\*n\*x^n + c^2\*d^3\*n), x) + ((m\*n\*e^m + n\*e^m)\*B\*b^2\*c\*d^2\*x\*e^(m\*log(x) + 2\*n\*log(x)) + (((m^2\*e^m + 2\*m\*(n + 1)\*e^m + (n^2 + 2\*n + 1)\*e^m)\*b^2\*c^2\*d - 2\*(m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a\*b\*c\*d^2 + (m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a^2\*d^3)\*A - ((m^2\*e^m + m\*(3\*n + 2)\*e^m + (2\*n^2 + 3\*n + 1)\*e^m)\*b^2\*c^3 - 2\*(m^2\*e^m + 2\*m\*(n + 1)\*e^m + (n^2 + 2\*n + 1)\*e^m)\*a\*b\*c^2\*d + (m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*a^2\*c\*d^2)\*B)\*x\*x^m + ((m\*n\*e^m + (n^2 + n)\*e^m)\*A\*b^2\*c\*d^2 - ((m\*n\*e^m + (2\*n^2 + n)\*e^m)\*b^2\*c^2\*d - 2\*(m\*n\*e^m + (n^2 + n)\*e^m)\*a\*b\*c\*d^2)\*B)\*x\*x^m + ((m^2\*n + (n^2 + 2\*n)\*m + n^2 + n)\*c\*d^4\*x^n + (m^2\*n + (n^2 + 2\*n)\*m + n^2 + n)\*c^2\*d^3)

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n)^2,x, algorithm="fricas")

[Out] integral((B\*b^2\*x^(3\*n) + A\*a^2 + (2\*B\*a\*b + A\*b^2)\*x^(2\*n) + (B\*a^2 + 2\*A\*a\*b)\*x^n)\*(x\*e)^m/(d^2\*x^(2\*n) + 2\*c\*d\*x^n + c^2), x)

**Sympy** [F]

time = 0.00, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^2}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*2\*(A+B\*x\*\*n)/(c+d\*x\*\*n)\*\*2,x)

[Out] Integral((e\*x)\*\*m\*(A + B\*x\*\*n)\*(a + b\*x\*\*n)\*\*2/(c + d\*x\*\*n)\*\*2, x)

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n)^2,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^2\*(x\*e)^m/(d\*x^n + c)^2, x)

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^2}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^2)/(c + d\*x^n)^2,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^2)/(c + d\*x^n)^2, x)

$$3.31 \quad \int \frac{(ex)^m (a+bx^n)(A+Bx^n)}{(c+dx^n)^2} dx$$

**Optimal.** Leaf size=178

$$\frac{B(ad(1+m) - bc(1+m+n))(ex)^{1+m}}{cd^2e(1+m)n} - \frac{(bc-ad)(ex)^{1+m}(A+Bx^n)}{cden(c+dx^n)} + \frac{(Ad(bc(1+m) - ad(1+m-n))}{cd^2e(1+m)n}$$

[Out]  $-B*(a*d*(1+m)-b*c*(1+m+n))*(e*x)^{(1+m)}/c/d^2/e/(1+m)/n - (-a*d+b*c)*(e*x)^{(1+m)}*(A+B*x^n)/c/d/e/n/(c+d*x^n) + (A*d*(b*c*(1+m)-a*d*(1+m-n))+B*c*(a*d*(1+m)-b*c*(1+m+n))*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^2/d^2/e/(1+m)/n$

**Rubi [A]**

time = 0.17, antiderivative size = 178, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {608, 470, 371}

$$\frac{(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}, -\frac{dx^n}{c}\right) (Ad(bc(m+1) - ad(m-n+1)) + Bc(ad(m+1) - bc(m+n+1)))}{c^2 d^2 e (m+1)n} - \frac{(ex)^{m+1} (bc-ad)(A+Bx^n)}{cden(c+dx^n)} - \frac{B(ex)^{m+1} (ad(m+1) - bc(m+n+1))}{cd^2 e (m+1)n}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n))/(c + d\*x^n)^2,x]

[Out]  $-((B*(a*d*(1+m) - b*c*(1+m+n))*(e*x)^{(1+m)})/(c*d^2*e*(1+m)*n) - ((b*c - a*d)*(e*x)^{(1+m)}*(A + B*x^n))/(c*d*e*n*(c + d*x^n)) + ((A*d*(b*c*(1+m) - a*d*(1+m-n)) + B*c*(a*d*(1+m) - b*c*(1+m+n)))*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)]/(c^2*d^2*e*(1+m)*n)$

Rule 371

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 470

Int[((e\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_)), x\_Symbol] := Simp[d\*(e\*x)^(m+1)\*((a + b\*x^n)^(p+1)/(b\*e\*(m+n\*(p+1)+1))), x] - Dist[(a\*d\*(m+1) - b\*c\*(m+n\*(p+1)+1))/(b\*(m+n\*(p+1)+1)), Int[(e\*x)^m\*(a + b\*x^n)^p, x], x] /; FreeQ[{a, b, c, d, e, m, n, p}, x] && NeQ[b\*c - a\*d, 0] && NeQ[m + n\*(p+1) + 1, 0]

Rule 608

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_)), x\_Symbol] := Simp[(-b\*e - a\*f)\*(g\*x)^(

```

m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^q/(a*b*g*n*(p + 1))), x] + Dist[1/(
a*b*n*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^(q - 1)*Simp[c*
(b*e*n*(p + 1) + (b*e - a*f)*(m + 1)) + d*(b*e*n*(p + 1) + (b*e - a*f)*(m +
n*q + 1))*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[
p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b*c - a*d, b*e - a*f])

```

Rubi steps

$$\begin{aligned}
\int \frac{(ex)^m (a + bx^n) (A + Bx^n)}{(c + dx^n)^2} dx &= -\frac{(bc - ad)(ex)^{1+m} (A + Bx^n)}{cdn(c + dx^n)} - \frac{\int \frac{(ex)^m (-A(bc(1+m) - ad(1+m-n)) + B(ad(1+m) - bc(1+m+n))}{c + dx^n} dx}{cdn} \\
&= -\frac{B(ad(1+m) - bc(1+m+n))(ex)^{1+m}}{cd^2e(1+m)n} - \frac{(bc - ad)(ex)^{1+m} (A + Bx^n)}{cdn(c + dx^n)} \\
&= -\frac{B(ad(1+m) - bc(1+m+n))(ex)^{1+m}}{cd^2e(1+m)n} - \frac{(bc - ad)(ex)^{1+m} (A + Bx^n)}{cdn(c + dx^n)}
\end{aligned}$$

**Mathematica [A]**

time = 0.29, size = 193, normalized size = 1.08

$$\frac{x(ex)^m \left( bc(-Bc + Ad) + ad \left( Bc + \frac{Ad(-1-m+n)}{1+m} \right) + \frac{ad(-Bc(1+m) + Ad(1+m-n) + bc(-Ad(1+m) + Bc(1+m+n)))}{1+m} + \frac{c(bc-ad)(Bc-Ad)}{c+dx^n} - \frac{(ad(-Bc(1+m) + Ad(1+m-n) + bc(-Ad(1+m) + Bc(1+m+n))) {}_2F_1 \left( 1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c} \right)}{1+m} \right)}{c^2 d^2 n}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n))/(c + d\*x^n)^2,x]

[Out] (x\*(e\*x)^m\*(b\*c\*(-(B\*c) + A\*d) + a\*d\*(B\*c + (A\*d\*(-1 - m + n))/(1 + m)) + (a\*d\*(-(B\*c\*(1 + m)) + A\*d\*(1 + m - n)) + b\*c\*(-(A\*d\*(1 + m)) + B\*c\*(1 + m + n)))/(1 + m) + (c\*(b\*c - a\*d)\*(B\*c - A\*d))/(c + d\*x^n) - ((a\*d\*(-(B\*c\*(1 + m)) + A\*d\*(1 + m - n)) + b\*c\*(-(A\*d\*(1 + m)) + B\*c\*(1 + m + n)))\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)]/(1 + m))/(c^2\*d^2\*n)

**Maple [F]**

time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n) (A + Bx^n)}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^2,x)

[Out] int((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^2,x, algorithm="maxima")

[Out] (((m\*e^m + e^m)\*b\*c\*d - (m\*e^m - (n - 1)\*e^m)\*a\*d^2)\*A - ((m\*e^m + (n + 1)\*e^m)\*b\*c^2 - (m\*e^m + e^m)\*a\*c\*d)\*B)\*integrate(x^m/(c\*d^3\*n\*x^n + c^2\*d^2\*n), x) + (B\*b\*c\*d\*n\*x\*e^(m\*log(x) + n\*log(x) + m) - (((m\*e^m + e^m)\*b\*c\*d - (m\*e^m + e^m)\*a\*d^2)\*A - ((m\*e^m + (n + 1)\*e^m)\*b\*c^2 - (m\*e^m + e^m)\*a\*c\*d)\*B)\*x\*x^m)/((m\*n + n)\*c\*d^3\*x^n + (m\*n + n)\*c^2\*d^2)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^2,x, algorithm="fricas")

[Out] integral((B\*b\*x^(2\*n) + A\*a + (B\*a + A\*b)\*x^n)\*(x\*e)^m/(d^2\*x^(2\*n) + 2\*c\*d\*x^n + c^2), x)

**Sympy [C]** Result contains complex when optimal does not.

time = 31.12, size = 4129, normalized size = 23.20

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*(A+B\*x\*\*n)/(c+d\*x\*\*n)\*\*2,x)

[Out] A\*a\*(-e\*\*m\*m\*\*2\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*(c\*n\*\*3\*gamma(m/n + 1 + 1/n) + d\*n\*\*3\*x\*\*n\*gamma(m/n + 1 + 1/n))) + e\*\*m\*m\*n\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*(c\*n\*\*3\*gamma(m/n + 1 + 1/n) + d\*n\*\*3\*x\*\*n\*gamma(m/n + 1 + 1/n))) + e\*\*m\*m\*n\*x\*x\*\*m\*gamma(m/n + 1/n)/(c\*(c\*n\*\*3\*gamma(m/n + 1 + 1/n) + d\*n\*\*3\*x\*\*n\*gamma(m/n + 1 + 1/n))) - 2\*e\*\*m\*m\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*(c\*n\*\*3\*gamma(m/n + 1 + 1/n) + d\*n\*\*3\*x\*\*n\*gamma(m/n + 1 + 1/n))) + e\*\*m\*n\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)/(c\*(c\*n\*\*3\*gamma(m/n + 1 + 1/n) + d\*n\*\*3\*x\*\*n\*gamma(m/n + 1 + 1/n))) + e\*\*m\*n\*x\*x\*\*m\*gamma(m/n + 1/n)/(c\*(c\*n\*\*3\*gamma(m/n + 1 + 1/n) + d\*n\*\*3\*x\*\*n\*gamma(m/n + 1 + 1/n))) - e\*\*m\*x\*x\*\*m\*lerchphi(d\*x\*\*n\*exp\_polar(I\*pi)/c, 1, m/n + 1/n)\*gamma(m/n + 1/n)



```

2*e**m*m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*g
amma(m/n + 1 + 1/n)/(c*(c*n**3*gamma(m/n + 2 + 1/n) + d*n**3*x**n*gamma(m/n
+ 2 + 1/n))) + e**m*n**2*x*x**m*x**n*gamma(m/n + 1 + 1/n)/(c*(c*n**3*gamma
(m/n + 2 + 1/n) + d*n**3*x**n*gamma(m/n + 2 + 1/n))) - e**m*n*x*x**m*x**n*l
erchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c
*(c*n**3*gamma(m/n + 2 + 1/n) + d*n**3*x**n*gamma(m/n + 2 + 1/n))) + e**m*n
*x*x**m*x**n*gamma(m/n + 1 + 1/n)/(c*(c*n**3*gamma(m/n + 2 + 1/n) + d*n**3*
x**n*gamma(m/n + 2 + 1/n))) - e**m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*
pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*(c*n**3*gamma(m/n + 2 + 1/
n) + d*n**3*x**n*gamma(m/n + 2 + 1/n))) - d*e**...

```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="giac")
```

```
[Out] integrate((B*x^n + A)*(b*x^n + a)*(x*e)^m/(d*x^n + c)^2, x)
```

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(e x)^m (A + B x^n) (a + b x^n)}{(c + d x^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(((e*x)^m*(A + B*x^n)*(a + b*x^n))/(c + d*x^n)^2,x)
```

```
[Out] int(((e*x)^m*(A + B*x^n)*(a + b*x^n))/(c + d*x^n)^2, x)
```



$$3.32 \quad \int \frac{(ex)^m(A+Bx^n)}{(c+dx^n)^2} dx$$

**Optimal.** Leaf size=107

$$-\frac{(Bc - Ad)(ex)^{1+m}}{cde n(c + dx^n)} + \frac{(Bc(1 + m) - Ad(1 + m - n))(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{c^2de(1 + m)n}$$

[Out]  $-(A*d+B*c)*(e*x)^{(1+m)}/c/d/e/n/(c+d*x^n)+(B*c*(1+m)-A*d*(1+m-n))*(e*x)^{(1+m)}*\text{hypergeom}\left(1, (1+m)/n, [(1+m+n)/n], -d*x^n/c\right)/c^2/d/e/(1+m)/n$

**Rubi** [A]

time = 0.04, antiderivative size = 107, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$ , Rules used = {468, 371}

$$\frac{(ex)^{m+1}(Bc(m+1) - Ad(m-n+1)) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right)}{c^2de(m+1)n} - \frac{(ex)^{m+1}(Bc - Ad)}{cde n(c + dx^n)}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(A + B*x^n)/(c + d*x^n)^2, x]$

[Out]  $-(((B*c - A*d)*(e*x)^{(1 + m)})/(c*d*e*n*(c + d*x^n))) + ((B*c*(1 + m) - A*d*(1 + m - n))*(e*x)^{(1 + m)}*\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)])/(c^2*d*e*(1 + m)*n)$

Rule 371

$\text{Int}[(c_*)*(x_)^{(m_*)}*((a_) + (b_)*(x_)^{(n_)})^{(p_)}, x\_Symbol] \rightarrow \text{Simp}[a^p * ((c*x)^{(m+1)}/(c*(m+1)))*\text{Hypergeometric2F1}[-p, (m+1)/n, (m+1)/n + 1, (-b)*(x^n/a)], x] /;$  FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 468

$\text{Int}[(e_*)*(x_)^{(m_*)}*((a_) + (b_)*(x_)^{(n_)})^{(p_*)}*((c_) + (d_)*(x_)^{(n_)})], x\_Symbol] \rightarrow \text{Simp}[(-b*c - a*d)*(e*x)^{(m+1)}*((a + b*x^n)^{(p+1)}/(a*b*e*n*(p+1))), x] - \text{Dist}[(a*d*(m+1) - b*c*(m+n*(p+1)+1))/(a*b*n*(p+1)), \text{Int}[(e*x)^m*(a + b*x^n)^{(p+1)}, x], x] /;$  FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && LtQ[p, -1] && (( !IntegerQ[p + 1/2] && NeQ[p, -5/4]) || !RationalQ[m] || (IGtQ[n, 0] && ILtQ[p + 1/2, 0] && LeQ[-1, m, (-n)\*(p + 1)]))

Rubi steps

$$\int \frac{(ex)^m (A + Bx^n)}{(c + dx^n)^2} dx = -\frac{(Bc - Ad)(ex)^{1+m}}{cde n (c + dx^n)} + \frac{(Bc(1 + m) - Ad(1 + m - n)) \int \frac{(ex)^m}{c + dx^n} dx}{cde n}$$

$$= -\frac{(Bc - Ad)(ex)^{1+m}}{cde n (c + dx^n)} + \frac{(Bc(1 + m) - Ad(1 + m - n))(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{c^2 de (1 + m) n}$$

**Mathematica [A]**

time = 0.14, size = 84, normalized size = 0.79

$$\frac{x(ex)^m \left( \frac{c(-Bc+Ad)}{c+dx^n} + \frac{(Bc(1+m)+Ad(-1-m+n)) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{1+m} \right)}{c^2 de n}$$

Antiderivative was successfully verified.

`[In] Integrate[((e*x)^m*(A + B*x^n))/(c + d*x^n)^2,x]`

```
[Out] (x*(e*x)^m*((c*(-B*c) + A*d))/(c + d*x^n) + ((B*c*(1 + m) + A*d*(-1 - m + n))*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)]/(1 + m)))/(c^2*d*n)
```

**Maple [F]**

time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

`[In] int((e*x)^m*(A+B*x^n)/(c+d*x^n)^2,x)``[Out] int((e*x)^m*(A+B*x^n)/(c+d*x^n)^2,x)`**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

`[In] integrate((e*x)^m*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="maxima")`

```
[Out] -(B*c*e^m - A*d*e^m)*x*x^m/(c*d^2*n*x^n + c^2*d*n) + ((m*e^m + e^m)*B*c - (m*e^m - (n - 1)*e^m)*A*d)*integrate(x^m/(c*d^2*n*x^n + c^2*d*n), x)
```

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

`[In] integrate((e*x)^m*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="fricas")``[Out] integral((B*x^n + A)*(x*e)^m/(d^2*x^(2*n) + 2*c*d*x^n + c^2), x)`**Sympy [C]** Result contains complex when optimal does not.

time = 9.76, size = 1897, normalized size = 17.73

Too large to display

Verification of antiderivative is not currently implemented for this CAS.

`[In] integrate((e*x)**m*(A+B*x**n)/(c+d*x**n)**2,x)`

```
[Out] A*(-e**m*m**2*x*x**m*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) + e**m*m*n*x*x**m*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) + e**m*m*n*x*x**m*gamma(m/n + 1/n)/(c*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) - 2*e**m*m*x*x**m*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) + e**m*n*x*x**m*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) + e**m*n*x*x**m*gamma(m/n + 1/n)/(c*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) - e**m*x*x**m*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) - d*e**m*m**2*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c**2*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) + d*e**m*m*n*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c**2*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) - 2*d*e**m*m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c**2*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) + d*e**m*n*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c**2*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) - d*e**m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1/n)*gamma(m/n + 1/n)/(c**2*(c*n**3*gamma(m/n + 1 + 1/n) + d*n**3*x**n*gamma(m/n + 1 + 1/n))) + B*(-e**m*m**2*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*(c*n**3*gamma(m/n + 2 + 1/n) + d*n**3*x**n*gamma(m/n + 2 + 1/n))) - e**m*m*n*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)
```

```

*gamma(m/n + 1 + 1/n)/(c*(c**3*gamma(m/n + 2 + 1/n) + d**3*x**n*gamma(m
/n + 2 + 1/n))) + e**m*m*n*x*x**m*x**n*gamma(m/n + 1 + 1/n)/(c*(c**3*gamma
a(m/n + 2 + 1/n) + d**3*x**n*gamma(m/n + 2 + 1/n))) - 2*e**m*m*x*x**m*x**
n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)
/(c*(c**3*gamma(m/n + 2 + 1/n) + d**3*x**n*gamma(m/n + 2 + 1/n))) + e**
m*n**2*x*x**m*x**n*gamma(m/n + 1 + 1/n)/(c*(c**3*gamma(m/n + 2 + 1/n) + d
**3*x**n*gamma(m/n + 2 + 1/n))) - e**m*n*x*x**m*x**n*lerchphi(d*x**n*exp_
polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c*(c**3*gamma(m/n
+ 2 + 1/n) + d**3*x**n*gamma(m/n + 2 + 1/n))) + e**m*n*x*x**m*x**n*gamma(
m/n + 1 + 1/n)/(c*(c**3*gamma(m/n + 2 + 1/n) + d**3*x**n*gamma(m/n + 2
+ 1/n))) - e**m*x*x**m*x**n*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 +
1/n)*gamma(m/n + 1 + 1/n)/(c*(c**3*gamma(m/n + 2 + 1/n) + d**3*x**n*ga
mma(m/n + 2 + 1/n))) - d*e**m*m**2*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_pola
r(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c**2*(c**3*gamma(m/n +
2 + 1/n) + d**3*x**n*gamma(m/n + 2 + 1/n))) - d*e**m*m*n*x*x**m*x**(2*n)
*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/
(c**2*(c**3*gamma(m/n + 2 + 1/n) + d**3*x**n*gamma(m/n + 2 + 1/n))) - 2
*d*e**m*m*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1
/n)*gamma(m/n + 1 + 1/n)/(c**2*(c**3*gamma(m/n + 2 + 1/n) + d**3*x**n*ga
mma(m/n + 2 + 1/n))) - d*e**m*n*x*x**m*x**(2*n)*lerchphi(d*x**n*exp_polar(
I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c**2*(c**3*gamma(m/n + 2
+ 1/n) + d**3*x**n*gamma(m/n + 2 + 1/n))) - d*e**m*x*x**m*x**(2*n)*lerch
phi(d*x**n*exp_polar(I*pi)/c, 1, m/n + 1 + 1/n)*gamma(m/n + 1 + 1/n)/(c**2*
(c**3*gamma(m/n + 2 + 1/n) + d**3*x**n*gamma(m/n + 2 + 1/n)))

```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="giac")
```

```
[Out] integrate((B*x^n + A)*(x*e)^m/(d*x^n + c)^2, x)
```

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(ex)^m (A + Bx^n)}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(((e*x)^m*(A + B*x^n))/(c + d*x^n)^2,x)
```

```
[Out] int(((e*x)^m*(A + B*x^n))/(c + d*x^n)^2, x)
```

$$3.33 \quad \int \frac{(ex)^m (A+Bx^n)}{(a+bx^n)(c+dx^n)^2} dx$$

**Optimal.** Leaf size=211

$$\frac{(Bc - Ad)(ex)^{1+m}}{c(bc - ad)en(c + dx^n)} + \frac{b(Ab - aB)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{a(bc - ad)^2 e(1+m)} + \frac{(bc(Ad(1+m-2n) - Bc(1+m))}{c^2 e(m+1)n(bc - ad)^2}$$

[Out]  $(-A*d+B*c)*(e*x)^{(1+m)}/c/(-a*d+b*c)/e/n/(c+d*x^n)+b*(A*b-B*a)*(e*x)^{(1+m)*h}$   
 $ypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/a/(-a*d+b*c)^2/e/(1+m)+(b*c*(A*$   
 $d*(1+m-2*n)-B*c*(1+m-n))+a*d*(B*c*(1+m)-A*d*(1+m-n)))*(e*x)^{(1+m)*hypergeom$   
 $([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^2/(-a*d+b*c)^2/e/(1+m)/n$

**Rubi [A]**

time = 0.35, antiderivative size = 211, normalized size of antiderivative = 1.00, number of steps used = 5, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {609, 611, 371}

$$\frac{(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right) (ad(Bc(m+1) - Ad(m-n+1)) + bc(Ad(m-2n+1) - Bc(m-n+1)))}{c^2 e(m+1)n(bc - ad)^2} + \frac{b(ex)^{m+1} (Ab - aB) {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{bx^n}{a}\right)}{ae(m+1)(bc - ad)^2} + \frac{(ex)^{m+1} (Bc - Ad)}{cen(bc - ad)(c + dx^n)}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(A + B*x^n)/((a + b*x^n)*(c + d*x^n)^2), x]$

[Out]  $((B*c - A*d)*(e*x)^{(1+m)}/(c*(b*c - a*d)*e*n*(c + d*x^n)) + (b*(A*b - a*B)$   
 $)*(e*x)^{(1+m)*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((b*x^n)/a)$   
 $])/(a*(b*c - a*d)^2*e*(1+m)) + ((b*c*(A*d*(1+m-2*n) - B*c*(1+m-n)$   
 $) + a*d*(B*c*(1+m) - A*d*(1+m-n)))*(e*x)^{(1+m)*Hypergeometric2F1[1,$   
 $(1+m)/n, (1+m+n)/n, -((d*x^n)/c)])/(c^2*(b*c - a*d)^2*e*(1+m)*n$

Rule 371

$\text{Int}[(c_*)*(x_)^{(m_*)}*((a_*) + (b_*)*(x_)^{(n_*)})^{(p_*)}, x\_Symbol] \rightarrow \text{Simp}[a^p$   
 $*((c*x)^{(m+1)}/(c*(m+1)))*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1$   
 $, (-b)*(x^n/a)], x] /; \text{FreeQ}\{a, b, c, m, n, p\}, x \ \&\& \ !\text{IGtQ}[p, 0] \ \&\& \ (\text{ILt}$   
 $Q[p, 0] \ || \ \text{GtQ}[a, 0])$

Rule 609

$\text{Int}[(g_*)*(x_)^{(m_*)}*((a_*) + (b_*)*(x_)^{(n_*)})^{(p_*)}*((c_*) + (d_*)*(x_)^{(n_*)}$   
 $)^{(q_*)}*((e_*) + (f_*)*(x_)^{(n_*)}), x\_Symbol] \rightarrow \text{Simp}[(-b*e - a*f)*(g*x)^{(m$   
 $+ 1)*(a + b*x^n)^{(p+1)}*((c + d*x^n)^{(q+1)}/(a*g*n*(b*c - a*d)*(p+1))$   
 $, x] + \text{Dist}[1/(a*n*(b*c - a*d)*(p+1)), \text{Int}[(g*x)^m*(a + b*x^n)^{(p+1)}*(c$   
 $+ d*x^n)^q*\text{Simp}[c*(b*e - a*f)*(m+1) + e*n*(b*c - a*d)*(p+1) + d*(b*e -$   
 $a*f)*(m+n*(p+q+2)+1)*x^n, x], x] /; \text{FreeQ}\{a, b, c, d, e, f, g$   
 $, m, n, q\}, x \ \&\& \ \text{LtQ}[p, -1]$

## Rule 611

```
Int[(((g_)*(x_)^(m_))*((a_) + (b_)*(x_)^(n_))^(p_))*((e_) + (f_)*(x_)^(n_)))/((c_) + (d_)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x]
```

## Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)(c + dx^n)^2} dx &= \frac{(Bc - Ad)(ex)^{1+m}}{c(bc - ad)en(c + dx^n)} + \frac{\int \frac{(ex)^m (-a(Bc - Ad)(1+m) + A(bc - ad)n - b(Bc - Ad)(1+m-n)x^n)}{(a+bx^n)(c+dx^n)} dx}{c(bc - ad)n} \\ &= \frac{(Bc - Ad)(ex)^{1+m}}{c(bc - ad)en(c + dx^n)} + \frac{\int \left( \frac{b(Ab - aB)cn(ex)^m}{(bc - ad)(a + bx^n)} + \frac{(bc(Ad(1+m-2n) - Bc(1+m-n)) + ad(Bc(1+m-n) - Bc(1+m-n)))}{(bc - ad)(c + dx^n)} \right) dx}{c(bc - ad)n} \\ &= \frac{(Bc - Ad)(ex)^{1+m}}{c(bc - ad)en(c + dx^n)} + \frac{(b(Ab - aB)) \int \frac{(ex)^m}{a + bx^n} dx}{(bc - ad)^2} + \frac{(bc(Ad(1+m-2n) - Bc(1+m-n)) - Bc(1+m-n))}{c(bc - ad)n} \\ &= \frac{(Bc - Ad)(ex)^{1+m}}{c(bc - ad)en(c + dx^n)} + \frac{b(Ab - aB)(ex)^{1+m} {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{a(bc - ad)^2 e(1+m)} + \frac{(bc(Ad(1+m-2n) - Bc(1+m-n)) - Bc(1+m-n))}{c(bc - ad)n} \end{aligned}$$

**Mathematica [A]**

time = 0.36, size = 177, normalized size = 0.84

$$\frac{x(ex)^m \left( \frac{(bc-ad)(Bc-Ad)}{cn(c+dx^n)} + \frac{b(Ab-aB) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{a(1+m)} - \frac{(bc(-Ad(1+m-2n)+Bc(1+m-n))+ad(-Bc(1+m)+Ad(1+m-n))) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{c^2(1+m)n} \right)}{(bc - ad)^2}$$

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(A + B*x^n))/((a + b*x^n)*(c + d*x^n)^2), x]
```

```
[Out] (x*(e*x)^m*(((b*c - a*d)*(B*c - A*d))/(c*n*(c + d*x^n)) + (b*(A*b - a*B)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)]/(a*(1 + m)) - ((b*c*(-(A*d*(1 + m - 2*n)) + B*c*(1 + m - n)) + a*d*(-(B*c*(1 + m)) + A*d*(1 + m - n)))*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)]/(c^2*(1 + m)*n)))/(b*c - a*d)^2
```

**Maple [F]**

time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{int}((e*x)^m*(A+B*x^n)/(a+b*x^n)/(c+d*x^n)^2,x)$

[Out]  $\text{int}((e*x)^m*(A+B*x^n)/(a+b*x^n)/(c+d*x^n)^2,x)$

**Maxima** [F]

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e*x)^m*(A+B*x^n)/(a+b*x^n)/(c+d*x^n)^2,x, \text{algorithm}="maxima")$

[Out]  $(B*c*e^m - A*d*e^m)*x*x^m/(b*c^3*n - a*c^2*d*n + (b*c^2*d*n - a*c*d^2*n)*x^n) + (((m*e^m - (2*n - 1)*e^m)*b*c*d - (m*e^m - (n - 1)*e^m)*a*d^2)*A - ((m*e^m - (n - 1)*e^m)*b*c^2 - (m*e^m + e^m)*a*c*d)*B*\text{integrate}(x^m/(b^2*c^4*n - 2*a*b*c^3*d*n + a^2*c^2*d^2*n + (b^2*c^3*d*n - 2*a*b*c^2*d^2*n + a^2*c*d^3*n)*x^n), x) - (B*a*b*e^m - A*b^2*e^m)*\text{integrate}(x^m/(a*b^2*c^2 - 2*a^2*b*c*d + a^3*d^2 + (b^3*c^2 - 2*a*b^2*c*d + a^2*b*d^2)*x^n), x)$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e*x)^m*(A+B*x^n)/(a+b*x^n)/(c+d*x^n)^2,x, \text{algorithm}="fricas")$

[Out]  $\text{integral}((B*x^n + A)*(x*e)^m/(b*d^2*x^{(3*n)} + a*c^2 + (2*b*c*d + a*d^2)*x^{(2*n)} + (b*c^2 + 2*a*c*d)*x^n), x)$

**Sympy** [F(-2)]

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e*x)**m*(A+B*x**n)/(a+b*x**n)/(c+d*x**n)**2,x)$

[Out] Exception raised: HeuristicGCDFailed >> no luck

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In]  $\text{integrate}((e*x)^m*(A+B*x^n)/(a+b*x^n)/(c+d*x^n)^2,x, \text{algorithm}="giac")$

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)\*(d\*x^n + c)^2), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)\*(c + d\*x^n)^2), x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)\*(c + d\*x^n)^2), x)



$$3.34 \quad \int \frac{(ex)^m (A+Bx^n)}{(a+bx^n)^2 (c+dx^n)^2} dx$$

**Optimal.** Leaf size=315

$$\frac{d(ABC - 2aBc + aAd)(ex)^{1+m}}{ac(bc - ad)^2 en (c + dx^n)} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)} + \frac{b(aB(bc(1 + m) - ad(1 + m - 2n)) + a^2c)}{a^2c(bc - ad)^2 en (c + dx^n)}$$

```
[Out] d*(A*a*d+A*b*c-2*B*a*c)*(e*x)^(1+m)/a/c/(-a*d+b*c)^2/e/n/(c+d*x^n)+(A*b-B*a)
*(e*x)^(1+m)/(-a*d+b*c)/e/n/(a+b*x^n)/(c+d*x^n)+b*(a*B*(b*c*(1+m)-a*d*(1
+m-2*n))+A*b*(a*d*(1+m-3*n)-b*c*(1+m-n)))*(e*x)^(1+m)*hypergeom([1, (1+m)/n
],[ (1+m+n)/n], -b*x^n/a)/a^2/(-a*d+b*c)^3/e/(1+m)/n-d*(b*c*(A*d*(1+m-3*n)-B*
c*(1+m-2*n))+a*d*(B*c*(1+m)-A*d*(1+m-n)))*(e*x)^(1+m)*hypergeom([1, (1+m)/n
],[ (1+m+n)/n], -d*x^n/c)/c^2/(-a*d+b*c)^3/e/(1+m)/n
```

**Rubi [A]**

time = 0.72, antiderivative size = 315, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {609, 611, 371}

$$\frac{b(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+1}{n}; -\frac{bc}{a}\right) (Ab(ad(m-3n+1) - bc(m-n+1)) + aB(bc(m+1) - ad(m-2n+1)))}{a^2e(m+1)n(bc-ad)^2} - \frac{d(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+1}{n}; -\frac{dc}{c}\right) (ad(Bc(m+1) - Ad(m-n+1)) + bc(Ad(m-3n+1) - Bc(m-2n+1)))}{c^2e(m+1)n(bc-ad)^2} + \frac{d(ex)^{m+1} (aAd - 2aBc + Abc)}{acn(bc-ad)^2(c+dx^n)} + \frac{(ex)^{m+1} (Ab - aB)}{aen(bc-ad)(a+bx^n)(c+dx^n)}$$

Antiderivative was successfully verified.

```
[In] Int[((e*x)^m*(A + B*x^n))/((a + b*x^n)^2*(c + d*x^n)^2), x]
```

```
[Out] (d*(A*b*c - 2*a*B*c + a*A*d)*(e*x)^(1 + m))/(a*c*(b*c - a*d)^2*e*n*(c + d*x
^n)) + ((A*b - a*B)*(e*x)^(1 + m))/(a*(b*c - a*d)*e*n*(a + b*x^n)*(c + d*x
^n)) + (b*(a*B*(b*c*(1 + m) - a*d*(1 + m - 2*n)) + A*b*(a*d*(1 + m - 3*n) -
b*c*(1 + m - n)))*(e*x)^(1 + m)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)
/n, -((b*x^n)/a)])/a^2*(b*c - a*d)^3*e*(1 + m)*n - (d*(b*c*(A*d*(1 + m -
3*n) - B*c*(1 + m - 2*n)) + a*d*(B*c*(1 + m) - A*d*(1 + m - n)))*(e*x)^(1 +
m)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)])/c^2*(b*c
- a*d)^3*e*(1 + m)*n
```

**Rule 371**

```
Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[a^p
*((c*x)^(m + 1)/(c*(m + 1))]*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1
, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILt
Q[p, 0] || GtQ[a, 0])
```

**Rule 609**

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_
))^q_)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(m
+ 1)*(a + b*x^n)^(p + 1)*(c + d*x^n)^(q + 1)/(a*g*n*(b*c - a*d)*(p + 1))
, x] + Dist[1/(a*n*(b*c - a*d)*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c
```

```
+ d*x^n)^q*Simp[c*(b*e - a*f)*(m + 1) + e*n*(b*c - a*d)*(p + 1) + d*(b*e -
a*f)*(m + n*(p + q + 2) + 1)*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g
, m, n, q}, x] && LtQ[p, -1]
```

### Rule 611

```
Int[(((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_.))^(p_.)*((e_) + (f_.)*(x_)^(n
_)))/((c_) + (d_.)*(x_)^(n_.)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a
+ b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g,
m, n, p}, x]
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)^2} dx &= \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)} - \frac{\int \frac{(ex)^m (-aBc(1+m) + Abc(1+m-n) + aAdn + (Ab - aB)(a + bx^n)(c + dx^n)^2)}{a(bc - ad)n} dx}{a(bc - ad)n} \\ &= \frac{d(Abc - 2aBc + aAd)(ex)^{1+m}}{ac(bc - ad)^2 en (c + dx^n)} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)} - \frac{\int \frac{(ex)^m (-aBc(1+m) + Abc(1+m-n) + aAdn + (Ab - aB)(a + bx^n)(c + dx^n)^2)}{a(bc - ad)n} dx}{a(bc - ad)n} \\ &= \frac{d(Abc - 2aBc + aAd)(ex)^{1+m}}{ac(bc - ad)^2 en (c + dx^n)} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)} - \frac{\int \left( \frac{bc(-aBc(1+m) + Abc(1+m-n) + aAdn + (Ab - aB)(a + bx^n)(c + dx^n)^2)}{a(bc - ad)n} \right) dx}{a(bc - ad)n} \\ &= \frac{d(Abc - 2aBc + aAd)(ex)^{1+m}}{ac(bc - ad)^2 en (c + dx^n)} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)} + \frac{b(aB(bc - ad) - a^2)}{a^2(bc - ad)^2} \\ &= \frac{d(Abc - 2aBc + aAd)(ex)^{1+m}}{ac(bc - ad)^2 en (c + dx^n)} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)} + \frac{b(aB(bc - ad) - a^2)}{a^2(bc - ad)^2} \end{aligned}$$

### Mathematica [A]

time = 0.74, size = 242, normalized size = 0.77

$$\frac{x(ex)^m \left( \frac{b(-Ab+aB)(-bc+ad)}{a(a+bx^n)} + \frac{d(-bc+ad)(Bc-Ad)}{c(c+dx^n)} - \frac{b(aB(-bc(1+m)+ad(1+m-2n))+Ab(-ad(1+m-3n)+bc(1+m-n))}{a^2(1+m)} {}_2F_1\left(1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{bx^n}{a}\right) + \frac{d(bc(-Ad(1+m-3n)+Bc(1+m-2n))+ad(-Bc(1+m)+Ad(1+m-n))}{c^2(1+m)} {}_2F_1\left(1, \frac{1+m}{n}, \frac{1+m+n}{n}, -\frac{dx^n}{c}\right) \right)}{(bc - ad)^{2n}}$$

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(A + B*x^n))/((a + b*x^n)^2*(c + d*x^n)^2), x]
```

```
[Out] (x*(e*x)^m*((b*(-(A*b) + a*B)*(-(b*c) + a*d))/(a*(a + b*x^n)) + (d*(-(b*c)
+ a*d)*(B*c - A*d))/(c*(c + d*x^n)) - (b*(a*B*(-(b*c*(1 + m)) + a*d*(1 + m
- 2*n)) + A*b*(-(a*d*(1 + m - 3*n)) + b*c*(1 + m - n)))*Hypergeometric2F1[1
, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)]/(a^2*(1 + m)) + (d*(b*c*(-(A*d*(
1 + m - 3*n)) + B*c*(1 + m - 2*n)) + a*d*(-(B*c*(1 + m)) + A*d*(1 + m - n))
)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)]/(c^2*(1 + m
))))/(b*c - a*d)^3*n)
```

**Maple [F]**

time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^2,x)

[Out] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^2,x, algorithm="maxima")

```
[Out] (((m*e^m - (n - 1)*e^m)*b^3*c - (m*e^m - (3*n - 1)*e^m)*a*b^2*d)*A - ((m*e^m + e^m)*a*b^2*c - (m*e^m - (2*n - 1)*e^m)*a^2*b*d)*B)*integrate(-x^m/(a^2*b^3*c^3*n - 3*a^3*b^2*c^2*d*n + 3*a^4*b*c*d^2*n - a^5*d^3*n + (a*b^4*c^3*n - 3*a^2*b^3*c^2*d*n + 3*a^3*b^2*c*d^2*n - a^4*b*d^3*n)*x^n), x) + (((m*e^m - (3*n - 1)*e^m)*b*c*d^2 - (m*e^m - (n - 1)*e^m)*a*d^3)*A - ((m*e^m - (2*n - 1)*e^m)*b*c^2*d - (m*e^m + e^m)*a*c*d^2)*B)*integrate(-x^m/(b^3*c^5*n - 3*a*b^2*c^4*d*n + 3*a^2*b*c^3*d^2*n - a^3*c^2*d^3*n + (b^3*c^4*d*n - 3*a*b^2*c^3*d^2*n + 3*a^2*b*c^2*d^3*n - a^3*c*d^4*n)*x^n), x) + (((b^2*c^2*e^m + a^2*d^2*e^m)*A - (a*b*c^2*e^m + a^2*c*d*e^m)*B)*x*x^m - (2*B*a*b*c*d*e^m - (b^2*c*d*e^m + a*b*d^2*e^m)*A)*x*e^(m*log(x) + n*log(x)))/(a^2*b^2*c^4*n - 2*a^3*b*c^3*d*n + a^4*c^2*d^2*n + (a*b^3*c^3*d*n - 2*a^2*b^2*c^2*d^2*n + a^3*b*c*d^3*n)*x^(2*n) + (a*b^3*c^4*n - a^2*b^2*c^3*d*n - a^3*b*c^2*d^2*n + a^4*c*d^3*n)*x^n)
```

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^2,x, algorithm="fricas")

```
[Out] integral((B*x^n + A)*(x*e)^m/(b^2*d^2*x^(4*n) + a^2*c^2 + 2*(b^2*c*d + a*b*d^2)*x^(3*n) + (b^2*c^2 + 4*a*b*c*d + a^2*d^2)*x^(2*n) + 2*(a*b*c^2 + a^2*c*d)*x^n), x)
```

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)/(a+b\*x\*\*n)\*\*2/(c+d\*x\*\*n)\*\*2,x)

[Out] Exception raised: HeuristicGCDFailed >> no luck

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^2,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)^2\*(d\*x^n + c)^2), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(e x)^m (A + B x^n)}{(a + b x^n)^2 (c + d x^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)^2),x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)^2), x)

$$3.35 \quad \int \frac{(ex)^m (A+Bx^n)}{(a+bx^n)^3 (c+dx^n)^2} dx$$

**Optimal.** Leaf size=567

$$\frac{d(aBc(bc(1+m) - ad(1+m-6n)) + A(abcd(1+m-6n) - b^2c^2(1+m-2n) - 2a^2d^2n))(ex)^{1+m}}{2a^2c(bc-ad)^3en^2(c+dx^n)} + \frac{2a($$

[Out]  $1/2*d*(a*B*c*(b*c*(1+m)-a*d*(1+m-6*n))+A*(a*b*c*d*(1+m-6*n)-b^2*c^2*(1+m-2*n)-2*a^2*d^2*n))*(e*x)^{(1+m)}/a^2/c/(-a*d+b*c)^3/e/n^2/(c+d*x^n)+1/2*(A*b-B*a)*(e*x)^{(1+m)}/a/(-a*d+b*c)/e/n/(a+b*x^n)^2/(c+d*x^n)+1/2*(a*B*(b*c*(1+m)-a*d*(1+m-3*n))+A*b*(a*d*(1+m-5*n)-b*c*(1+m-2*n)))*(e*x)^{(1+m)}/a^2/(-a*d+b*c)^2/e/n^2/(a+b*x^n)/(c+d*x^n)+1/2*b*(a*B*(2*a*b*c*d*(1+m)*(1+m-3*n)-b^2*c^2*(1+m)*(1+m-n)-a^2*d^2*(1+m^2+m*(2-5*n)-5*n+6*n^2))+A*b*(b^2*c^2*(1+m^2+m*(2-3*n)-3*n+2*n^2)-2*a*b*c*d*(1+m^2+m*(2-5*n)-5*n+4*n^2)+a^2*d^2*(1+m^2+m*(2-7*n)-7*n+12*n^2)))*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/a^3/(-a*d+b*c)^4/e/(1+m)/n^2+d^2*(b*c*(A*d*(1+m-4*n)-B*c*(1+m-3*n))+a*d*(B*c*(1+m)-A*d*(1+m-n)))*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^2/(-a*d+b*c)^4/e/(1+m)/n$

**Rubi [A]**

time = 1.56, antiderivative size = 567, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {609, 611, 371}

Antiderivative was successfully verified.

[In]  $\text{Int}[\frac{(e*x)^m*(A + B*x^n)}{(a + b*x^n)^3*(c + d*x^n)^2}, x]$

[Out]  $(d*(a*B*c*(b*c*(1+m) - a*d*(1+m-6*n)) + A*(a*b*c*d*(1+m-6*n) - b^2*c^2*(1+m-2*n) - 2*a^2*d^2*n))*(e*x)^{(1+m)}/(2*a^2*c*(b*c - a*d)^3*e*n^2*(c + d*x^n)) + ((A*b - a*B)*(e*x)^{(1+m)}/(2*a*(b*c - a*d)*e*n*(a + b*x^n)^2*(c + d*x^n)) + ((a*B*(b*c*(1+m) - a*d*(1+m-3*n)) + A*b*(a*d*(1+m-5*n) - b*c*(1+m-2*n)))*(e*x)^{(1+m)}/(2*a^2*(b*c - a*d)^2*e*n^2*(a + b*x^n)*(c + d*x^n)) + (b*(a*B*(2*a*b*c*d*(1+m)*(1+m-3*n) - b^2*c^2*(1+m)*(1+m-n) - a^2*d^2*(1+m^2+m*(2-5*n) - 5*n+6*n^2)) + A*b*(b^2*c^2*(1+m^2+m*(2-3*n) - 3*n+2*n^2) - 2*a*b*c*d*(1+m^2+m*(2-5*n) - 5*n+4*n^2) + a^2*d^2*(1+m^2+m*(2-7*n) - 7*n+12*n^2)))*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((b*x^n)/a)])/ (2*a^3*(b*c - a*d)^4*e*(1+m)*n^2) + (d^2*(b*c*(A*d*(1+m-4*n) - B*c*(1+m-3*n)) + a*d*(B*c*(1+m) - A*d*(1+m-n)))*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)])/ (c^2*(b*c - a*d)^4*e*(1+m)*n)$

Rule 371

```
Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[a^p
*((c*x)^(m + 1)/(c*(m + 1)))*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1
, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILt
Q[p, 0] || GtQ[a, 0])
```

### Rule 609

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_
))^ (q_)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(m
+ 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^(q + 1)/(a*g*n*(b*c - a*d)*(p + 1))
, x] + Dist[1/(a*n*(b*c - a*d)*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c
+ d*x^n)^q*Simp[c*(b*e - a*f)*(m + 1) + e*n*(b*c - a*d)*(p + 1) + d*(b*e -
a*f)*(m + n*(p + q + 2) + 1)*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g
, m, n, q}, x] && LtQ[p, -1]
```

### Rule 611

```
Int[(((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((e_) + (f_.)*(x_)^(n_
)))/((c_) + (d_.)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a
+ b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g,
m, n, p}, x]
```

### Rubi steps

$$\begin{aligned}
\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^3 (c + dx^n)^2} dx &= \frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en (a + bx^n)^2 (c + dx^n)} - \frac{\int \frac{(ex)^m (-aBc(1+m) + Abc(1+m-2n) + 2aAdn + (Ab - aB)c)}{(a + bx^n)^2 (c + dx^n)^2} dx}{2a(bc - ad)n} \\
&= \frac{(Ab - aB)(ex)^{1+m}}{2a(bc - ad)en (a + bx^n)^2 (c + dx^n)} + \frac{(aB(bc(1 + m) - ad(1 + m - 3n)) + A(bc(1 + m) - ad(1 + m - 3n)))}{2a^2(bc - ad)^2 en} \\
&= \frac{d(aBc(bc(1 + m) - ad(1 + m - 6n)) + A(abcd(1 + m - 6n) - b^2c^2(1 + m - 6n))}{2a^2c(bc - ad)^3 en^2 (c + dx^n)} \\
&= \frac{d(aBc(bc(1 + m) - ad(1 + m - 6n)) + A(abcd(1 + m - 6n) - b^2c^2(1 + m - 6n))}{2a^2c(bc - ad)^3 en^2 (c + dx^n)} \\
&= \frac{d(aBc(bc(1 + m) - ad(1 + m - 6n)) + A(abcd(1 + m - 6n) - b^2c^2(1 + m - 6n))}{2a^2c(bc - ad)^3 en^2 (c + dx^n)} \\
&= \frac{d(aBc(bc(1 + m) - ad(1 + m - 6n)) + A(abcd(1 + m - 6n) - b^2c^2(1 + m - 6n))}{2a^2c(bc - ad)^3 en^2 (c + dx^n)}
\end{aligned}$$

**Mathematica** [B] Leaf count is larger than twice the leaf count of optimal. 2176 vs. 2(567) = 1134.

time = 1.88, size = 2176, normalized size = 3.84

Result too large to show

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^3\*(c + d\*x^n)^2),x]

[Out]  $(x*(e*x)^m*(2*a^3*c*d^2*(b*c - a*d)*(B*c - A*d)*(1 + m)*n*(a + b*x^n)^2 + a^2*b*(A*b - a*B)*c^2*(b*c - a*d)^2*(1 + m)*n*(c + d*x^n) + a*b*c^2*(-(b*c) + a*d)*(1 + m)*(a*B*(-(b*c*(1 + m)) + a*d*(1 + m - 4*n)) + A*b*(-(a*d*(1 + m - 6*n)) + b*c*(1 + m - 2*n)))*(a + b*x^n)*(c + d*x^n) + A*b^4*c^4*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - a*b^3*B*c^4*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 2*a*A*b^3*c^3*d*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 2*a^2*b^2*B*c^3*d*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + a^2*A*b^2*c^2*d^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - a^3*b*B*c^2*d^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 2*A*b^4*c^4*m*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 2*a*b^3*B*c^4*m*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 4*a*A*b^3*c^3*d*m*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 4*a^2*b^2*B*c^3*d*m*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 2*a^2*A*b^2*c^2*d^2*m*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 2*a^3*b*B*c^2*d^2*m*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + A*b^4*c^4*m^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - a*b^3*B*c^4*m^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 2*a*A*b^3*c^3*d*m^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 2*a^2*b^2*B*c^3*d*m^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + a^2*A*b^2*c^2*d^2*m^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - a^3*b*B*c^2*d^2*m^2*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 3*A*b^4*c^4*n*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + a*b^3*B*c^4*n*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 10*a*A*b^3*c^3*d*n*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 6*a^2*b^2*B*c^3*d*n*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 7*a^2*A*b^2*c^2*d^2*n*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] + 5*a^3*b*B*c^2*d^2*n*(a + b*x^n)^2*(c + d*x^n)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)] - 3*A*b^4*c$

$$c^4 m^n (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] + a b^3 B c^4 m^n (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] + 10 a A b^3 c^3 d m^n (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] - 6 a^2 b^2 B c^3 d m^n (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] - 7 a^2 A b^2 c^2 d^2 m^n (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] + 5 a^3 b B c^2 d^2 m^n (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] + 2 A b^4 c^4 n^2 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] - 8 a A b^3 c^3 d n^2 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] + 12 a^2 A b^2 c^2 d^2 n^2 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] - 6 a^3 b B c^2 d^2 n^2 (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((b x^n)/a)] + 2 a^3 d^2 n (b c (A d (1 + m - 4 n) - B c (1 + m - 3 n)) + a d (B c (1 + m) + A d (-1 - m + n))) (a + b x^n)^2 (c + d x^n) \text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d x^n)/c)] / (2 a^3 c^2 (b c - a d)^4 (1 + m) n^2 (a + b x^n)^2 (c + d x^n))$$

**Maple [F]**

time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^3 (c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n)^2,x)

[Out] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n)^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n)^2,x, algorithm="maxima")

[Out] ((m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*b^4\*c^2 - 2\*(m^2\*e^m - m\*(5\*n - 2)\*e^m + (4\*n^2 - 5\*n + 1)\*e^m)\*a\*b^3\*c\*d + (m^2\*e^m - m\*(7\*n - 2)\*e^m + (12\*n^2 - 7\*n + 1)\*e^m)\*a^2\*b^2\*d^2)\*A - ((m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a\*b^3\*c^2 - 2\*(m^2\*e^m - m\*(3\*n - 2)\*e^m - (3\*n - 1)\*e^m)\*a^2\*b^2\*c\*d + (m^2\*e^m - m\*(5\*n - 2)\*e^m + (6\*n^2 - 5\*n + 1)\*e^m)\*a^3\*b\*d^2)\*B)\*integrate(1/2\*x^m/(a^3\*b^4\*c^4\*n^2 - 4\*a^4\*b^3\*c^3\*d\*n^2 + 6\*a^5\*b^2\*c^2\*d^2\*n^2 - 4\*a^6\*b\*c\*d^3\*n^2 + a^7\*d^4\*n^2 + (a^2\*b^5\*c^4\*n^2 - 4\*a^3\*b^4\*c^3\*d\*n^2 + 6\*a^4\*b^3\*c^2\*d^2\*n^2 - 4\*a^5\*b^2\*c\*d^3\*n^2 + a^6\*b\*d^4\*n^2)\*x^



$$n), x) + (((m*e^m - (4*n - 1)*e^m)*b*c*d^3 - (m*e^m - (n - 1)*e^m)*a*d^4)*A - ((m*e^m - (3*n - 1)*e^m)*b*c^2*d^2 - (m*e^m + e^m)*a*c*d^3)*B)*integrate(x^m/(b^4*c^6*n - 4*a*b^3*c^5*d*n + 6*a^2*b^2*c^4*d^2*n - 4*a^3*b*c^3*d^3*n + a^4*c^2*d^4*n + (b^4*c^5*d*n - 4*a*b^3*c^4*d^2*n + 6*a^2*b^2*c^3*d^3*n - 4*a^3*b*c^2*d^4*n + a^4*c*d^5*n)*x^n), x) - 1/2*(((2*a^4*d^3*n*e^m + (m*e^m - (3*n - 1)*e^m)*a*b^3*c^3 - (m*e^m - (7*n - 1)*e^m)*a^2*b^2*c^2*d)*A - (2*a^4*c*d^2*n*e^m + (m*e^m - (n - 1)*e^m)*a^2*b^2*c^3 - (m*e^m - (5*n - 1)*e^m)*a^3*b*c^2*d)*B)*x*x^m + ((2*a^2*b^2*d^3*n*e^m + (m*e^m - (2*n - 1)*e^m)*b^4*c^2*d - (m*e^m - (6*n - 1)*e^m)*a*b^3*c*d^2)*A - ((m*e^m + e^m)*a*b^3*c^2*d - (m*e^m - (6*n - 1)*e^m)*a^2*b^2*c*d^2)*B)*x*e^(m*log(x) + 2*n*log(x)) + (((3*a*b^3*c^2*d*n*e^m + 4*a^3*b*d^3*n*e^m + (m*e^m - (2*n - 1)*e^m)*b^4*c^3 - (m*e^m - (7*n - 1)*e^m)*a^2*b^2*c*d^2)*A - (3*a^2*b^2*c^2*d*n*e^m + (m*e^m + e^m)*a*b^3*c^3 - (m*e^m - (9*n - 1)*e^m)*a^3*b*c*d^2)*B)*x*e^(m*log(x) + n*log(x)))/(a^4*b^3*c^5*n^2 - 3*a^5*b^2*c^4*d*n^2 + 3*a^6*b*c^3*d^2*n^2 - a^7*c^2*d^3*n^2 + (a^2*b^5*c^4*d*n^2 - 3*a^3*b^4*c^3*d^2*n^2 + 3*a^4*b^3*c^2*d^3*n^2 - a^5*b^2*c*d^4*n^2)*x^(3*n) + (a^2*b^5*c^5*n^2 - a^3*b^4*c^4*d*n^2 - 3*a^4*b^3*c^3*d^2*n^2 + 5*a^5*b^2*c^2*d^3*n^2 - 2*a^6*b*c*d^4*n^2)*x^(2*n) + (2*a^3*b^4*c^5*n^2 - 5*a^4*b^3*c^4*d*n^2 + 3*a^5*b^2*c^3*d^2*n^2 + a^6*b*c^2*d^3*n^2 - a^7*c*d^4*n^2)*x^n)$$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n)^2,x, algorithm="fricas")

[Out] integral((B\*x^n + A)\*(x\*e)^m/(b^3\*d^2\*x^(5\*n) + a^3\*c^2 + (2\*b^3\*c\*d + 3\*a\*b^2\*d^2)\*x^(4\*n) + (b^3\*c^2 + 6\*a\*b^2\*c\*d + 3\*a^2\*b\*d^2)\*x^(3\*n) + (3\*a\*b^2\*c^2 + 6\*a^2\*b\*c\*d + a^3\*d^2)\*x^(2\*n) + (3\*a^2\*b\*c^2 + 2\*a^3\*c\*d)\*x^n), x)

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)/(a+b\*x\*\*n)\*\*3/(c+d\*x\*\*n)\*\*2,x)

[Out] Timed out

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^3/(c+d\*x^n)^2,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)^3\*(d\*x^n + c)^2), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(e x)^m (A + B x^n)}{(a + b x^n)^3 (c + d x^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^3\*(c + d\*x^n)^2),x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^3\*(c + d\*x^n)^2), x)

$$3.36 \quad \int \frac{(ex)^m (a+bx^n)^2 (A+Bx^n)}{(c+dx^n)^3} dx$$

**Optimal.** Leaf size=322

$$\frac{b(ad(1+m) - bc(1+m+n))(Ad(1+m) - Bc(1+m+2n))(ex)^{1+m}}{2c^2d^3e(1+m)n^2} - \frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^2}{2cden (c + dx^n)^2} - \frac{(b$$

```
[Out] 1/2*b*(a*d*(1+m)-b*c*(1+m+n))*(A*d*(1+m)-B*c*(1+m+2*n))*(e*x)^(1+m)/c^2/d^3
/e/(1+m)/n^2-1/2*(-A*d+B*c)*(e*x)^(1+m)*(a+b*x^n)^2/c/d/e/n/(c+d*x^n)^2-1/2
*(-a*d+b*c)*(e*x)^(1+m)*(a*(B*c*(1+m)-A*d*(1+m-2*n))-b*(A*d*(1+m)-B*c*(1+m+
2*n))*x^n)/c^2/d^2/e/n^2/(c+d*x^n)+1/2*(a*d*(B*c*(1+m)-A*d*(1+m-2*n))*(b*c*
(1+m)-a*d*(1+m-n))-b*c*(a*d*(1+m)-b*c*(1+m+n))*(A*d*(1+m)-B*c*(1+m+2*n))*
(e*x)^(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^3/d^3/e/(1+m)/n^2
```

**Rubi [A]**

time = 0.37, antiderivative size = 322, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {608, 470, 371}

$$\frac{(ex)^{m+1} F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{d}{c}\right) (ad(b(m+1) - a(m-n+1))(Bc(m+1) - Ad(m-2n+1)) - bc(ad(m+1) - b(m+n+1))(Ad(m+1) - Bc(m+2n+1)))}{2c^2d^3e(1+m)n^2} - \frac{(ex)^{m+1} (a+bx^n)^2 (Bc - Ad)}{2c^2den(c+dx^n)^2} - \frac{(ex)^{m+1} (a+bx^n)^2 (Bc - Ad)}{2cden(c+dx^n)^2}$$

Antiderivative was successfully verified.

```
[In] Int[((e*x)^m*(a + b*x^n)^2*(A + B*x^n))/(c + d*x^n)^3,x]
```

```
[Out] (b*(a*d*(1 + m) - b*c*(1 + m + n))*(A*d*(1 + m) - B*c*(1 + m + 2*n))*(e*x)^(
1 + m))/(2*c^2*d^3*e*(1 + m)*n^2) - ((B*c - A*d)*(e*x)^(1 + m)*(a + b*x^n)
^2)/(2*c*d*e*n*(c + d*x^n)^2) - ((b*c - a*d)*(e*x)^(1 + m)*(a*(B*c*(1 + m)
- A*d*(1 + m - 2*n)) - b*(A*d*(1 + m) - B*c*(1 + m + 2*n))*x^n)/(2*c^2*d^2
*e*n^2*(c + d*x^n)) + ((a*d*(B*c*(1 + m) - A*d*(1 + m - 2*n))*(b*c*(1 + m)
- a*d*(1 + m - n)) - b*c*(a*d*(1 + m) - b*c*(1 + m + n))*(A*d*(1 + m) - B*c
*(1 + m + 2*n))*(e*x)^(1 + m)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/
n, -(d*x^n/c)]/(2*c^3*d^3*e*(1 + m)*n^2)
```

**Rule 371**

```
Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] :> Simp[a^p
*((c*x)^(m + 1)/(c*(m + 1)))*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1
, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILt
Q[p, 0] || GtQ[a, 0])
```

**Rule 470**

```
Int[((e_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n
_)), x_Symbol] :> Simp[d*(e*x)^(m + 1)*((a + b*x^n)^(p + 1)/(b*e*(m + n*(p
+ 1) + 1))), x] - Dist[(a*d*(m + 1) - b*c*(m + n*(p + 1) + 1))/(b*(m + n*(p
```

+ 1) + 1)), Int[(e\*x)^m\*(a + b\*x^n)^p, x], x] /; FreeQ[{a, b, c, d, e, m, n, p}, x] && NeQ[b\*c - a\*d, 0] && NeQ[m + n\*(p + 1) + 1, 0]

### Rule 608

Int[((g\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_.)\*((e\_) + (f\_.)\*(x\_)^(n\_)), x\_Symbol] := Simp[(-b\*e - a\*f)\*(g\*x)^(m + 1)\*(a + b\*x^n)^(p + 1)\*(c + d\*x^n)^q/(a\*b\*g\*n\*(p + 1)), x] + Dist[1/(a\*b\*n\*(p + 1)), Int[(g\*x)^m\*(a + b\*x^n)^(p + 1)\*(c + d\*x^n)^(q - 1)\*Simp[c\*(b\*e\*n\*(p + 1) + (b\*e - a\*f)\*(m + 1)) + d\*(b\*e\*n\*(p + 1) + (b\*e - a\*f)\*(m + n\*q + 1))\*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b\*c - a\*d, b\*e - a\*f])

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (a + bx^n)^2 (A + Bx^n)}{(c + dx^n)^3} dx &= -\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^2}{2cdn (c + dx^n)^2} - \frac{\int \frac{(ex)^m (a + bx^n) (-a(Bc(1+m) - Ad(1+m-2n))}{(c + dx^n)^2}}{2cdn} \\ &= -\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^2}{2cdn (c + dx^n)^2} - \frac{(bc - ad)(ex)^{1+m} (a(Bc(1+m) - A}}{2c^2d^3e(1+m)n^2} \\ &= \frac{b(ad(1+m) - bc(1+m+n))(Ad(1+m) - Bc(1+m+2n))(ex)^{1+m}}{2c^2d^3e(1+m)n^2} \\ &= \frac{b(ad(1+m) - bc(1+m+n))(Ad(1+m) - Bc(1+m+2n))(ex)^{1+m}}{2c^2d^3e(1+m)n^2} \end{aligned}$$

**Mathematica** [B] Leaf count is larger than twice the leaf count of optimal. 1924 vs. 2(322) = 644.

time = 1.14, size = 1924, normalized size = 5.98

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)^2\*(A + B\*x^n))/(c + d\*x^n)^3,x]

[Out] (x\*(e\*x)^m\*(-(b^2\*B\*c^5\*(1 + m)\*n) + A\*b^2\*c^4\*d\*(1 + m)\*n + 2\*a\*b\*B\*c^4\*d\*(1 + m)\*n - 2\*a\*A\*b\*c^3\*d^2\*(1 + m)\*n - a^2\*B\*c^3\*d^2\*(1 + m)\*n + a^2\*A\*c^2\*d^3\*(1 + m)\*n + b^2\*B\*c^4\*(1 + m)\*(c + d\*x^n) - A\*b^2\*c^3\*d\*(1 + m)\*(c + d\*x^n) - 2\*a\*b\*B\*c^3\*d\*(1 + m)\*(c + d\*x^n) + 2\*a\*A\*b\*c^2\*d^2\*(1 + m)\*(c + d\*x^n) + a^2\*B\*c^2\*d^2\*(1 + m)\*(c + d\*x^n) - a^2\*A\*c\*d^3\*(1 + m)\*(c + d\*x^n) + b^2\*B\*c^4\*m\*(1 + m)\*(c + d\*x^n) - A\*b^2\*c^3\*d\*m\*(1 + m)\*(c + d\*x^n) - 2\*a

$$\begin{aligned}
& *b*B*c^3*d*m*(1+m)*(c+d*x^n) + 2*a*A*b*c^2*d^2*m*(1+m)*(c+d*x^n) + \\
& a^2*B*c^2*d^2*m*(1+m)*(c+d*x^n) - a^2*A*c*d^3*m*(1+m)*(c+d*x^n) + 4 \\
& *b^2*B*c^4*(1+m)*n*(c+d*x^n) - 2*A*b^2*c^3*d*(1+m)*n*(c+d*x^n) - 4* \\
& a*b*B*c^3*d*(1+m)*n*(c+d*x^n) + 2*a^2*A*c*d^3*(1+m)*n*(c+d*x^n) + 2 \\
& *b^2*B*c^3*n^2*(c+d*x^n)^2 - b^2*B*c^3*(c+d*x^n)^2*Hypergeometric2F1[1, \\
& (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + A*b^2*c^2*d*(c+d*x^n)^2*Hyperg \\
& eometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + 2*a*b*B*c^2*d*(c+d \\
& *x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] - 2* \\
& a*A*b*c*d^2*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -( \\
& (d*x^n)/c)] - a^2*B*c*d^2*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1 \\
& +m+n)/n, -((d*x^n)/c)] + a^2*A*d^3*(c+d*x^n)^2*Hypergeometric2F1[1, (1 \\
& +m)/n, (1+m+n)/n, -((d*x^n)/c)] - 2*b^2*B*c^3*m*(c+d*x^n)^2*Hyperge \\
& ometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + 2*A*b^2*c^2*d*m*(c \\
& +d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + 4 \\
& *a*b*B*c^2*d*m*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, \\
& -((d*x^n)/c)] - 4*a*A*b*c*d^2*m*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m) \\
& /n, (1+m+n)/n, -((d*x^n)/c)] - 2*a^2*B*c*d^2*m*(c+d*x^n)^2*Hypergeome \\
& tric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + 2*a^2*A*d^3*m*(c+d*x \\
& ^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] - b^2*B* \\
& c^3*m^2*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x \\
& ^n)/c)] + A*b^2*c^2*d*m^2*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1 \\
& +m+n)/n, -((d*x^n)/c)] + 2*a*b*B*c^2*d*m^2*(c+d*x^n)^2*Hypergeometric2 \\
& F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] - 2*a*A*b*c*d^2*m^2*(c+d*x \\
& ^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] - a^2*B*c \\
& *d^2*m^2*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x \\
& ^n)/c)] + a^2*A*d^3*m^2*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m \\
& +n)/n, -((d*x^n)/c)] - 3*b^2*B*c^3*n*(c+d*x^n)^2*Hypergeometric2F1[1, \\
& (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + A*b^2*c^2*d*n*(c+d*x^n)^2*Hype \\
& rgeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + 2*a*b*B*c^2*d*n* \\
& (c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] \\
& + 2*a*A*b*c*d^2*n*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n) \\
& /n, -((d*x^n)/c)] + a^2*B*c*d^2*n*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m \\
& )/n, (1+m+n)/n, -((d*x^n)/c)] - 3*a^2*A*d^3*n*(c+d*x^n)^2*Hypergeomet \\
& ric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] - 3*b^2*B*c^3*m*n*(c+d* \\
& x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + A*b^2 \\
& *c^2*d*m*n*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(( \\
& d*x^n)/c)] + 2*a*b*B*c^2*d*m*n*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n \\
& , (1+m+n)/n, -((d*x^n)/c)] + 2*a*A*b*c*d^2*m*n*(c+d*x^n)^2*Hypergeome \\
& tric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] + a^2*B*c*d^2*m*n*(c+d \\
& *x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)] - 3*a^ \\
& 2*A*d^3*m*n*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -( \\
& (d*x^n)/c)] - 2*b^2*B*c^3*n^2*(c+d*x^n)^2*Hypergeometric2F1[1, (1+m)/n, \\
& (1+m+n)/n, -((d*x^n)/c)] + 2*a^2*A*d^3*n^2*(c+d*x^n)^2*Hypergeometri \\
& c2F1[1, (1+m)/n, (1+m+n)/n, -((d*x^n)/c)))/(2*c^3*d^3*(1+m)*n^2*(c \\
& +d*x^n)^2)
\end{aligned}$$

**Maple [F]**

time = 0.08, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^2 (A + Bx^n)}{(c + dx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(a+b*x^n)^2*(A+B*x^n)/(c+d*x^n)^3,x)
```

```
[Out] int((e*x)^m*(a+b*x^n)^2*(A+B*x^n)/(c+d*x^n)^3,x)
```

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)/(c+d*x^n)^3,x, algorithm="maxima")
```

```
[Out] (((m^2*e^m + m*(n + 2)*e^m + (n + 1)*e^m)*b^2*c^2*d - 2*(m^2*e^m - m*(n - 2)*e^m - (n - 1)*e^m)*a*b*c*d^2 + (m^2*e^m - m*(3*n - 2)*e^m + (2*n^2 - 3*n + 1)*e^m)*a^2*d^3)*A - ((m^2*e^m + m*(3*n + 2)*e^m + (2*n^2 + 3*n + 1)*e^m)*b^2*c^3 - 2*(m^2*e^m + m*(n + 2)*e^m + (n + 1)*e^m)*a*b*c^2*d + (m^2*e^m - m*(n - 2)*e^m - (n - 1)*e^m)*a^2*c*d^2)*B)*integrate(1/2*x^m/(c^2*d^4*n^2*x^n + c^3*d^3*n^2), x) + 1/2*(2*B*b^2*c^2*d^2*n^2*x*e^(m*log(x) + 2*n*log(x) + m) - ((m^2*e^m + m*(n + 2)*e^m + (n + 1)*e^m)*b^2*c^3*d - 2*(m^2*e^m - m*(n - 2)*e^m - (n - 1)*e^m)*a*b*c^2*d^2 + (m^2*e^m - m*(3*n - 2)*e^m - (3*n - 1)*e^m)*a^2*c*d^3)*A - ((m^2*e^m + m*(3*n + 2)*e^m + (2*n^2 + 3*n + 1)*e^m)*b^2*c^4 - 2*(m^2*e^m + m*(n + 2)*e^m + (n + 1)*e^m)*a*b*c^3*d + (m^2*e^m - m*(n - 2)*e^m - (n - 1)*e^m)*a^2*c^2*d^2)*B)*x*x^m - (((m^2*e^m + 2*m*(n + 1)*e^m + (2*n + 1)*e^m)*b^2*c^2*d^2 - 2*(m^2*e^m + 2*m*e^m + e^m)*a*b*c*d^3 + (m^2*e^m - 2*m*(n - 1)*e^m - (2*n - 1)*e^m)*a^2*d^4)*A - ((m^2*e^m + 2*m*(2*n + 1)*e^m + (4*n^2 + 4*n + 1)*e^m)*b^2*c^3*d - 2*(m^2*e^m + 2*m*(n + 1)*e^m + (2*n + 1)*e^m)*a*b*c^2*d^2 + (m^2*e^m + 2*m*e^m + e^m)*a^2*c*d^3)*B)*x*e^(m*log(x) + n*log(x)))/((m*n^2 + n^2)*c^2*d^5*x^(2*n) + 2*(m*n^2 + n^2)*c^3*d^4*x^n + (m*n^2 + n^2)*c^4*d^3)
```

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^2*(A+B*x^n)/(c+d*x^n)^3,x, algorithm="fricas")
```

[Out] integral((B\*b^2\*x^(3\*n) + A\*a^2 + (2\*B\*a\*b + A\*b^2)\*x^(2\*n) + (B\*a^2 + 2\*A\*a\*b)\*x^n)\*(x\*e)^m/(d^3\*x^(3\*n) + 3\*c\*d^2\*x^(2\*n) + 3\*c^2\*d\*x^n + c^3), x)

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*2\*(A+B\*x\*\*n)/(c+d\*x\*\*n)\*\*3,x)

[Out] Timed out

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^2\*(A+B\*x^n)/(c+d\*x^n)^3,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^2\*(x\*e)^m/(d\*x^n + c)^3, x)

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^2}{(c + dx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^2)/(c + d\*x^n)^3,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^2)/(c + d\*x^n)^3, x)

$$3.37 \quad \int \frac{(ex)^m (a+bx^n)(A+Bx^n)}{(c+dx^n)^3} dx$$

**Optimal.** Leaf size=228

$$\frac{(bc-ad)(ex)^{1+m}(A+Bx^n)}{2cde(c+dx^n)^2} - \frac{(ad(Ad(1+m-2n)-Bc(1+m-n))-bc(Ad(1+m)-Bc(1+m+n)))}{2c^2d^2en^2(c+dx^n)}$$

[Out]  $-1/2*(-a*d+b*c)*(e*x)^{(1+m)}*(A+B*x^n)/c/d/e/n/(c+d*x^n)^2-1/2*(a*d*(A*d*(1+m-2*n)-B*c*(1+m-n))-b*c*(A*d*(1+m)-B*c*(1+m+n))*(e*x)^{(1+m)}/c^2/d^2/e/n^2/(c+d*x^n)-1/2*(A*d*(b*c*(1+m)-a*d*(1+m-2*n))*(1+m-n)+B*c*(1+m)*(a*d*(1+m-n)-b*c*(1+m+n))*(e*x)^{(1+m)}*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^3/d^2/e/(1+m)/n^2$

**Rubi [A]**

time = 0.19, antiderivative size = 227, normalized size of antiderivative = 1.00, number of steps used = 3, number of rules used = 3, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.103$ , Rules used = {608, 468, 371}

$$\frac{(ex)^{m+1} {}_2F_1\left(1, \frac{m+1}{n}; \frac{m+1}{n}; -\frac{dx^n}{c}\right) (Ad(m-n+1)(bc(m+1)-ad(m-2n+1))+Bc(m+1)(ad(m-n+1)-bc(m+n+1)))}{2c^2d^2e(m+1)n^2} + \frac{(ex)^{m+1} (Ad(bc(m+1)-ad(m-2n+1))+Bc(ad(m-n+1)-bc(m+n+1)))}{2c^2d^2en^2(c+dx^n)} - \frac{(ex)^{m+1} (bc-ad)(A+Bx^n)}{2cde(c+dx^n)^2}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n))/(c + d\*x^n)^3,x]

[Out]  $-1/2*((b*c - a*d)*(e*x)^{(1+m)}*(A + B*x^n))/(c*d*e*n*(c + d*x^n)^2) + ((A*d*(b*c*(1+m) - a*d*(1+m-2*n)) + B*c*(a*d*(1+m-n) - b*c*(1+m+n)))*(e*x)^{(1+m)}/(2*c^2*d^2*e*n^2*(c + d*x^n)) - ((A*d*(b*c*(1+m) - a*d*(1+m-2*n))*(1+m-n) + B*c*(1+m)*(a*d*(1+m-n) - b*c*(1+m+n)))*(e*x)^{(1+m)}*Hypergeometric2F1[1, (1+m)/n, (1+m+n)/n, -(d*x^n)/c]]/(2*c^3*d^2*e*(1+m)*n^2)$

Rule 371

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 468

Int[((e\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_.)\*((c\_) + (d\_.)\*(x\_)^(n\_)), x\_Symbol] :> Simp[(-b\*c - a\*d)\*(e\*x)^(m+1)\*((a + b\*x^n)^(p+1)/(a\*b\*e\*n\*(p+1))), x] - Dist[(a\*d\*(m+1) - b\*c\*(m+n\*(p+1)+1))/(a\*b\*n\*(p+1)), Int[(e\*x)^m\*(a + b\*x^n)^(p+1), x], x] /; FreeQ[{a, b, c, d, e, m, n}, x] && NeQ[b\*c - a\*d, 0] && LtQ[p, -1] && (!IntegerQ[p + 1/2] && NeQ[p, -5/4]) || !RationalQ[m] || (IGtQ[n, 0] && ILtQ[p + 1/2, 0] && LeQ[-1,



m, (-n)\*(p + 1]]))

### Rule 608

```
Int[((g_.)*(x_))^(m_.)*((a_.) + (b_.)*(x_)^(n_))^(p_)*((c_.) + (d_.)*(x_)^(n_))^(q_.)*((e_.) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^q/(a*b*g*n*(p + 1))), x] + Dist[1/(a*b*n*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^(q - 1)*Simp[c*(b*e*n*(p + 1) + (b*e - a*f)*(m + 1)) + d*(b*e*n*(p + 1) + (b*e - a*f)*(m + n*q + 1))*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n}, x] && LtQ[p, -1] && GtQ[q, 0] && !(EqQ[q, 1] && SimplerQ[b*c - a*d, b*e - a*f])
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (a + bx^n) (A + Bx^n)}{(c + dx^n)^3} dx &= -\frac{(bc - ad)(ex)^{1+m} (A + Bx^n)}{2cdn (c + dx^n)^2} - \frac{\int \frac{(ex)^m (-A(bc(1+m) - ad(1+m-2n)) + B(ad(1+m) - bc(1+m-2n))}{(c+dx^n)^2} dx}{2cdn} \\ &= -\frac{(bc - ad)(ex)^{1+m} (A + Bx^n)}{2cdn (c + dx^n)^2} - \frac{(ad(Ad(1 + m - 2n) - Bc(1 + m - 2n))}{2c^2d} \\ &= -\frac{(bc - ad)(ex)^{1+m} (A + Bx^n)}{2cdn (c + dx^n)^2} - \frac{(ad(Ad(1 + m - 2n) - Bc(1 + m - 2n))}{2c^2d} \end{aligned}$$

**Mathematica** [B] Leaf count is larger than twice the leaf count of optimal. 1153 vs. 2(228) = 456.

time = 0.59, size = 1153, normalized size = 5.06

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)\*(A + B\*x^n))/(c + d\*x^n)^3,x]

[Out] (x\*(e\*x)^m\*(b\*B\*c^4\*(1 + m)\*n - A\*b\*c^3\*d\*(1 + m)\*n - a\*B\*c^3\*d\*(1 + m)\*n + a\*A\*c^2\*d^2\*(1 + m)\*n - b\*B\*c^3\*(1 + m)\*(c + d\*x^n) + A\*b\*c^2\*d\*(1 + m)\*(c + d\*x^n) + a\*B\*c^2\*d\*(1 + m)\*(c + d\*x^n) - a\*A\*c\*d^2\*(1 + m)\*(c + d\*x^n) - b\*B\*c^3\*m\*(1 + m)\*(c + d\*x^n) + A\*b\*c^2\*d\*m\*(1 + m)\*(c + d\*x^n) + a\*B\*c^2\*d\*m\*(1 + m)\*(c + d\*x^n) - a\*A\*c\*d^2\*m\*(1 + m)\*(c + d\*x^n) - 2\*b\*B\*c^3\*(1 + m)\*n\*(c + d\*x^n) + 2\*a\*A\*c\*d^2\*(1 + m)\*n\*(c + d\*x^n) + b\*B\*c^2\*(c + d\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] - A\*b\*c\*d\*(c + d\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] - a\*B\*c\*d\*(c + d\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] + a\*A\*d^2\*(c + d\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)

$$\begin{aligned} & /n, -((d*x^n)/c)] + 2*b*B*c^2*m*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/ \\ & n, (1 + m + n)/n, -((d*x^n)/c)] - 2*A*b*c*d*m*(c + d*x^n)^2*Hypergeometric2 \\ & F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] - 2*a*B*c*d*m*(c + d*x^n)^2*H \\ & ypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + 2*a*A*d^2*m*( \\ & c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + \\ & b*B*c^2*m^2*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, - \\ & ((d*x^n)/c)] - A*b*c*d*m^2*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 \\ & + m + n)/n, -((d*x^n)/c)] - a*B*c*d*m^2*(c + d*x^n)^2*Hypergeometric2F1[1, \\ & (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + a*A*d^2*m^2*(c + d*x^n)^2*Hyp \\ & ergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + b*B*c^2*n*(c + d*x \\ & ^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + A*b*c* \\ & d*n*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/ \\ & c)] + a*B*c*d*n*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n \\ & , -((d*x^n)/c)] - 3*a*A*d^2*n*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, \\ & (1 + m + n)/n, -((d*x^n)/c)] + b*B*c^2*m*n*(c + d*x^n)^2*Hypergeometric2F1 \\ & [1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + A*b*c*d*m*n*(c + d*x^n)^2*Hyp \\ & ergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + a*B*c*d*m*n*(c \\ & + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] - 3 \\ & *a*A*d^2*m*n*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, - \\ & ((d*x^n)/c)] + 2*a*A*d^2*n^2*(c + d*x^n)^2*Hypergeometric2F1[1, (1 + m)/n, \\ & (1 + m + n)/n, -((d*x^n)/c)))/(2*c^3*d^2*(1 + m)*n^2*(c + d*x^n)^2) \end{aligned}$$

**Maple [F]**

time = 0.07, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n) (A + Bx^n)}{(c + dx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^3,x)

[Out] int((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^3,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^3,x, algorithm="maxima")

[Out] -(((m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*b\*c\*d - (m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*a\*d^2)\*A - ((m^2\*e^m + m\*(n + 2)\*e^m + (n + 1)\*e^m)\*b\*c^2 - (m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a\*c\*d)\*B)\*integrate(1/2\*x^m/(c^2\*d^3\*n^2\*x^n + c^3\*d^2\*n^2), x) + 1/2\*(((m\*e^m - (n - 1)\*e^m)\*b\*c^2\*d - (m\*e^m - (3\*n - 1)\*e^m)\*a\*c\*d^2)\*A - ((m\*e^m + (n + 1)\*e^m)\*b\*c^3 -

$$\frac{(m e^m - (n - 1) e^m) a c^{2d} B x x^m + ((m e^m + e^m) b c d^2 - (m e^m - (2n - 1) e^m) a d^3) A - ((m e^m + (2n + 1) e^m) b c^2 d - (m e^m + e^m) a c d^2) B x e^{(m \log(x) + n \log(x))}}{(c^2 d^4 n^2 x^{(2n)} + 2 c^3 d^3 n^2 x^n + c^4 d^2 n^2)}$$
**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^3,x, algorithm="fricas")

[Out] integral((B\*b\*x^(2\*n) + A\*a + (B\*a + A\*b)\*x^n)\*(x\*e)^m/(d^3\*x^(3\*n) + 3\*c\*d^2\*x^(2\*n) + 3\*c^2\*d\*x^n + c^3), x)

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*(A+B\*x\*\*n)/(c+d\*x\*\*n)\*\*3,x)

[Out] Timed out

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)\*(A+B\*x^n)/(c+d\*x^n)^3,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)\*(x\*e)^m/(d\*x^n + c)^3, x)

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(e x)^m (A + B x^n) (a + b x^n)}{(c + d x^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n))/(c + d\*x^n)^3,x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n))/(c + d\*x^n)^3, x)

$$3.38 \quad \int \frac{(ex)^m (A+Bx^n)}{(c+dx^n)^3} dx$$

**Optimal.** Leaf size=112

$$-\frac{(Bc-Ad)(ex)^{1+m}}{2cde n (c+dx^n)^2} + \frac{(Bc(1+m)-Ad(1+m-2n))(ex)^{1+m} {}_2F_1\left(2, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{2c^3 de (1+m)n}$$

[Out]  $-1/2*(-A*d+B*c)*(e*x)^{(1+m)}/c/d/e/n/(c+d*x^n)^2+1/2*(B*c*(1+m)-A*d*(1+m-2*n))*(e*x)^{(1+m)}*hypergeom([2, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^3/d/e/(1+m)/n$

**Rubi [A]**

time = 0.04, antiderivative size = 112, normalized size of antiderivative = 1.00, number of steps used = 2, number of rules used = 2, integrand size = 22,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.091$ ,

Rules used = {468, 371}

$$\frac{(ex)^{m+1}(Bc(m+1)-Ad(m-2n+1)) {}_2F_1\left(2, \frac{m+1}{n}; \frac{m+n+1}{n}; -\frac{dx^n}{c}\right)}{2c^3 de (m+1)n} - \frac{(ex)^{m+1}(Bc-Ad)}{2cde n (c+dx^n)^2}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[\frac{(e*x)^m*(A+B*x^n)}{(c+d*x^n)^3}, x]$

[Out]  $-1/2*((B*c-A*d)*(e*x)^{(1+m)})/(c*d*e*n*(c+d*x^n)^2) + ((B*c*(1+m)-A*d*(1+m-2*n))*(e*x)^{(1+m)}*Hypergeometric2F1[2, (1+m)/n, (1+m+n)/n, -(d*x^n/c)])/(2*c^3*d*e*(1+m)*n)$

Rule 371

$\text{Int}[\frac{(c_*)*(x_*)^{(m_*)}*((a_*) + (b_*)*(x_*)^{(n_*)})^{(p_*)}}{(c*x)^{(m+1)}/(c*(m+1))} * \text{Hypergeometric2F1}[-p, (m+1)/n, (m+1)/n+1, (-b)*(x^n/a)], x] /; \text{FreeQ}\{a, b, c, m, n, p\}, x \ \&\& \ !\text{IGtQ}[p, 0] \ \&\& \ (\text{ILtQ}[p, 0] \ || \ \text{GtQ}[a, 0])$

Rule 468

$\text{Int}[\frac{(e_*)*(x_*)^{(m_*)}*((a_*) + (b_*)*(x_*)^{(n_*)})^{(p_*)}*((c_*) + (d_*)*(x_*)^{(n_*)})}{(-b*c-a*d)*(e*x)^{(m+1)}*((a+b*x^n)^{(p+1)}/(a*b*e*n*(p+1)))}, x] - \text{Dist}[(a*d*(m+1)-b*c*(m+n*(p+1)+1))/(a*b*n*(p+1)), \text{Int}[(e*x)^m*(a+b*x^n)^{(p+1)}, x], x] /; \text{FreeQ}\{a, b, c, d, e, m, n\}, x \ \&\& \ \text{NeQ}[b*c-a*d, 0] \ \&\& \ \text{LtQ}[p, -1] \ \&\& \ ((\ !\text{IntegerQ}[p+1/2] \ \&\& \ \text{NeQ}[p, -5/4]) \ || \ \ !\text{RationalQ}[m] \ || \ (\text{IGtQ}[n, 0] \ \&\& \ \text{ILtQ}[p+1/2, 0] \ \&\& \ \text{LeQ}[-1, m, (-n)*(p+1)]))$

Rubi steps

$$\int \frac{(ex)^m (A + Bx^n)}{(c + dx^n)^3} dx = -\frac{(Bc - Ad)(ex)^{1+m}}{2cdn(c + dx^n)^2} + \frac{(Bc(1+m) - Ad(1+m-2n)) \int \frac{(ex)^m}{(c+dx^n)^2} dx}{2cdn}$$

$$= -\frac{(Bc - Ad)(ex)^{1+m}}{2cdn(c + dx^n)^2} + \frac{(Bc(1+m) - Ad(1+m-2n))(ex)^{1+m} {}_2F_1\left(2, \frac{1+m}{n}; \frac{1+m}{n}\right)}{2c^3de(1+m)n}$$

**Mathematica [A]**

time = 0.18, size = 127, normalized size = 1.13

$$\frac{x(ex)^m \left( -\frac{c^2(Bc-Ad)n}{(c+dx^n)^2} + \frac{c(Bc(1+m)-Ad(1+m-2n))}{c+dx^n} - \frac{(Bc(1+m)-Ad(1+m-2n))(1+m-n) {}_2F_1\left(1, \frac{1+m}{n}; \frac{1+m+n}{n}; -\frac{dx^n}{c}\right)}{1+m} \right)}{2c^3dn^2}$$

Antiderivative was successfully verified.

**[In]** Integrate[((e\*x)^m\*(A + B\*x^n))/(c + d\*x^n)^3,x]

**[Out]** (x\*(e\*x)^m\*(-((c^2\*(B\*c - A\*d)\*n)/(c + d\*x^n)^2) + (c\*(B\*c\*(1 + m) - A\*d\*(1 + m - 2\*n)))/(c + d\*x^n) - ((B\*c\*(1 + m) - A\*d\*(1 + m - 2\*n))\*(1 + m - n)\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)]/(1 + m)))/(2\*c^3\*d\*n^2)

**Maple [F]**

time = 0.06, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(c + dx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

**[In]** int((e\*x)^m\*(A+B\*x^n)/(c+d\*x^n)^3,x)**[Out]** int((e\*x)^m\*(A+B\*x^n)/(c+d\*x^n)^3,x)**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

**[In]** integrate((e\*x)^m\*(A+B\*x^n)/(c+d\*x^n)^3,x, algorithm="maxima")

**[Out]** -((m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*B\*c - (m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*A\*d)\*integrate(1/2\*x^m/(c^2\*d^2\*n^2\*x^n + c^3\*d\*n^2), x) + 1/2\*((m\*e^m - (n - 1)\*e^m)\*B\*c^2 - (m\*e^m - (3\*n - 1)\*e^m)\*A\*c\*d)

```
*x*x^m + ((m*e^m + e^m)*B*c*d - (m*e^m - (2*n - 1)*e^m)*A*d^2)*x*e^(m*log(x)
) + n*log(x)))/(c^2*d^3*n^2*x^(2*n) + 2*c^3*d^2*n^2*x^n + c^4*d*n^2)
```

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)/(c+d*x^n)^3,x, algorithm="fricas")
```

```
[Out] integral((B*x^n + A)*(x*e)^m/(d^3*x^(3*n) + 3*c*d^2*x^(2*n) + 3*c^2*d*x^n +
c^3), x)
```

**Sympy [F(-1)]** Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(A+B*x**n)/(c+d*x**n)**3,x)
```

```
[Out] Timed out
```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)/(c+d*x^n)^3,x, algorithm="giac")
```

```
[Out] integrate((B*x^n + A)*(x*e)^m/(d*x^n + c)^3, x)
```

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(e x)^m (A + B x^n)}{(c + d x^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(((e*x)^m*(A + B*x^n))/(c + d*x^n)^3,x)
```

```
[Out] int(((e*x)^m*(A + B*x^n))/(c + d*x^n)^3, x)
```

$$3.39 \quad \int \frac{(ex)^m (A+Bx^n)}{(a+bx^n)(c+dx^n)^3} dx$$

**Optimal.** Leaf size=366

$$\frac{(Bc - Ad)(ex)^{1+m}}{2c(bc - ad)en(c + dx^n)^2} + \frac{(bc(Ad(1 + m - 4n) - Bc(1 + m - 2n)) + ad(Bc(1 + m) - Ad(1 + m - 2n)))}{2c^2(bc - ad)^2en^2(c + dx^n)}$$

[Out]  $1/2*(-A*d+B*c)*(e*x)^(1+m)/c/(-a*d+b*c)/e/n/(c+d*x^n)^2+1/2*(b*c*(A*d*(1+m-4*n)-B*c*(1+m-2*n))+a*d*(B*c*(1+m)-A*d*(1+m-2*n))*(e*x)^(1+m)/c^2/(-a*d+b*c)^2/e/n^2/(c+d*x^n)+b^2*(A*b-B*a)*(e*x)^(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/a/(-a*d+b*c)^3/e/(1+m)-1/2*(b^2*c^2*(A*d*(1+m-3*n)-B*c*(1+m-n))*(1+m-2*n)-a^2*d^2*(B*c*(1+m)-A*d*(1+m-2*n))*(1+m-n)+2*a*b*c*d*(B*c*(1+m)*(1+m-2*n)-A*d*(1+m^2+m*(2-4*n)-4*n+3*n^2)))*(e*x)^(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^3/(-a*d+b*c)^3/e/(1+m)/n^2$

**Rubi** [A]

time = 0.80, antiderivative size = 366, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {609, 611, 371}

$$\frac{(ex)^{m+1} F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{b^2 x^{2n}}{a^2 (bc-ad)^2}\right) - (ex)^{m+1} F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{b^2 x^{2n}}{a^2 (bc-ad)^2}\right) - (ex)^{m+1} F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{b^2 x^{2n}}{a^2 (bc-ad)^2}\right)}{2c^2 (bc-ad)^2 en^2 (c+dx^n)^2} + \frac{(ex)^{m+1} F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{b^2 x^{2n}}{a^2 (bc-ad)^2}\right) - (ex)^{m+1} F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{b^2 x^{2n}}{a^2 (bc-ad)^2}\right) - (ex)^{m+1} F_1\left(1, \frac{m+1}{n}, \frac{m+1}{n}, -\frac{b^2 x^{2n}}{a^2 (bc-ad)^2}\right)}{2c^2 (bc-ad)^2 en^2 (c+dx^n)^2}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)\*(c + d\*x^n)^3), x]

[Out]  $((B*c - A*d)*(e*x)^(1 + m))/(2*c*(b*c - a*d)*e*n*(c + d*x^n)^2) + ((b*c*(A*d*(1 + m - 4*n) - B*c*(1 + m - 2*n)) + a*d*(B*c*(1 + m) - A*d*(1 + m - 2*n)))*(e*x)^(1 + m))/(2*c^2*(b*c - a*d)^2*e*n^2*(c + d*x^n)) + (b^2*(A*b - a*B)*(e*x)^(1 + m)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b*x^n)/a)])/((a*(b*c - a*d)^3*e*(1 + m)) - ((b^2*c^2*(A*d*(1 + m - 3*n) - B*c*(1 + m - n))*(1 + m - 2*n) - a^2*d^2*(B*c*(1 + m) - A*d*(1 + m - 2*n))*(1 + m - n) + 2*a*b*c*d*(B*c*(1 + m)*(1 + m - 2*n) - A*d*(1 + m^2 + m*(2 - 4*n) - 4*n + 3*n^2)))*(e*x)^(1 + m)*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)])/(2*c^3*(b*c - a*d)^3*e*(1 + m)*n^2)$

Rule 371

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p \* ((c\*x)^(m + 1)/(c\*(m + 1)))\*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

Rule 609

Int[((g\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_))^(q\_)\*((e\_) + (f\_)\*(x\_)^(n\_)), x\_Symbol] := Simp[(-b\*e - a\*f)\*(g\*x)^(m

```
+ 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^(q + 1)/(a*g*n*(b*c - a*d)*(p + 1)))
, x] + Dist[1/(a*n*(b*c - a*d)*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(
+ d*x^n)^q* Simp[c*(b*e - a*f)*(m + 1) + e*n*(b*c - a*d)*(p + 1) + d*(b*e -
a*f)*(m + n*(p + q + 2) + 1)*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g
, m, n, q}, x] && LtQ[p, -1]
```

Rule 611

```
Int[(((g_)*(x_))^(m_)*((a_) + (b_)*(x_)^(n_))^(p_)*((e_) + (f_)*(x_)^(n
_)))/((c_) + (d_)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a
+ b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g,
m, n, p}, x]
```

Rubi steps

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)(c + dx^n)^3} dx = \frac{(Bc - Ad)(ex)^{1+m}}{2c(bc - ad)en(c + dx^n)^2} + \frac{\int \frac{(ex)^m(-aBc(1+m)+aAd(1+m-2n)+2Abcn-b(Bc-Ad)(1+m-2n)}{(a+bx^n)(c+dx^n)^2} dx}{2c(bc - ad)n}$$

$$= \frac{(Bc - Ad)(ex)^{1+m}}{2c(bc - ad)en(c + dx^n)^2} + \frac{(bc(Ad(1 + m - 4n) - Bc(1 + m - 2n)) + ad(Bc(1 + m - 2n) - Ad(1 + m - 4n)))}{2c^2(bc - ad)^2en^2(c + dx^n)}$$

$$= \frac{(Bc - Ad)(ex)^{1+m}}{2c(bc - ad)en(c + dx^n)^2} + \frac{(bc(Ad(1 + m - 4n) - Bc(1 + m - 2n)) + ad(Bc(1 + m - 2n) - Ad(1 + m - 4n)))}{2c^2(bc - ad)^2en^2(c + dx^n)}$$

$$= \frac{(Bc - Ad)(ex)^{1+m}}{2c(bc - ad)en(c + dx^n)^2} + \frac{(bc(Ad(1 + m - 4n) - Bc(1 + m - 2n)) + ad(Bc(1 + m - 2n) - Ad(1 + m - 4n)))}{2c^2(bc - ad)^2en^2(c + dx^n)}$$

$$= \frac{(Bc - Ad)(ex)^{1+m}}{2c(bc - ad)en(c + dx^n)^2} + \frac{(bc(Ad(1 + m - 4n) - Bc(1 + m - 2n)) + ad(Bc(1 + m - 2n) - Ad(1 + m - 4n)))}{2c^2(bc - ad)^2en^2(c + dx^n)}$$

Mathematica [A]

time = 1.25, size = 357, normalized size = 0.98

```
Integrate[(e*x)^m*(A + B*x^n)/((a + b*x^n)*(c + d*x^n)^3), x]
```

Antiderivative was successfully verified.

```
[In] Integrate[((e*x)^m*(A + B*x^n))/((a + b*x^n)*(c + d*x^n)^3), x]
```

```
[Out] -1/2*(x*(e*x)^m*(-(a*c*(b*c - a*d)*(1 + m)*(b*c*(-(A*d*(c*(1 + m - 5*n) + d
*(1 + m - 4*n)*x^n)) + B*c*(c*(1 + m - 3*n) + d*(1 + m - 2*n)*x^n)) + a*d*(
-(B*c*(c*(1 + m - n) + d*(1 + m)*x^n)) + A*d*(c*(1 + m - 3*n) + d*(1 + m -
2*n)*x^n)))) + 2*b^2*(A*b - a*B)*c^3*n^2*(c + d*x^n)^2*Hypergeometric2F1[1,
(1 + m)/n, (1 + m + n)/n, -(b*x^n)/a] + a*(b^2*c^2*(-(A*d*(1 + m - 3*n))
```



+ B\*c\*(1 + m - n))\*(1 + m - 2\*n) + a^2\*d^2\*(B\*c\*(1 + m) - A\*d\*(1 + m - 2\*n))\*(1 + m - n) + 2\*a\*b\*c\*d\*(-(B\*c\*(1 + m)\*(1 + m - 2\*n)) + A\*d\*(1 + m^2 + m\*(2 - 4\*n) - 4\*n + 3\*n^2)))\*(c + d\*x^n)^2\*Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -(d\*x^n)/c]]/(a\*c^3\*(-(b\*c) + a\*d)^3\*(1 + m)\*n^2\*(c + d\*x^n)^2)

**Maple [F]**

time = 0.11, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)(c + dx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n)^3,x)

[Out] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n)^3,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)/(c+d\*x^n)^3,x, algorithm="maxima")

[Out] (((m^2\*e^m - m\*(5\*n - 2)\*e^m + (6\*n^2 - 5\*n + 1)\*e^m)\*b^2\*c^2\*d - 2\*(m^2\*e^m - 2\*m\*(2\*n - 1)\*e^m + (3\*n^2 - 4\*n + 1)\*e^m)\*a\*b\*c\*d^2 + (m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*a^2\*d^3)\*A - ((m^2\*e^m - m\*(3\*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*b^2\*c^3 - 2\*(m^2\*e^m - 2\*m\*(n - 1)\*e^m - (2\*n - 1)\*e^m)\*a\*b\*c^2\*d + (m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a^2\*c\*d^2)\*B)\*integrate(-1/2\*x^m/(b^3\*c^6\*n^2 - 3\*a\*b^2\*c^5\*d\*n^2 + 3\*a^2\*b\*c^4\*d^2\*n^2 - a^3\*c^3\*d^3\*n^2 + (b^3\*c^5\*d\*n^2 - 3\*a\*b^2\*c^4\*d^2\*n^2 + 3\*a^2\*b\*c^3\*d^3\*n^2 - a^3\*c^2\*d^4\*n^2)\*x^n), x) + (B\*a\*b^2\*e^m - A\*b^3\*e^m)\*integrate(-x^m/(a\*b^3\*c^3 - 3\*a^2\*b^2\*c^2\*d + 3\*a^3\*b\*c\*d^2 - a^4\*d^3 + (b^4\*c^3 - 3\*a\*b^3\*c^2\*d + 3\*a^2\*b^2\*c\*d^2 - a^3\*b\*d^3)\*x^n), x) + 1/2\*(((m\*e^m - (5\*n - 1)\*e^m)\*b\*c^2\*d - (m\*e^m - (3\*n - 1)\*e^m)\*a\*c\*d^2)\*A - ((m\*e^m - (3\*n - 1)\*e^m)\*b\*c^3 - (m\*e^m - (n - 1)\*e^m)\*a\*c^2\*d)\*B)\*x\*x^m + (((m\*e^m - (4\*n - 1)\*e^m)\*b\*c\*d^2 - (m\*e^m - (2\*n - 1)\*e^m)\*a\*d^3)\*A - ((m\*e^m - (2\*n - 1)\*e^m)\*b\*c^2\*d - (m\*e^m + e^m)\*a\*c\*d^2)\*B)\*x\*e^(m\*log(x) + n\*log(x))/(b^2\*c^6\*n^2 - 2\*a\*b\*c^5\*d\*n^2 + a^2\*c^4\*d^2\*n^2 + (b^2\*c^4\*d^2\*n^2 - 2\*a\*b\*c^3\*d^3\*n^2 + a^2\*c^2\*d^4\*n^2)\*x^(2\*n) + 2\*(b^2\*c^5\*d\*n^2 - 2\*a\*b\*c^4\*d^2\*n^2 + a^2\*c^3\*d^3\*n^2)\*x^n)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)/(a+b*x^n)/(c+d*x^n)^3,x, algorithm="fricas")
```

```
[Out] integral((B*x^n + A)*(x*e)^m/(b*d^3*x^(4*n) + a*c^3 + (3*b*c*d^2 + a*d^3)*x^(3*n) + 3*(b*c^2*d + a*c*d^2)*x^(2*n) + (b*c^3 + 3*a*c^2*d)*x^n), x)
```

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(A+B*x**n)/(a+b*x**n)/(c+d*x**n)**3,x)
```

```
[Out] Exception raised: HeuristicGCDFailed >> no luck
```

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(A+B*x^n)/(a+b*x^n)/(c+d*x^n)^3,x, algorithm="giac")
```

```
[Out] integrate((B*x^n + A)*(x*e)^m/((b*x^n + a)*(d*x^n + c)^3), x)
```

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(e x)^m (A + B x^n)}{(a + b x^n) (c + d x^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(((e*x)^m*(A + B*x^n))/((a + b*x^n)*(c + d*x^n)^3),x)
```

```
[Out] int(((e*x)^m*(A + B*x^n))/((a + b*x^n)*(c + d*x^n)^3), x)
```

$$3.40 \quad \int \frac{(ex)^m (A+Bx^n)}{(a+bx^n)^2 (c+dx^n)^3} dx$$

**Optimal.** Leaf size=482

$$\frac{d(2Abc - 3aBc + aAd)(ex)^{1+m}}{2ac(bc - ad)^2 en (c + dx^n)^2} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)^2} - \frac{d(a^2d(Bc(1 + m) - Ad(1 + m - 2n))}{2ac^2(b$$

```
[Out] 1/2*d*(A*a*d+2*A*b*c-3*B*a*c)*(e*x)^(1+m)/a/c/(-a*d+b*c)^2/e/n/(c+d*x^n)^2+
(A*b-B*a)*(e*x)^(1+m)/a/(-a*d+b*c)/e/n/(a+b*x^n)/(c+d*x^n)^2-1/2*d*(a^2*d*(
B*c*(1+m)-A*d*(1+m-2*n))-a*b*c*(-A*d+B*c)*(1+m-6*n)-2*A*b^2*c^2*n)*(e*x)^(1
+m)/a/c^2/(-a*d+b*c)^3/e/n^2/(c+d*x^n)+b^2*(a*B*(b*c*(1+m)-a*d*(1+m-3*n))+A
*b*(a*d*(1+m-4*n)-b*c*(1+m-n)))*(e*x)^(1+m)*hypergeom([1, (1+m)/n], [(1+m+n)
/n], -b*x^n/a)/a^2/(-a*d+b*c)^4/e/(1+m)/n+1/2*d*(b^2*c^2*(A*d*(1+m-4*n)-B*c*
(1+m-2*n))*(1+m-3*n)-a^2*d^2*(B*c*(1+m)-A*d*(1+m-2*n))*(1+m-n)+2*a*b*c*d*(B
*c*(1+m)*(1+m-3*n)-A*d*(1+m^2+m*(2-5*n)-5*n+4*n^2)))*(e*x)^(1+m)*hypergeom(
[1, (1+m)/n], [(1+m+n)/n], -d*x^n/c)/c^3/(-a*d+b*c)^4/e/(1+m)/n^2
```

**Rubi [A]**

time = 1.36, antiderivative size = 482, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {609, 611, 371}

Antiderivative was successfully verified.

```
[In] Int[((e*x)^m*(A + B*x^n))/((a + b*x^n)^2*(c + d*x^n)^3), x]
```

```
[Out] (d*(2*A*b*c - 3*a*B*c + a*A*d)*(e*x)^(1 + m))/(2*a*c*(b*c - a*d)^2*e*n*(c +
d*x^n)^2) + ((A*b - a*B)*(e*x)^(1 + m))/(a*(b*c - a*d)*e*n*(a + b*x^n)*(c
+ d*x^n)^2) - (d*(a^2*d*(B*c*(1 + m) - A*d*(1 + m - 2*n)) - a*b*c*(B*c - A*
d)*(1 + m - 6*n) - 2*A*b^2*c^2*n)*(e*x)^(1 + m))/(2*a*c^2*(b*c - a*d)^3*e*n
^2*(c + d*x^n)) + (b^2*(a*B*(b*c*(1 + m) - a*d*(1 + m - 3*n)) + A*b*(a*d*(1
+ m - 4*n) - b*c*(1 + m - n)))*(e*x)^(1 + m)*Hypergeometric2F1[1, (1 + m)/
n, (1 + m + n)/n, -((b*x^n)/a)])/a^2*(b*c - a*d)^4*e*(1 + m)*n) + (d*(b^2*c
^2*(A*d*(1 + m - 4*n) - B*c*(1 + m - 2*n))*(1 + m - 3*n) - a^2*d^2*(B*c*(1
+ m) - A*d*(1 + m - 2*n))*(1 + m - n) + 2*a*b*c*d*(B*c*(1 + m)*(1 + m - 3*
n) - A*d*(1 + m^2 + m*(2 - 5*n) - 5*n + 4*n^2)))*(e*x)^(1 + m)*Hypergeometr
ic2F1[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)])/2*c^3*(b*c - a*d)^4*e*(1
+ m)*n^2)
```

**Rule 371**

```
Int[((c_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_), x_Symbol] := Simp[a^p
*((c*x)^(m + 1)/(c*(m + 1)))*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1
, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGTQ[p, 0] && (ILt
```

$Q[p, 0] \parallel GtQ[a, 0]$

### Rule 609

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_))^(q_)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-b*e - a*f)*(g*x)^(m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^(q + 1)/(a*g*n*(b*c - a*d)*(p + 1))], x] + Dist[1/(a*n*(b*c - a*d)*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^q*Simp[c*(b*e - a*f)*(m + 1) + e*n*(b*c - a*d)*(p + 1) + d*(b*e - a*f)*(m + n*(p + q + 2) + 1)*x^n, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, q}, x] && LtQ[p, -1]
```

### Rule 611

```
Int[(((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((e_) + (f_.)*(x_)^(n_)))/((c_) + (d_.)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x]
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)^3} dx &= \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)^2} - \frac{\int \frac{(ex)^m (-aBc(1+m) + Abc(1+m-n) + aAdn + (Ab - aB)(c + dx^n))}{(a + bx^n)(c + dx^n)^3} dx}{a(bc - ad)n} \\ &= \frac{d(2Abc - 3aBc + aAd)(ex)^{1+m}}{2ac(bc - ad)^2 en (c + dx^n)^2} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)^2} - \frac{\int \frac{(ex)^m}{(a + bx^n)(c + dx^n)^3} dx}{a(bc - ad)n} \\ &= \frac{d(2Abc - 3aBc + aAd)(ex)^{1+m}}{2ac(bc - ad)^2 en (c + dx^n)^2} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)^2} - \frac{d(a^2 d)}{a(bc - ad)n} \\ &= \frac{d(2Abc - 3aBc + aAd)(ex)^{1+m}}{2ac(bc - ad)^2 en (c + dx^n)^2} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)^2} - \frac{d(a^2 d)}{a(bc - ad)n} \\ &= \frac{d(2Abc - 3aBc + aAd)(ex)^{1+m}}{2ac(bc - ad)^2 en (c + dx^n)^2} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)^2} - \frac{d(a^2 d)}{a(bc - ad)n} \\ &= \frac{d(2Abc - 3aBc + aAd)(ex)^{1+m}}{2ac(bc - ad)^2 en (c + dx^n)^2} + \frac{(Ab - aB)(ex)^{1+m}}{a(bc - ad)en (a + bx^n) (c + dx^n)^2} - \frac{d(a^2 d)}{a(bc - ad)n} \end{aligned}$$

**Mathematica** [B] Leaf count is larger than twice the leaf count of optimal. 2178 vs. 2(482) = 964.

time = 1.85, size = 2178, normalized size = 4.52

Result too large to show

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)^3),x]

[Out]  $(x*(e*x)^m*(-(a^2*c^2*d*(b*c - a*d)^2*(B*c - A*d)*(1 + m)*n*(a + b*x^n)) + a^2*c*d*(-(b*c) + a*d)*(1 + m)*(b*c*(A*d*(1 + m - 6*n) - B*c*(1 + m - 4*n)) + a*d*(B*c*(1 + m) - A*d*(1 + m - 2*n)))*(a + b*x^n)*(c + d*x^n) + 2*a*b^2*(-(A*b) + a*B)*c^3*(-(b*c) + a*d)*(1 + m)*n*(c + d*x^n)^2 + 2*b^2*c^3*(a*B*(b*c*(1 + m) - a*d*(1 + m - 3*n)) + A*b*(a*d*(1 + m - 4*n) - b*c*(1 + m - n)))*n*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((b\*x^n)/a)] -  $a^2*b^2*B*c^3*d*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $a^2*A*b^2*c^2*d^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $2*a^3*b*B*c^2*d^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $2*a^3*A*b*c*d^3*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $a^4*B*c*d^3*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $a^4*A*d^4*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $2*a^2*b^2*B*c^3*d*m*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $2*a^2*A*b^2*c^2*d^2*m*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $4*a^3*b*B*c^2*d^2*m*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $4*a^3*A*b*c*d^3*m*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $2*a^4*B*c*d^3*m*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $2*a^4*A*d^4*m*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $a^2*b^2*B*c^3*d*m^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $a^2*A*b^2*c^2*d^2*m^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $2*a^3*b*B*c^2*d^2*m^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $2*a^3*A*b*c*d^3*m^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $a^4*B*c*d^3*m^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $a^4*A*d^4*m^2*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $5*a^2*b^2*B*c^3*d*n*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $7*a^2*A*b^2*c^2*d^2*n*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $6*a^3*b*B*c^2*d^2*n*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $10*a^3*A*b*c*d^3*n*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $a^4*B*c*d^3*n*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] -  $3*a^4*A*d^4*n*(a + b*x^n)*(c + d*x^n)^2*$ Hypergeometric2F1[1, (1 + m)/n, (1 + m + n)/n, -((d\*x^n)/c)] +  $5*a^2*b^2*B*c^3*d*m*n*(a + b*x^n)*(c + d*x^n)$

$$\begin{aligned} &^2\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] - 7*a^2*A*b \\ &^2*c^2*d^2*m*n*(a + b*x^n)*(c + d*x^n)^2\text{Hypergeometric2F1}[1, (1 + m)/n, (1 \\ &+ m + n)/n, -((d*x^n)/c)] - 6*a^3*b*B*c^2*d^2*m*n*(a + b*x^n)*(c + d*x^n)^ \\ &2\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + 10*a^3*A*b \\ &*c*d^3*m*n*(a + b*x^n)*(c + d*x^n)^2\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m \\ &+ n)/n, -((d*x^n)/c)] + a^4*B*c*d^3*m*n*(a + b*x^n)*(c + d*x^n)^2\text{Hypergeo} \\ &\text{metric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] - 3*a^4*A*d^4*m*n*(a + \\ &b*x^n)*(c + d*x^n)^2\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d*x \\ &^n)/c)] - 6*a^2*b^2*B*c^3*d*n^2*(a + b*x^n)*(c + d*x^n)^2\text{Hypergeometric2F1} \\ &[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + 12*a^2*A*b^2*c^2*d^2*n^2*(a + \\ &b*x^n)*(c + d*x^n)^2\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d*x \\ &^n)/c)] - 8*a^3*A*b*c*d^3*n^2*(a + b*x^n)*(c + d*x^n)^2\text{Hypergeometric2F1}[1 \\ &, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)] + 2*a^4*A*d^4*n^2*(a + b*x^n)*(c \\ &+ d*x^n)^2\text{Hypergeometric2F1}[1, (1 + m)/n, (1 + m + n)/n, -((d*x^n)/c)))/( \\ &2*a^2*c^3*(b*c - a*d)^4*(1 + m)*n^2*(a + b*x^n)*(c + d*x^n)^2 \end{aligned}$$

**Maple [F]**

time = 0.12, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^3,x)

[Out] int((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^3,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^3,x, algorithm="maxima")

[Out] (((m^2\*e^m - m\*(7\*n - 2)\*e^m + (12\*n^2 - 7\*n + 1)\*e^m)\*b^2\*c^2\*d^2 - 2\*(m^2 \*e^m - m\*(5\*n - 2)\*e^m + (4\*n^2 - 5\*n + 1)\*e^m)\*a\*b\*c\*d^3 + (m^2\*e^m - m\*(3 \*n - 2)\*e^m + (2\*n^2 - 3\*n + 1)\*e^m)\*a^2\*d^4)\*A - ((m^2\*e^m - m\*(5\*n - 2)\*e ^m + (6\*n^2 - 5\*n + 1)\*e^m)\*b^2\*c^3\*d - 2\*(m^2\*e^m - m\*(3\*n - 2)\*e^m - (3\*n - 1)\*e^m)\*a\*b\*c^2\*d^2 + (m^2\*e^m - m\*(n - 2)\*e^m - (n - 1)\*e^m)\*a^2\*c\*d^3) \*B)\*integrate(1/2\*x^m/(b^4\*c^7\*n^2 - 4\*a\*b^3\*c^6\*d\*n^2 + 6\*a^2\*b^2\*c^5\*d^2\*n ^2 - 4\*a^3\*b\*c^4\*d^3\*n^2 + a^4\*c^3\*d^4\*n^2 + (b^4\*c^6\*d\*n^2 - 4\*a\*b^3\*c^5\*d ^2\*n^2 + 6\*a^2\*b^2\*c^4\*d^3\*n^2 - 4\*a^3\*b\*c^3\*d^4\*n^2 + a^4\*c^2\*d^5\*n^2)\*x^ n), x) - (((m\*e^m - (n - 1)\*e^m)\*b^4\*c - (m\*e^m - (4\*n - 1)\*e^m)\*a\*b^3\*d)\*A - ((m\*e^m + e^m)\*a\*b^3\*c - (m\*e^m - (3\*n - 1)\*e^m)\*a^2\*b^2\*d)\*B)\*integrate (x^m/(a^2\*b^4\*c^4\*n - 4\*a^3\*b^3\*c^3\*d\*n + 6\*a^4\*b^2\*c^2\*d^2\*n - 4\*a^5\*b\*c\*d

$$\begin{aligned} & ^3n + a^6d^4n + (a^5b^5c^4n - 4a^2b^4c^3d^3n + 6a^3b^3c^2d^2n - \\ & 4a^4b^2c^3d^3n + a^5b^1d^4n)x^n, x) + 1/2(((2b^3c^4ne^m - (me^m - \\ & (7n - 1)e^m)a^2b^2c^2d^2 + (me^m - (3n - 1)e^m)a^3c^3d^3)*A - ( \\ & 2a^2b^2c^4ne^m - (me^m - (5n - 1)e^m)a^2b^2c^3d + (me^m - (n - 1)e^m) \\ & a^3c^2d^2)*B)*x*x^m + ((2b^3c^2d^2ne^m - (me^m - (6n - 1)e^m) \\ & )a^2b^2c^3d + (me^m - (2n - 1)e^m)a^2b^2d^4)*A + ((me^m - (6n - 1)e^m) \\ & a^2b^2c^2d^2 - (me^m + e^m)a^2b^2c^3d^3)*B)*x*e^{(m\log(x) + 2n\log(x))} \\ & + ((4b^3c^3d^3ne^m + 3a^2b^2c^3d^3ne^m - (me^m - (7n - 1)e^m)a \\ & a^2b^2c^2d^2 + (me^m - (2n - 1)e^m)a^3d^4)*A - (3a^2b^2c^2d^2ne^m \\ & - (me^m - (9n - 1)e^m)a^2b^2c^3d + (me^m + e^m)a^3c^3d^3)*B)*x*e^{(m\log(x) + n\log(x))} \\ & )/(a^2b^3c^7n^2 - 3a^3b^2c^6d^3n^2 + 3a^4b^1c^5d^2n^2 - a^5c^4d^3n^2 + (a^2b^4c^5d^2n^2 - 3a^2b^3c^4d^3n^2 + 3a^3b^2c^3d^4n^2 - a^4b^1c^2d^5n^2) \\ & )x^{(3n)} + (2a^2b^4c^6d^3n^2 - 5a^2b^3c^5d^2n^2 + 3a^3b^2c^4d^3n^2 + a^4b^1c^3d^4n^2 - a^5c^2d^5n^2) \\ & )x^{(2n)} + (a^2b^4c^7n^2 - a^2b^3c^6d^3n^2 - 3a^3b^2c^5d^2n^2 + 5a^4b^1c^4d^3n^2 - 2a^5c^3d^4n^2)x^n) \end{aligned}$$

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^3,x, algorithm="fricas")

[Out] integral((B\*x^n + A)\*(x\*e)^m/(b^2\*d^3\*x^(5\*n) + a^2\*c^3 + (3\*b^2\*c\*d^2 + 2\*a\*b\*d^3)\*x^(4\*n) + (3\*b^2\*c^2\*d + 6\*a\*b\*c\*d^2 + a^2\*d^3)\*x^(3\*n) + (b^2\*c^3 + 6\*a\*b\*c^2\*d + 3\*a^2\*c\*d^2)\*x^(2\*n) + (2\*a\*b\*c^3 + 3\*a^2\*c^2\*d)\*x^n), x)

**Sympy** [F(-1)] Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(A+B\*x\*\*n)/(a+b\*x\*\*n)\*\*2/(c+d\*x\*\*n)\*\*3,x)

[Out] Timed out

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(A+B\*x^n)/(a+b\*x^n)^2/(c+d\*x^n)^3,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(x\*e)^m/((b\*x^n + a)^2\*(d\*x^n + c)^3), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n)}{(a + bx^n)^2 (c + dx^n)^3} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)^3), x)

[Out] int(((e\*x)^m\*(A + B\*x^n))/((a + b\*x^n)^2\*(c + d\*x^n)^3), x)



### 3.41 $\int (ex)^m (a + bx^n)^p (A + Bx^n) (c + dx^n)^q dx$

**Optimal.** Leaf size=211

$$\frac{A(ex)^{1+m} (a + bx^n)^p \left(1 + \frac{bx^n}{a}\right)^{-p} (c + dx^n)^q \left(1 + \frac{dx^n}{c}\right)^{-q} F_1\left(\frac{1+m}{n}; -p, -q; \frac{1+m+n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right)}{e(1+m)} + \frac{Bx^{1+n}(ex)^n}{e(1+m)}$$

[Out]  $A*(e*x)^{(1+m)}*(a+b*x^n)^p*(c+d*x^n)^q*AppellF1((1+m)/n, -p, -q, (1+m+n)/n, -b*x^n/a, -d*x^n/c)/e/(1+m)/((1+b*x^n/a)^p)/((1+d*x^n/c)^q)+B*x^{(1+n)}*(e*x)^m*(a+b*x^n)^p*(c+d*x^n)^q*AppellF1((1+m+n)/n, -p, -q, (1+m+2*n)/n, -b*x^n/a, -d*x^n/c)/(1+m+n)/((1+b*x^n/a)^p)/((1+d*x^n/c)^q)$

**Rubi** [A]

time = 0.16, antiderivative size = 211, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 3, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.097$ , Rules used = {612, 525, 524}

$$\frac{A(ex)^{m+1} (a + bx^n)^p \left(\frac{bx^n}{a} + 1\right)^{-p} (c + dx^n)^q \left(\frac{dx^n}{c} + 1\right)^{-q} F_1\left(\frac{m+1}{n}; -p, -q; \frac{m+1+n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right)}{e(m+1)} + \frac{Bx^{n+1}(ex)^m (a + bx^n)^p \left(\frac{bx^n}{a} + 1\right)^{-p} (c + dx^n)^q \left(\frac{dx^n}{c} + 1\right)^{-q} F_1\left(\frac{m+n+1}{n}; -p, -q; \frac{m+n+1+n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right)}{m+n+1}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(a + b*x^n)^p*(A + B*x^n)*(c + d*x^n)^q, x]$

[Out]  $(A*(e*x)^{(1+m)}*(a + b*x^n)^p*(c + d*x^n)^q*AppellF1[(1+m)/n, -p, -q, (1+m+n)/n, -(b*x^n)/a, -(d*x^n)/c])/(e*(1+m)*(1 + (b*x^n)/a)^p*(1 + (d*x^n)/c)^q) + (B*x^{(1+n)}*(e*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*AppellF1[(1+m+n)/n, -p, -q, (1+m+2*n)/n, -(b*x^n)/a, -(d*x^n)/c])/(1+m+n)*(1 + (b*x^n)/a)^p*(1 + (d*x^n)/c)^q$

Rule 524

$\text{Int}[(e_*)*(x_*)^{(m_*)}*((a_*) + (b_*)*(x_*)^{(n_*)})^{(p_*)}*((c_*) + (d_*)*(x_*)^{(n_*)})^{(q_*)}, x\_Symbol] :> \text{Simp}[a^p*c^q*((e*x)^{(m+1)}/(e*(m+1)))*AppellF1[(m+1)/n, -p, -q, 1 + (m+1)/n, (b)*(x^n/a), (d)*(x^n/c)], x] /; \text{FreeQ}\{a, b, c, d, e, m, n, p, q\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{NeQ}[m, -1] \ \&\& \ \text{NeQ}[m, n - 1] \ \&\& \ (\text{IntegerQ}[p] \ || \ \text{GtQ}[a, 0]) \ \&\& \ (\text{IntegerQ}[q] \ || \ \text{GtQ}[c, 0])$

Rule 525

$\text{Int}[(e_*)*(x_*)^{(m_*)}*((a_*) + (b_*)*(x_*)^{(n_*)})^{(p_*)}*((c_*) + (d_*)*(x_*)^{(n_*)})^{(q_*)}, x\_Symbol] :> \text{Dist}[a^p*\text{IntPart}[p]*((a + b*x^n)^{\text{FracPart}[p]}/(1 + b*(x^n/a))^{\text{FracPart}[p]}), \text{Int}[(e*x)^m*(1 + b*(x^n/a))^p*(c + d*x^n)^q, x], x] /; \text{FreeQ}\{a, b, c, d, e, m, n, p, q\}, x \ \&\& \ \text{NeQ}[b*c - a*d, 0] \ \&\& \ \text{NeQ}[m, -1] \ \&\& \ \text{NeQ}[m, n - 1] \ \&\& \ !(\text{IntegerQ}[p] \ || \ \text{GtQ}[a, 0])$

Rule 612

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_))^(q_)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Dist[e, Int[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^q, x], x] + Dist[f*((g*x)^m/x^m), Int[x^(m + n)*(a + b*x^n)^p*(c + d*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p, q}, x]
```

Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^p (A + Bx^n) (c + dx^n)^q dx &= A \int (ex)^m (a + bx^n)^p (c + dx^n)^q dx + (Bx^{-m}(ex)^m) \int x^{m+n} (a + bx^n)^p (c + dx^n)^q dx \\ &= \left( A(a + bx^n)^p \left( 1 + \frac{bx^n}{a} \right)^{-p} \right) \int (ex)^m \left( 1 + \frac{bx^n}{a} \right)^p (c + dx^n)^q dx \\ &= \left( A(a + bx^n)^p \left( 1 + \frac{bx^n}{a} \right)^{-p} (c + dx^n)^q \left( 1 + \frac{dx^n}{c} \right)^{-q} \right) \int (ex)^m dx \\ &= \frac{A(ex)^{1+m} (a + bx^n)^p \left( 1 + \frac{bx^n}{a} \right)^{-p} (c + dx^n)^q \left( 1 + \frac{dx^n}{c} \right)^{-q} F_1\left( \frac{1+m}{n} \right)}{e(1+m)} \end{aligned}$$

**Mathematica [A]**

time = 0.31, size = 162, normalized size = 0.77

$$\frac{x(ex)^m (a + bx^n)^p \left( 1 + \frac{bx^n}{a} \right)^{-p} (c + dx^n)^q \left( 1 + \frac{dx^n}{c} \right)^{-q} \left( A(1+m+n) F_1\left( \frac{1+m}{n}; -p, -q; \frac{1+m+n}{n}, -\frac{bx^n}{a}, -\frac{dx^n}{c} \right) + B(1+m)x^n F_1\left( \frac{1+m+n}{n}; -p, -q; \frac{1+m+2n}{n}, -\frac{bx^n}{a}, -\frac{dx^n}{c} \right) \right)}{(1+m)(1+m+n)}$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*(a + b*x^n)^p*(A + B*x^n)*(c + d*x^n)^q,x]
```

```
[Out] (x*(e*x)^m*(a + b*x^n)^p*(c + d*x^n)^q*(A*(1 + m + n)*AppellF1[(1 + m)/n, -p, -q, (1 + m + n)/n, -((b*x^n)/a), -((d*x^n)/c)] + B*(1 + m)*x^n*AppellF1[(1 + m + n)/n, -p, -q, (1 + m + 2*n)/n, -((b*x^n)/a), -((d*x^n)/c)])/((1 + m)*(1 + m + n)*(1 + (b*x^n)/a)^p*(1 + (d*x^n)/c)^q)
```

**Maple [F]**

time = 0.33, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^p (A + Bx^n) (c + dx^n)^q dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(a+b*x^n)^p*(A+B*x^n)*(c+d*x^n)^q,x)
```

```
[Out] int((e*x)^m*(a+b*x^n)^p*(A+B*x^n)*(c+d*x^n)^q,x)
```

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)\*(c+d\*x^n)^q,x, algorithm="maxima")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^p\*(d\*x^n + c)^q\*(x\*e)^m, x)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)\*(c+d\*x^n)^q,x, algorithm="fricas")

[Out] integral((B\*x^n + A)\*(b\*x^n + a)^p\*(d\*x^n + c)^q\*(x\*e)^m, x)

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*p\*(A+B\*x\*\*n)\*(c+d\*x\*\*n)\*\*q,x)

[Out] Exception raised: HeuristicGCDFailed &gt;&gt; no luck

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)\*(c+d\*x^n)^q,x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^p\*(d\*x^n + c)^q\*(x\*e)^m, x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int (e x)^m (A + B x^n) (a + b x^n)^p (c + d x^n)^q dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^p\*(c + d\*x^n)^q,x)

[Out] int((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^p\*(c + d\*x^n)^q, x)

### 3.42 $\int (ex)^m (a + bx^n)^p (A + Bx^n) (c + dx^n) dx$

**Optimal.** Leaf size=271

$$\frac{(aBd(1+m+n) - b(Adn + Bc(1+m+n(2+p))))(ex)^{1+m} (a + bx^n)^{1+p}}{b^2e(1+m+n+np)(1+m+n(2+p))} + \frac{d(ex)^{1+m} (a + bx^n)^{1+p} (A + Bx^n)}{be(1+m+n(2+p))}$$

[Out]  $-(a*B*d*(1+m+n)-b*(A*d*n+B*c*(1+m+n*(2+p))))*(e*x)^{(1+m)}*(a+b*x^n)^{(1+p)}/b^2/e/(n*p+m+n+1)/(1+m+n*(2+p))+d*(e*x)^{(1+m)}*(a+b*x^n)^{(1+p)}*(A+B*x^n)/b/e/(1+m+n*(2+p))-(A*b*(n*p+m+n+1)*(a*d*(1+m)-b*c*(1+m+n*(2+p)))-a*(1+m)*(a*B*d*(1+m+n)-b*(A*d*n+B*c*(1+m+n*(2+p))))*(e*x)^{(1+m)}*(a+b*x^n)^p*\text{hypergeom}([-p, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/b^2/e/(1+m)/(n*p+m+n+1)/(1+m+n*(2+p))/((1+b*x^n/a)^p)$

**Rubi [A]**

time = 0.41, antiderivative size = 255, normalized size of antiderivative = 0.94, number of steps used = 4, number of rules used = 4, integrand size = 29,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.138$ , Rules used = {610, 470, 372, 371}

$$\frac{(ex)^{m+1} (a + bx^n)^{p+1} (-aBd(m+n+1) + Abdn + bBc(m+n(p+2)+1))}{b^2e(m+np+n+1)(m+n(p+2)+1)} - \frac{(ex)^{m+1} (a + bx^n)^p \left(\frac{bx^n}{a} + 1\right)^{-p} {}_2F_1\left(\frac{m+1}{n}, -p; \frac{m+n+1}{n}, -\frac{bx^n}{a}\right) \left(\frac{-aBd(m+n+1) + Abdn + bBc(m+n(p+2)+1)}{b(m+n(p+2)+1)} + aAd - \frac{Abc(m+n(p+2)+1)}{m+1}\right)}{b(m+n(p+2)+1)} + \frac{d(ex)^{m+1} (A + Bx^n) (a + bx^n)^{p+1}}{be(m+n(p+2)+1)}$$

Antiderivative was successfully verified.

[In]  $\text{Int}[(e*x)^m*(a + b*x^n)^p*(A + B*x^n)*(c + d*x^n), x]$

[Out]  $((A*b*d*n - a*B*d*(1+m+n) + b*B*c*(1+m+n*(2+p)))*(e*x)^{(1+m)}*(a + b*x^n)^{(1+p)})/(b^2*e*(1+m+n+np)*(1+m+n*(2+p))) + (d*(e*x)^{(1+m)}*(a + b*x^n)^{(1+p)}*(A + B*x^n))/(b*e*(1+m+n*(2+p))) - ((a*A*d - (A*b*c*(1+m+n*(2+p))))/(1+m) + (a*(A*b*d*n - a*B*d*(1+m+n) + b*B*c*(1+m+n*(2+p))))/(b*(1+m+n+np)))*(e*x)^{(1+m)}*(a + b*x^n)^p*\text{Hypergeometric2F1}[(1+m)/n, -p, (1+m+n)/n, -((b*x^n)/a)]/(b*e*(1+m+n*(2+p))*(1 + (b*x^n)/a)^p)$

**Rule 371**

$\text{Int}[(c*x)^m*(a + b*x^n)^p, x\_Symbol] := \text{Simp}[a^p*(c*x)^{(m+1)}/(c*(m+1))*\text{Hypergeometric2F1}[-p, (m+1)/n, (m+1)/n+1, (-b)*(x^n/a)], x] /; \text{FreeQ}\{a, b, c, m, n, p\}, x \ \&\& \ !\text{IGtQ}[p, 0] \ \&\& \ (\text{ILtQ}[p, 0] \ || \ \text{GtQ}[a, 0])$

**Rule 372**

$\text{Int}[(c*x)^m*(a + b*x^n)^p, x\_Symbol] := \text{Dist}[\text{IntPart}[p]*(a + b*x^n)^{\text{FracPart}[p]}/(1 + b*(x^n/a))^{\text{FracPart}[p]}, \text{Int}[(c*x)^m*(1 + b*(x^n/a))^p, x], x] /; \text{FreeQ}\{a, b, c, m, n, p\}, x \ \&\& \ !\text{IGtQ}[p, 0] \ \&\& \ !(\text{ILtQ}[p, 0] \ || \ \text{GtQ}[a, 0])$

Rule 470

```
Int[((e_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_)), x_Symbol] := Simp[d*(e*x)^(m + 1)*((a + b*x^n)^(p + 1)/(b*e*(m + n*(p + 1) + 1))), x] - Dist[(a*d*(m + 1) - b*c*(m + n*(p + 1) + 1))/(b*(m + n*(p + 1) + 1)), Int[(e*x)^m*(a + b*x^n)^p, x], x] /; FreeQ[{a, b, c, d, e, m, n, p}, x] && NeQ[b*c - a*d, 0] && NeQ[m + n*(p + 1) + 1, 0]
```

Rule 610

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_.)*((c_) + (d_.)*(x_)^(n_))^(q_.)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[f*(g*x)^(m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^q/(b*g*(m + n*(p + q + 1) + 1))), x] + Dist[1/(b*(m + n*(p + q + 1) + 1)), Int[(g*x)^m*(a + b*x^n)^p*(c + d*x^n)^(q - 1)*Simp[c*((b*e - a*f)*(m + 1) + b*e*n*(p + q + 1)) + (d*(b*e - a*f)*(m + 1) + f*n*q*(b*c - a*d) + b*e*d*n*(p + q + 1))*x^n, x], x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x] && GtQ[q, 0] && !(EqQ[q, 1] && SimplifierQ[e + f*x^n, c + d*x^n])
```

Rubi steps

$$\begin{aligned} \int (ex)^m (a + bx^n)^p (A + Bx^n) (c + dx^n) dx &= \frac{d(ex)^{1+m} (a + bx^n)^{1+p} (A + Bx^n)}{be(1 + m + n(2 + p))} + \frac{\int (ex)^m (a + bx^n)^p (-A + Bx^n) dx}{b^2e(1 + m + n + np)(1 + m + n(2 + p))} \\ &= \frac{(Abdn - aBd(1 + m + n) + bBc(1 + m + n(2 + p)))(ex)^{1+n}}{b^2e(1 + m + n + np)(1 + m + n(2 + p))} \\ &= \frac{(Abdn - aBd(1 + m + n) + bBc(1 + m + n(2 + p)))(ex)^{1+n}}{b^2e(1 + m + n + np)(1 + m + n(2 + p))} \\ &= \frac{(Abdn - aBd(1 + m + n) + bBc(1 + m + n(2 + p)))(ex)^{1+n}}{b^2e(1 + m + n + np)(1 + m + n(2 + p))} \end{aligned}$$

**Mathematica** [A]

time = 0.40, size = 164, normalized size = 0.61

$$x(ex)^m (a + bx^n)^p \left(1 + \frac{bx^n}{a}\right)^{-p} \left( \frac{Ac_2 F_1\left(\frac{1+m}{n}, -p; \frac{1+m+n}{n}; -\frac{bx^n}{a}\right)}{1+m} + x^n \left( \frac{(Bc + Ad) {}_2F_1\left(\frac{1+m+n}{n}, -p; \frac{1+m+2n}{n}; -\frac{bx^n}{a}\right)}{1+m+n} + \frac{Bdx^n {}_2F_1\left(\frac{1+m+2n}{n}, -p; \frac{1+m+3n}{n}; -\frac{bx^n}{a}\right)}{1+m+2n} \right) \right)$$

Antiderivative was successfully verified.

```
[In] Integrate[(e*x)^m*(a + b*x^n)^p*(A + B*x^n)*(c + d*x^n), x]
```

```
[Out] (x*(e*x)^m*(a + b*x^n)^p*((A*c*Hypergeometric2F1[(1 + m)/n, -p, (1 + m + n)/n, -(b*x^n)/a]))/(1 + m) + x^n*((B*c + A*d)*Hypergeometric2F1[(1 + m + n
```

)/n, -p, (1 + m + 2\*n)/n, -((b\*x^n)/a)]/(1 + m + n) + (B\*d\*x^n\*Hypergeometric2F1[(1 + m + 2\*n)/n, -p, (1 + m + 3\*n)/n, -((b\*x^n)/a)]/(1 + m + 2\*n)))/(1 + (b\*x^n)/a)^p

**Maple [F]**

time = 0.09, size = 0, normalized size = 0.00

$$\int (ex)^m (a + bx^n)^p (A + Bx^n)(c + dx^n) dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)\*(c+d\*x^n),x)

[Out] int((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)\*(c+d\*x^n),x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="maxima")

[Out] integrate((B\*x^n + A)\*(d\*x^n + c)\*(b\*x^n + a)^p\*(x\*e)^m, x)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)\*(c+d\*x^n),x, algorithm="fricas")

[Out] integral((B\*d\*x^(2\*n) + A\*c + (B\*c + A\*d)\*x^n)\*(b\*x^n + a)^p\*(x\*e)^m, x)

**Sympy [F(-1)]** Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*p\*(A+B\*x\*\*n)\*(c+d\*x\*\*n),x)

[Out] Timed out

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^p*(A+B*x^n)*(c+d*x^n),x, algorithm="giac")
```

```
[Out] integrate((B*x^n + A)*(d*x^n + c)*(b*x^n + a)^p*(x*e)^m, x)
```

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.00

$$\int (e x)^m (A + B x^n) (a + b x^n)^p (c + d x^n) dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((e*x)^m*(A + B*x^n)*(a + b*x^n)^p*(c + d*x^n),x)
```

```
[Out] int((e*x)^m*(A + B*x^n)*(a + b*x^n)^p*(c + d*x^n), x)
```

$$3.43 \quad \int \frac{(ex)^m (a+bx^n)^p (A+Bx^n)}{c+dx^n} dx$$

**Optimal.** Leaf size=164

$$\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^p \left(1 + \frac{bx^n}{a}\right)^{-p} F_1\left(\frac{1+m}{n}; -p, 1; \frac{1+m+n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right)}{cde(1+m)} + \frac{B(ex)^{1+m} (a + bx^n)^p (1 + \frac{bx^n}{a})^{-p}}{d}$$

[Out]  $-(A*d+B*c)*(e*x)^{(1+m)}*(a+b*x^n)^p*AppellF1((1+m)/n,-p,1,(1+m+n)/n,-b*x^n/a,-d*x^n/c)/c/d/e/(1+m)/((1+b*x^n/a)^p)+B*(e*x)^{(1+m)}*(a+b*x^n)^p*hypergeom([-p,(1+m)/n],[(1+m+n)/n],-b*x^n/a)/d/e/(1+m)/((1+b*x^n/a)^p)$

**Rubi [A]**

time = 0.12, antiderivative size = 164, normalized size of antiderivative = 1.00, number of steps used = 6, number of rules used = 5, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.161$ , Rules used = {611, 372, 371, 525, 524}

$$\frac{B(ex)^{m+1} (a + bx^n)^p \left(\frac{bx^n}{a} + 1\right)^{-p} {}_2F_1\left(\frac{m+1}{n}, -p; \frac{m+n+1}{n}; -\frac{bx^n}{a}\right)}{de(m+1)} - \frac{(ex)^{m+1} (Bc - Ad) (a + bx^n)^p \left(\frac{bx^n}{a} + 1\right)^{-p} F_1\left(\frac{m+1}{n}; -p, 1; \frac{m+n+1}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right)}{cde(m+1)}$$

Antiderivative was successfully verified.

[In] Int[((e\*x)^m\*(a + b\*x^n)^p\*(A + B\*x^n))/(c + d\*x^n),x]

[Out]  $-(((B*c - A*d)*(e*x)^{(1+m)}*(a + b*x^n)^p*AppellF1[(1+m)/n, -p, 1, (1+m+n)/n, -(b*x^n)/a, -(d*x^n)/c])/(c*d*e*(1+m)*(1+(b*x^n)/a)^p) + (B*(e*x)^{(1+m)}*(a + b*x^n)^p*Hypergeometric2F1[(1+m)/n, -p, (1+m+n)/n, -(b*x^n)/a])/(d*e*(1+m)*(1+(b*x^n)/a)^p)$

**Rule 371**

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

**Rule 372**

Int[((c\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_), x\_Symbol] :> Dist[a^IntPart[p]\*((a + b\*x^n)^FracPart[p]/(1 + b\*(x^n/a))^FracPart[p]), Int[(c\*x)^m\*(1 + b\*(x^n/a))^p, x], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && !(ILtQ[p, 0] || GtQ[a, 0])

**Rule 524**

Int[((e\_.)\*(x\_))^(m\_.)\*((a\_) + (b\_.)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_.)\*(x\_)^(n\_))^(q\_), x\_Symbol] :> Simp[a^p\*c^q\*((e\*x)^(m+1)/(e\*(m+1)))\*AppellF1[(m+1)/n, -p, -q, 1+(m+1)/n, (-b)\*(x^n/a), (-d)\*(x^n/c)], x] /; FreeQ[{a, b, c, d, e, m, n, p, q}, x] && NeQ[b\*c - a\*d, 0] && NeQ[m, -1] && NeQ[m, n]



- 1] && (IntegerQ[p] || GtQ[a, 0]) && (IntegerQ[q] || GtQ[c, 0])

### Rule 525

```
Int[((e_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_))^(q_), x_Symbol] :> Dist[a^IntPart[p]*((a + b*x^n)^FracPart[p]/(1 + b*(x^n/a)^FracPart[p]), Int[(e*x)^m*(1 + b*(x^n/a))^p*(c + d*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, m, n, p, q}, x] && NeQ[b*c - a*d, 0] && NeQ[m, -1] && NeQ[m, n - 1] && !(IntegerQ[p] || GtQ[a, 0])
```

### Rule 611

```
Int[(((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((e_) + (f_.)*(x_)^(n_)))/((c_) + (d_.)*(x_)^(n_)), x_Symbol] :> Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*(e + f*x^n)/(c + d*x^n), x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x]
```

### Rubi steps

$$\begin{aligned} \int \frac{(ex)^m (a + bx^n)^p (A + Bx^n)}{c + dx^n} dx &= \int \left( \frac{B(ex)^m (a + bx^n)^p}{d} + \frac{(-Bc + Ad)(ex)^m (a + bx^n)^p}{d(c + dx^n)} \right) dx \\ &= \frac{B \int (ex)^m (a + bx^n)^p dx}{d} + \frac{(-Bc + Ad) \int \frac{(ex)^m (a + bx^n)^p}{c + dx^n} dx}{d} \\ &= \frac{\left( B(a + bx^n)^p \left( 1 + \frac{bx^n}{a} \right)^{-p} \right) \int (ex)^m \left( 1 + \frac{bx^n}{a} \right)^p dx}{d} + \frac{((-Bc + Ad)(a + bx^n)^p)}{d} \\ &= -\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^p \left( 1 + \frac{bx^n}{a} \right)^{-p} F_1\left(\frac{1+m}{n}; -p, 1; \frac{1+m+n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right) + B(1+m)x^n F_1\left(\frac{1+m+n}{n}; -p, 1; \frac{1+m+2n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right)}{cde(1+m)} \end{aligned}$$

### Mathematica [A]

time = 0.20, size = 138, normalized size = 0.84

$$\frac{x(ex)^m (a + bx^n)^p \left( 1 + \frac{bx^n}{a} \right)^{-p} \left( A(1+m+n) F_1\left(\frac{1+m}{n}; -p, 1; \frac{1+m+n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right) + B(1+m)x^n F_1\left(\frac{1+m+n}{n}; -p, 1; \frac{1+m+2n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right) \right)}{c(1+m)(1+m+n)}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)^p\*(A + B\*x^n))/(c + d\*x^n),x]

[Out] (x\*(e\*x)^m\*(a + b\*x^n)^p\*(A\*(1 + m + n)\*AppellF1[(1 + m)/n, -p, 1, (1 + m + n)/n, -(b\*x^n)/a, -(d\*x^n)/c] + B\*(1 + m)\*x^n\*AppellF1[(1 + m + n)/n, -p, 1, (1 + m + 2\*n)/n, -(b\*x^n)/a, -(d\*x^n)/c]))/(c\*(1 + m)\*(1 + m + n)\*(1 + (b\*x^n)/a)^p)

**Maple [F]**

time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^p (A + Bx^n)}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)/(c+d\*x^n),x)

[Out] int((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)/(c+d\*x^n),x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="maxima")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^p\*(x\*e)^m/(d\*x^n + c), x)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="fricas")

[Out] integral((B\*x^n + A)\*(b\*x^n + a)^p\*(x\*e)^m/(d\*x^n + c), x)

**Sympy [F(-2)]**

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)\*\*m\*(a+b\*x\*\*n)\*\*p\*(A+B\*x\*\*n)/(c+d\*x\*\*n),x)

[Out] Exception raised: HeuristicGCDFailed &gt;&gt; no luck

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)/(c+d\*x^n),x, algorithm="giac")

[Out] integrate((B\*x^n + A)\*(b\*x^n + a)^p\*(x\*e)^m/(d\*x^n + c), x)

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^p}{c + dx^n} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^p)/(c + d\*x^n),x)

[Out] int(((e\*x)^m\*(A + B\*x^n)\*(a + b\*x^n)^p)/(c + d\*x^n), x)

$$3.44 \quad \int \frac{(ex)^m (a+bx^n)^p (A+Bx^n)}{(c+dx^n)^2} dx$$

**Optimal.** Leaf size=304

$$\frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^{1+p}}{c(bc - ad)en(c + dx^n)} \frac{(ad(Bc(1 + m) - Ad(1 + m - n)) + bc(Ad(1 + m - n(1 - p)) - Bc(1 + m - n))}{c^2 d(bc - ad)}$$

[Out]  $(-A*d+B*c)*(e*x)^{(1+m)}*(a+b*x^n)^{(1+p)}/c/(-a*d+b*c)/e/n/(c+d*x^n)-(a*d*(B*c*(1+m)-A*d*(1+m-n))+b*c*(A*d*(1+m-n*(1-p))-B*c*(n*p+m+1)))*(e*x)^{(1+m)}*(a+b*x^n)^p*$ AppellF1 $((1+m)/n, -p, 1, (1+m+n)/n, -b*x^n/a, -d*x^n/c)/c^2/d/(-a*d+b*c)/e/(1+m)/n/(((1+b*x^n/a)^p)-b*(-A*d+B*c)*(n*p+m+1)*(e*x)^{(1+m)}*(a+b*x^n)^p*$ hypergeom $([-p, (1+m)/n], [(1+m+n)/n], -b*x^n/a)/c/d/(-a*d+b*c)/e/(1+m)/n/((1+b*x^n/a)^p)$

**Rubi [A]**

time = 0.35, antiderivative size = 304, normalized size of antiderivative = 1.00, number of steps used = 7, number of rules used = 6, integrand size = 31,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.194$ , Rules used = {609, 611, 372, 371, 525, 524}

$$\frac{(ex)^{m+1}(a+bx^n)^p \left(\frac{bc}{c^2} + 1\right)^{-p} (ad(Bc(m+1) - Ad(m-n+1)) + bc(Ad(m-n(1-p)+1) - Bc(m+np+1))) {}_2F_1\left(\frac{m+1}{n}, 1; \frac{m+1}{n}, -\frac{bx^n}{a}, -\frac{dx^n}{c}\right) - \frac{b(ex)^{m+1}(m+np+1)(Bc-Ad)(a+bx^n)^p \left(\frac{bc}{c^2} + 1\right)^{-p} {}_2F_1\left(\frac{m+1}{n}, -p; \frac{m+1}{n}, -\frac{bx^n}{a}\right) + \frac{(ex)^{m+1}(Bc-Ad)(a+bx^n)^{p+1}}{en(bc-ad)(c+dx^n)}$$

Antiderivative was successfully verified.

[In] Int $([(e*x)^m*(a + b*x^n)^p*(A + B*x^n)]/(c + d*x^n)^2, x]$

[Out]  $((B*c - A*d)*(e*x)^{(1 + m)}*(a + b*x^n)^{(1 + p)})/(c*(b*c - a*d)*e*n*(c + d*x^n) - ((a*d*(B*c*(1 + m) - A*d*(1 + m - n)) + b*c*(A*d*(1 + m - n*(1 - p)) - B*c*(1 + m + n*p)))*(e*x)^{(1 + m)}*(a + b*x^n)^p*$ AppellF1 $[(1 + m)/n, -p, 1, (1 + m + n)/n, -((b*x^n)/a), -((d*x^n)/c)]/(c^2*d*(b*c - a*d)*e*(1 + m)*n*(1 + (b*x^n)/a)^p - (b*(B*c - A*d)*(1 + m + n*p)*(e*x)^{(1 + m)}*(a + b*x^n)^p*$ Hypergeometric2F1 $[(1 + m)/n, -p, (1 + m + n)/n, -((b*x^n)/a)]/(c*d*(b*c - a*d)*e*(1 + m)*n*(1 + (b*x^n)/a)^p)$

**Rule 371**

Int $([(c_.)*(x_.)]^{(m_.)}*((a_.) + (b_.)*(x_.)^{(n_.)})^{(p_.)}, x\_Symbol] :> Simp[a^p*((c*x)^{(m+1)}/(c*(m+1)))*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])$

**Rule 372**

Int $([(c_.)*(x_.)]^{(m_.)}*((a_.) + (b_.)*(x_.)^{(n_.)})^{(p_.)}, x\_Symbol] :> Dist[a^IntPart[p]*((a + b*x^n)^FracPart[p]/(1 + b*(x^n/a))^FracPart[p]), Int[(c*x)^m*(1 + b*(x^n/a))^p, x], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && !(ILtQ[p, 0] || GtQ[a, 0])$

Rule 524

```
Int[((e_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_))^(q_), x_Symbol] := Simp[a^p*c^q*((e*x)^(m + 1)/(e*(m + 1)))*AppellF1[(m + 1)/n, -p, -q, 1 + (m + 1)/n, (-b)*(x^n/a), (-d)*(x^n/c)], x] /; FreeQ[{a, b, c, d, e, m, n, p, q}, x] && NeQ[b*c - a*d, 0] && NeQ[m, -1] && NeQ[m, n - 1] && (IntegerQ[p] || GtQ[a, 0]) && (IntegerQ[q] || GtQ[c, 0])
```

Rule 525

```
Int[((e_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_))^(q_), x_Symbol] := Dist[a^IntPart[p]*((a + b*x^n)^FracPart[p]/(1 + b*(x^n/a))^FracPart[p]), Int[(e*x)^m*(1 + b*(x^n/a))^p*(c + d*x^n)^q, x], x] /; FreeQ[{a, b, c, d, e, m, n, p, q}, x] && NeQ[b*c - a*d, 0] && NeQ[m, -1] && NeQ[m, n - 1] && !(IntegerQ[p] || GtQ[a, 0])
```

Rule 609

```
Int[((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((c_) + (d_.)*(x_)^(n_))^(q_)*((e_) + (f_.)*(x_)^(n_)), x_Symbol] := Simp[(-(b*e - a*f))*(g*x)^(m + 1)*(a + b*x^n)^(p + 1)*((c + d*x^n)^(q + 1)/(a*g*n*(b*c - a*d)*(p + 1))), x] + Dist[1/(a*n*(b*c - a*d)*(p + 1)), Int[(g*x)^m*(a + b*x^n)^(p + 1)*(c + d*x^n)^q*Simp[c*(b*e - a*f)*(m + 1) + e*n*(b*c - a*d)*(p + 1) + d*(b*e - a*f)*(m + n*(p + q + 2) + 1)*x^n, x], x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, q}, x] && LtQ[p, -1]
```

Rule 611

```
Int[(((g_.)*(x_))^(m_.)*((a_) + (b_.)*(x_)^(n_))^(p_)*((e_) + (f_.)*(x_)^(n_)))/((c_) + (d_.)*(x_)^(n_)), x_Symbol] := Int[ExpandIntegrand[(g*x)^m*(a + b*x^n)^p*((e + f*x^n)/(c + d*x^n)), x], x] /; FreeQ[{a, b, c, d, e, f, g, m, n, p}, x]
```

Rubi steps

$$\begin{aligned}
\int \frac{(ex)^m (a + bx^n)^p (A + Bx^n)}{(c + dx^n)^2} dx &= \frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^{1+p}}{c(bc - ad)en (c + dx^n)} + \frac{\int \frac{(ex)^m (a + bx^n)^p (-a(Bc - Ad)(1+m) + A(bc - ad))}{c + dx^n}}{c(bc - ad)n} \\
&= \frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^{1+p}}{c(bc - ad)en (c + dx^n)} + \frac{\int \left( -\frac{b(Bc - Ad)(1+m+np)(ex)^m (a + bx^n)^p}{d} + \right)}{c(bc - ad)n} \\
&= \frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^{1+p}}{c(bc - ad)en (c + dx^n)} - \frac{(b(Bc - Ad)(1 + m + np)) \int (ex)^m (a + bx^n)^p}{cd(bc - ad)n} \\
&= \frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^{1+p}}{c(bc - ad)en (c + dx^n)} - \frac{(b(Bc - Ad)(1 + m + np) (a + bx^n)^p)}{cd(bc - ad)n} \\
&= \frac{(Bc - Ad)(ex)^{1+m} (a + bx^n)^{1+p}}{c(bc - ad)en (c + dx^n)} - \frac{(ad(Bc - Ad)(1 + m) - Ad(bc - ad)) \int (ex)^m (a + bx^n)^p}{c^2(1 + m)(1 + m + n)}
\end{aligned}$$

**Mathematica [A]**

time = 0.27, size = 138, normalized size = 0.45

$$\frac{x(ex)^m (a + bx^n)^p \left(1 + \frac{bx^n}{a}\right)^{-p} \left(A(1 + m + n)F_1\left(\frac{1+m}{n}; -p, 2; \frac{1+m+n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right) + B(1 + m)x^n F_1\left(\frac{1+m+n}{n}; -p, 2; \frac{1+m+2n}{n}; -\frac{bx^n}{a}, -\frac{dx^n}{c}\right)\right)}{c^2(1 + m)(1 + m + n)}$$

Antiderivative was successfully verified.

[In] Integrate[((e\*x)^m\*(a + b\*x^n)^p\*(A + B\*x^n))/(c + d\*x^n)^2,x]

[Out] (x\*(e\*x)^m\*(a + b\*x^n)^p\*(A\*(1 + m + n)\*AppellF1[(1 + m)/n, -p, 2, (1 + m + n)/n, -((b\*x^n)/a), -((d\*x^n)/c)] + B\*(1 + m)\*x^n\*AppellF1[(1 + m + n)/n, -p, 2, (1 + m + 2\*n)/n, -((b\*x^n)/a), -((d\*x^n)/c)]))/(c^2\*(1 + m)\*(1 + m + n)\*(1 + (b\*x^n)/a)^p)

**Maple [F]**

time = 0.14, size = 0, normalized size = 0.00

$$\int \frac{(ex)^m (a + bx^n)^p (A + Bx^n)}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)/(c+d\*x^n)^2,x)

[Out] int((e\*x)^m\*(a+b\*x^n)^p\*(A+B\*x^n)/(c+d\*x^n)^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^p*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="maxima")
```

```
[Out] integrate((B*x^n + A)*(b*x^n + a)^p*(x*e)^m/(d*x^n + c)^2, x)
```

**Fricas** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^p*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="fricas")
```

```
[Out] integral((B*x^n + A)*(b*x^n + a)^p*(x*e)^m/(d^2*x^(2*n) + 2*c*d*x^n + c^2),
x)
```

**Sympy** [F(-2)]

time = 0.00, size = 0, normalized size = 0.00

Exception raised: HeuristicGCDFailed

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)**m*(a+b*x**n)**p*(A+B*x**n)/(c+d*x**n)**2,x)
```

```
[Out] Exception raised: HeuristicGCDFailed >> no luck
```

**Giac** [F]

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((e*x)^m*(a+b*x^n)^p*(A+B*x^n)/(c+d*x^n)^2,x, algorithm="giac")
```

```
[Out] integrate((B*x^n + A)*(b*x^n + a)^p*(x*e)^m/(d*x^n + c)^2, x)
```

**Mupad** [F]

time = 0.00, size = -1, normalized size = -0.00

$$\int \frac{(ex)^m (A + Bx^n) (a + bx^n)^p}{(c + dx^n)^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(((e*x)^m*(A + B*x^n)*(a + b*x^n)^p)/(c + d*x^n)^2,x)
```

```
[Out] int(((e*x)^m*(A + B*x^n)*(a + b*x^n)^p)/(c + d*x^n)^2, x)
```

$$3.45 \quad \int \frac{(-a+bx^{n/2})^{-1+\frac{1}{n}} (a+bx^{n/2})^{-1+\frac{1}{n}} (c+dx^n)}{x^2} dx$$

**Optimal.** Leaf size=139

$$\frac{\left(\frac{c}{a^2} + \frac{d}{b^2}\right) (-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} - \frac{d(-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}} \left(1 - \frac{b^2 x^n}{a^2}\right)^{-1/n}}{b^2 x} {}_2F_1\left(-\frac{1}{n}, -\frac{1}{n}; -\frac{1-n}{n}; \frac{b^2 x^n}{a^2}\right)$$

[Out] (c/a^2+d/b^2)\*(-a+b\*x^(1/2\*n))^(1/n)\*(a+b\*x^(1/2\*n))^(1/n)/x-d\*(-a+b\*x^(1/2\*n))^(1/n)\*(a+b\*x^(1/2\*n))^(1/n)\*hypergeom([-1/n, -1/n], [(-1+n)/n], b^2\*x^n/a^2)/b^2/x/((1-b^2\*x^n/a^2)^(1/n))

**Rubi [A]**

time = 0.07, antiderivative size = 139, normalized size of antiderivative = 1.00, number of steps used = 4, number of rules used = 4, integrand size = 47,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.085$ , Rules used = {533, 463, 372, 371}

$$\frac{\left(\frac{c}{a^2} + \frac{d}{b^2}\right) (bx^{n/2} - a)^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} - \frac{d(bx^{n/2} - a)^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}} \left(1 - \frac{b^2 x^n}{a^2}\right)^{-1/n}}{b^2 x} {}_2F_1\left(-\frac{1}{n}, -\frac{1}{n}; -\frac{1-n}{n}; \frac{b^2 x^n}{a^2}\right)$$

Antiderivative was successfully verified.

[In] Int[((-a + b\*x^(n/2))^(n-1)\*(a + b\*x^(n/2))^(n-1)\*(c + d\*x^n))/x^2,x]

[Out] ((c/a^2 + d/b^2)\*(-a + b\*x^(n/2))^(n-1)\*(a + b\*x^(n/2))^(n-1))/x - (d\*(-a + b\*x^(n/2))^(n-1)\*(a + b\*x^(n/2))^(n-1)\*Hypergeometric2F1[-n^(-1), -n^(-1), -(1-n)/n, (b^2\*x^n)/a^2])/(b^2\*x\*(1 - (b^2\*x^n)/a^2)^(n-1))

**Rule 371**

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m+1)/(c\*(m+1)))\*Hypergeometric2F1[-p, (m+1)/n, (m+1)/n+1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

**Rule 372**

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Dist[a^IntPart[p]\*((a + b\*x^n)^FracPart[p]/(1 + b\*(x^n/a))^FracPart[p]), Int[(c\*x)^(m\*(1 + b\*(x^n/a))^p, x], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && !(ILtQ[p, 0] || GtQ[a, 0])

**Rule 463**

Int[((e\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_)\*((c\_) + (d\_)\*(x\_)^(n\_)), x\_Symbol] := Simp[(b\*c - a\*d)\*(e\*x)^(m+1)\*((a + b\*x^n)^(p+1)/(a\*b\*



```
e*(m + 1))), x] + Dist[d/b, Int[(e*x)^m*(a + b*x^n)^(p + 1), x], x] /; Free
Q[{a, b, c, d, e, m, n, p}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n*(p + 1) +
1, 0] && NeQ[m, -1]
```

### Rule 533

```
Int[(u_)*((c_) + (d_)*(x_)^(n_))^(q_)*((a1_) + (b1_)*(x_)^(non2_))^(p
_)*((a2_) + (b2_)*(x_)^(non2_))^(p_), x_Symbol] := Dist[(a1 + b1*x^(n/2))
^FracPart[p]*((a2 + b2*x^(n/2))^FracPart[p]/(a1*a2 + b1*b2*x^n)^FracPart[p]
), Int[u*(a1*a2 + b1*b2*x^n)^p*(c + d*x^n)^q, x] /; FreeQ[{a1, b1, a2,
b2, c, d, n, p, q}, x] && EqQ[non2, n/2] && EqQ[a2*b1 + a1*b2, 0] && !(EqQ
[n, 2] && IGtQ[q, 0])
```

### Rubi steps

$$\begin{aligned} \int \frac{(-a + bx^{n/2})^{-1+\frac{1}{n}} (a + bx^{n/2})^{-1+\frac{1}{n}} (c + dx^n)}{x^2} dx &= \left( (-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}} (-a^2 + b^2 x^n)^{-1/n} \right) \int \\ &= \frac{\left( \frac{c}{a^2} + \frac{d}{b^2} \right) (-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} + \frac{d(-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} \\ &= \frac{\left( \frac{c}{a^2} + \frac{d}{b^2} \right) (-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} + \frac{d(-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} \\ &= \frac{\left( \frac{c}{a^2} + \frac{d}{b^2} \right) (-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} - \frac{d(-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} \end{aligned}$$

### Mathematica [A]

time = 0.33, size = 124, normalized size = 0.89

$$\frac{(-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}} \left(1 - \frac{b^2 x^n}{a^2}\right)^{-1/n} \left( c(-1 + n) \left(1 - \frac{b^2 x^n}{a^2}\right)^{\frac{1}{n}} - dx^n {}_2F_1\left(\frac{-1+n}{n}, \frac{-1+n}{n}; 2 - \frac{1}{n}; \frac{b^2 x^n}{a^2}\right) \right)}{a^2(-1 + n)x}$$

Antiderivative was successfully verified.

```
[In] Integrate[((-a + b*x^(n/2))^(n^(-1))*(a + b*x^(n/2))^(n^(-1))*(c
+ d*x^n))/x^2,x]
```

```
[Out] ((-a + b*x^(n/2))^n^(-1)*(a + b*x^(n/2))^n^(-1)*(c*(-1 + n)*(1 - (b^2*x^n)/
a^2)^n^(-1) - d*x^n*Hypergeometric2F1[(-1 + n)/n, (-1 + n)/n, 2 - n^(-1), (
b^2*x^n)/a^2]))/(a^2*(-1 + n)*x*(1 - (b^2*x^n)/a^2)^n^(-1))
```

**Maple [F]**

time = 0.16, size = 0, normalized size = 0.00

$$\int \frac{(-a + bx^{\frac{n}{2}})^{-1+\frac{1}{n}} (a + bx^{\frac{n}{2}})^{-1+\frac{1}{n}} (c + dx^n)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-a+b\*x^(1/2\*n))^(-1+1/n)\*(a+b\*x^(1/2\*n))^(-1+1/n)\*(c+d\*x^n)/x^2,x)

[Out] int((-a+b\*x^(1/2\*n))^(-1+1/n)\*(a+b\*x^(1/2\*n))^(-1+1/n)\*(c+d\*x^n)/x^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-a+b\*x^(1/2\*n))^(-1+1/n)\*(a+b\*x^(1/2\*n))^(-1+1/n)\*(c+d\*x^n)/x^2, x, algorithm="maxima")

[Out] integrate((d\*x^n + c)\*(b\*x^(1/2\*n) + a)^(1/n - 1)\*(b\*x^(1/2\*n) - a)^(1/n - 1)/x^2, x)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-a+b\*x^(1/2\*n))^(-1+1/n)\*(a+b\*x^(1/2\*n))^(-1+1/n)\*(c+d\*x^n)/x^2, x, algorithm="fricas")

[Out] integral((d\*x^n + c)/((b\*x^(1/2\*n) + a)^((n - 1)/n)\*(b\*x^(1/2\*n) - a)^((n - 1)/n)\*x^2), x)

**Sympy [F(-1)]** Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-a+b\*x\*\*(1/2\*n))\*\*(-1+1/n)\*(a+b\*x\*\*(1/2\*n))\*\*(-1+1/n)\*(c+d\*x\*\*n)/x\*\*2,x)

[Out] Timed out

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-a+b*x^(1/2*n))^(1/n)*(a+b*x^(1/2*n))^(1/n)*(c+d*x^n)/x^2,
x, algorithm="giac")
```

```
[Out] integrate((d*x^n + c)*(b*x^(1/2*n) + a)^(1/n - 1)*(b*x^(1/2*n) - a)^(1/n -
1)/x^2, x)
```

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{(a + b x^{n/2})^{\frac{1}{n}-1} (b x^{n/2} - a)^{\frac{1}{n}-1} (c + d x^n)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int(((a + b*x^(n/2))^(1/n - 1)*(b*x^(n/2) - a)^(1/n - 1)*(c + d*x^n))/x^2,x
)
```

```
[Out] int(((a + b*x^(n/2))^(1/n - 1)*(b*x^(n/2) - a)^(1/n - 1)*(c + d*x^n))/x^2,
x)
```

$$3.46 \quad \int \frac{\left(-a+bx^{n/2}\right)^{\frac{1-n}{n}} \left(a+bx^{n/2}\right)^{\frac{1-n}{n}} (c+dx^n)}{x^2} dx$$

**Optimal.** Leaf size=139

$$\frac{\left(\frac{c}{a^2} + \frac{d}{b^2}\right) (-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}}}{x} - \frac{d(-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}} \left(1 - \frac{b^2 x^n}{a^2}\right)^{-1/n}}{b^2 x} {}_2F_1\left(-\frac{1}{n}, -\frac{1}{n}; -\frac{1-n}{n}; \frac{b^2 x^n}{a^2}\right)$$

[Out] (c/a^2+d/b^2)\*(-a+b\*x^(1/2\*n))^(1/n)\*(a+b\*x^(1/2\*n))^(1/n)/x-d\*(-a+b\*x^(1/2\*n))^(1/n)\*(a+b\*x^(1/2\*n))^(1/n)\*hypergeom([-1/n, -1/n], [(-1+n)/n], b^2\*x^n/a^2)/b^2/x/((1-b^2\*x^n/a^2)^(1/n))

**Rubi [A]**

time = 0.08, antiderivative size = 167, normalized size of antiderivative = 1.20, number of steps used = 4, number of rules used = 4, integrand size = 55,  $\frac{\text{number of rules}}{\text{integrand size}} = 0.073$ , Rules used = {533, 463, 372, 371}

$$\frac{a^2 d (bx^{n/2} - a)^{\frac{1}{n}-1} (a + bx^{n/2})^{\frac{1}{n}-1} \left(1 - \frac{b^2 x^n}{a^2}\right)^{-\frac{1-n}{n}} {}_2F_1\left(-\frac{1}{n}, -\frac{1}{n}; -\frac{1-n}{n}; \frac{b^2 x^n}{a^2}\right)}{b^2 x} - \frac{\left(\frac{c}{a^2} + \frac{d}{b^2}\right) (bx^{n/2} - a)^{\frac{1}{n}-1} (a + bx^{n/2})^{\frac{1}{n}-1} (a^2 - b^2 x^n)}{x}$$

Antiderivative was successfully verified.

[In] Int[((-a + b\*x^(n/2))^(1 - n/n)\*(a + b\*x^(n/2))^(1 - n/n)\*(c + d\*x^n))/x^2, x]

[Out] -(((c/a^2 + d/b^2)\*(-a + b\*x^(n/2))^(1 - n/n)\*(a + b\*x^(n/2))^(1 - n/n)\*(a^2 - b^2\*x^n))/x) + (a^2\*d\*(-a + b\*x^(n/2))^(1 - n/n)\*(a + b\*x^(n/2))^(1 - n/n)\*Hypergeometric2F1[-n/n, -n/n, -((1 - n)/n), (b^2\*x^n/a^2)]/(b^2\*x\*(1 - (b^2\*x^n)/a^2)^(1 - n/n))

**Rule 371**

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Simp[a^p\*((c\*x)^(m + 1)/(c\*(m + 1)))\*Hypergeometric2F1[-p, (m + 1)/n, (m + 1)/n + 1, (-b)\*(x^n/a)], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && (ILtQ[p, 0] || GtQ[a, 0])

**Rule 372**

Int[((c\_)\*(x\_))^(m\_)\*((a\_) + (b\_)\*(x\_)^(n\_))^(p\_), x\_Symbol] := Dist[a^IntPart[p]\*((a + b\*x^n)^FracPart[p]/(1 + b\*(x^n/a))^FracPart[p]), Int[(c\*x)^m\*(1 + b\*(x^n/a))^p, x], x] /; FreeQ[{a, b, c, m, n, p}, x] && !IGtQ[p, 0] && !(ILtQ[p, 0] || GtQ[a, 0])

**Rule 463**

```
Int[((e._)*(x_))^(m._)*((a_) + (b._)*(x_)^(n_))^(p._)*((c_) + (d._)*(x_)^(n_)), x_Symbol] := Simp[(b*c - a*d)*(e*x)^(m + 1)*((a + b*x^n)^(p + 1)/(a*b*e*(m + 1))), x] + Dist[d/b, Int[(e*x)^m*(a + b*x^n)^(p + 1), x], x] /; FreeQ[{a, b, c, d, e, m, n, p}, x] && NeQ[b*c - a*d, 0] && EqQ[m + n*(p + 1) + 1, 0] && NeQ[m, -1]
```

### Rule 533

```
Int[(u._)*((c_) + (d._)*(x_)^(n_))^(q._)*((a1_) + (b1._)*(x_)^(non2_))^(p_)*((a2_) + (b2._)*(x_)^(non2_))^(p_), x_Symbol] := Dist[(a1 + b1*x^(n/2))^(FracPart[p])*((a2 + b2*x^(n/2))^(FracPart[p])/(a1*a2 + b1*b2*x^n)^(FracPart[p])), Int[u*(a1*a2 + b1*b2*x^n)^p*(c + d*x^n)^q, x], x] /; FreeQ[{a1, b1, a2, b2, c, d, n, p, q}, x] && EqQ[non2, n/2] && EqQ[a2*b1 + a1*b2, 0] && !(EqQ[n, 2] && IGtQ[q, 0])
```

### Rubi steps

$$\int \frac{(-a + bx^{n/2})^{\frac{1-n}{n}} (a + bx^{n/2})^{\frac{1-n}{n}} (c + dx^n)}{x^2} dx = \left( (-a + bx^{n/2})^{\frac{1-n}{n}} (a + bx^{n/2})^{\frac{1-n}{n}} (-a^2 + b^2 x^n)^{-\frac{1-n}{n}} \right) \int \frac{(\frac{c}{a^2} + \frac{d}{b^2}) (-a + bx^{n/2})^{-1+\frac{1}{n}} (a + bx^{n/2})^{-1+\frac{1}{n}} (a^2 - b^2 x^n)^{-\frac{1-n}{n}}}{x} dx$$

$$= -\frac{(\frac{c}{a^2} + \frac{d}{b^2}) (-a + bx^{n/2})^{-1+\frac{1}{n}} (a + bx^{n/2})^{-1+\frac{1}{n}} (a^2 - b^2 x^n)^{-\frac{1-n}{n}}}{x}$$

$$= -\frac{(\frac{c}{a^2} + \frac{d}{b^2}) (-a + bx^{n/2})^{-1+\frac{1}{n}} (a + bx^{n/2})^{-1+\frac{1}{n}} (a^2 - b^2 x^n)^{-\frac{1-n}{n}}}{x}$$

$$= -\frac{(\frac{c}{a^2} + \frac{d}{b^2}) (-a + bx^{n/2})^{-1+\frac{1}{n}} (a + bx^{n/2})^{-1+\frac{1}{n}} (a^2 - b^2 x^n)^{-\frac{1-n}{n}}}{x}$$

### Mathematica [A]

time = 0.07, size = 124, normalized size = 0.89

$$\frac{(-a + bx^{n/2})^{\frac{1}{n}} (a + bx^{n/2})^{\frac{1}{n}} \left(1 - \frac{b^2 x^n}{a^2}\right)^{-1/n} \left(c(-1 + n) \left(1 - \frac{b^2 x^n}{a^2}\right)^{\frac{1}{n}} - dx^n {}_2F_1\left(\frac{-1+n}{n}, \frac{-1+n}{n}; 2 - \frac{1}{n}, \frac{b^2 x^n}{a^2}\right)\right)}{a^2(-1 + n)x}$$

Antiderivative was successfully verified.

```
[In] Integrate[((-a + b*x^(n/2))^(1/n)*(a + b*x^(n/2))^(1/n)*(c + d*x^n))/x^2, x]
```

```
[Out] ((-a + b*x^(n/2))^(1/n)*(a + b*x^(n/2))^(1/n)*(c*(-1 + n)*(1 - (b^2*x^n)/a^2)^(1/n) - d*x^n*Hypergeometric2F1[(-1 + n)/n, (-1 + n)/n, 2 - n^(-1), (b^2*x^n)/a^2]))/(a^2*(-1 + n)*x*(1 - (b^2*x^n)/a^2)^(1/n))
```

**Maple [F]**

time = 0.15, size = 0, normalized size = 0.00

$$\int \frac{(-a + b x^{\frac{n}{2}})^{\frac{1-n}{n}} (a + b x^{\frac{n}{2}})^{\frac{1-n}{n}} (c + d x^n)}{x^2} dx$$

Verification of antiderivative is not currently implemented for this CAS.

[In] int((-a+b\*x^(1/2\*n))^(1-n/n)\*(a+b\*x^(1/2\*n))^(1-n/n)\*(c+d\*x^n)/x^2,x)

[Out] int((-a+b\*x^(1/2\*n))^(1-n/n)\*(a+b\*x^(1/2\*n))^(1-n/n)\*(c+d\*x^n)/x^2,x)

**Maxima [F]**

time = 0.00, size = 0, normalized size = 0.00

Failed to integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-a+b\*x^(1/2\*n))^(1-n/n)\*(a+b\*x^(1/2\*n))^(1-n/n)\*(c+d\*x^n)/x^2,x, algorithm="maxima")

[Out] integrate((d\*x^n + c)/((b\*x^(1/2\*n) + a)^(n-1/n)\*(b\*x^(1/2\*n) - a)^(n-1/n)\*x^2), x)

**Fricas [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-a+b\*x^(1/2\*n))^(1-n/n)\*(a+b\*x^(1/2\*n))^(1-n/n)\*(c+d\*x^n)/x^2,x, algorithm="fricas")

[Out] integral((d\*x^n + c)/((b\*x^(1/2\*n) + a)^(n-1/n)\*(b\*x^(1/2\*n) - a)^(n-1/n)\*x^2), x)

**Sympy [F(-1)]** Timed out

time = 0.00, size = 0, normalized size = 0.00

Timed out

Verification of antiderivative is not currently implemented for this CAS.

[In] integrate((-a+b\*x\*\*(1/2\*n))\*\*(1-n/n)\*(a+b\*x\*\*(1/2\*n))\*\*(1-n/n)\*(c+d\*x\*\*n)/x\*\*2,x)

[Out] Timed out

**Giac [F]**

time = 0.00, size = 0, normalized size = 0.00

could not integrate

Verification of antiderivative is not currently implemented for this CAS.

```
[In] integrate((-a+b*x^(1/2*n))^(1/n)*(a+b*x^(1/2*n))^(1/n)*(c+d*x^n)/x^2,x, algorithm="giac")
```

```
[Out] integrate((d*x^n + c)/((b*x^(1/2*n) + a)^((n - 1)/n)*(b*x^(1/2*n) - a)^((n - 1)/n)*x^2), x)
```

**Mupad [F]**

time = 0.00, size = -1, normalized size = -0.01

$$\int \frac{c + dx^n}{x^2 (a + bx^{n/2})^{\frac{n-1}{n}} (bx^{n/2} - a)^{\frac{n-1}{n}}} dx$$

Verification of antiderivative is not currently implemented for this CAS.

```
[In] int((c + d*x^n)/(x^2*(a + b*x^(n/2))^(n-1/n)*(b*x^(n/2) - a)^(n-1/n)),x)
```

```
[Out] int((c + d*x^n)/(x^2*(a + b*x^(n/2))^(n-1/n)*(b*x^(n/2) - a)^(n-1/n)), x)
```





# Chapter 4

## Appendix

### Local contents

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## 4.1 Download section

The following zip files contain the raw integrals used in this test.

**Mathematica format** Mathematica\_syntax.zip

**Maple and Mupad format** Maple\_syntax.zip

**Sympy format** SYMPY\_syntax.zip

**Sage math format** SAGE\_syntax.zip

## 4.2 Listing of Grading functions

The following are the current version of the grading functions used for grading the quality of the antiderivative with reference to the optimal antiderivative included in the test suite.

There is a version for Maple and for Mathematica/Rubi. There is a version for grading Sympy and version for use with Sagemath.

The following are links to the current source code.

The following are the listings of source code of the grading functions.

### 4.2.1 Mathematica and Rubi grading function

```
(* Original version thanks to Albert Rich emailed on 03/21/2017 *)
(* ::Package:: *)

(* Nasser: April 7, 2022. add second output which gives reason for the grade *)
(*           Small rewrite of logic in main function to make it*)
(*           match Maple's logic. No change in functionality otherwise*)

(* ::Subsection:: *)
(*GradeAntiderivative[result,optimal]*)

(* ::Text:: *)
(*If result and optimal are mathematical expressions, *)
(*           GradeAntiderivative[result,optimal] returns*)
(* "F" if the result fails to integrate an expression that*)
(*           is integrable*)
(* "C" if result involves higher level functions than necessary*)
(* "B" if result is more than twice the size of the optimal*)
(*           antiderivative*)
(* "A" if result can be considered optimal*)
```

```

GradeAntiderivative[result_,optimal_] := Module[{expnResult,expnOptimal,leafCountResult,leafC
  expnResult = ExpnType[result];
  expnOptimal = ExpnType[optimal];
  leafCountResult = LeafCount[result];
  leafCountOptimal = LeafCount[optimal];

  (*Print["expnResult=",expnResult," expnOptimal=",expnOptimal];*)
  If[expnResult<=expnOptimal,
    If[Not[FreeQ[result,Complex]], (*result contains complex*)
      If[Not[FreeQ[optimal,Complex]], (*optimal contains complex*)
        If[leafCountResult<=2*leafCountOptimal,
          finalresult={"A","none"}
          ,(*ELSE*)
          finalresult={"B","Both result and optimal contain complex but leaf count
        ]
        ,(*ELSE*)
        finalresult={"C","Result contains complex when optimal does not."}
      ]
      ,(*ELSE*)(*result does not contains complex*)
      If[leafCountResult<=2*leafCountOptimal,
        finalresult={"A","none"}
        ,(*ELSE*)
        finalresult={"B","Leaf count is larger than twice the leaf count of optimal. $
      ]
    ]
    ,(*ELSE*)(*expnResult>expnOptimal*)
    If[FreeQ[result,Integrate] && FreeQ[result,Int],
      finalresult={"C","Result contains higher order function than in optimal. Order "<
    ,
    finalresult={"F","Contains unresolved integral."}
  ]
];

finalresult
]

(* ::Text:: *)
(*The following summarizes the type number assigned an *)
(*expression based on the functions it involves*)
(*1 = rational function*)
(*2 = algebraic function*)
(*3 = elementary function*)
(*4 = special function*)
(*5 = hyperpergeometric function*)
(*6 = appell function*)
(*7 = rootsum function*)
(*8 = integrate function*)

```



```

ExpIntegralE, ExpIntegralEi, LogIntegral,
SinIntegral, CosIntegral, SinhIntegral, CoshIntegral,
Gamma, LogGamma, PolyGamma,
Zeta, PolyLog, ProductLog,
EllipticF, EllipticE, EllipticPi
},func]

HypergeometricFunctionQ[func_] :=
  MemberQ[{Hypergeometric1F1,Hypergeometric2F1,HypergeometricPFQ},func]

AppellFunctionQ[func_] :=
  MemberQ[{AppellF1},func]

```

## 4.2.2 Maple grading function

```

# File: GradeAntiderivative.mpl
# Original version thanks to Albert Rich emailed on 03/21/2017

#Nasser 03/22/2017 Use Maple leaf count instead since buildin
#Nasser 03/23/2017 missing 'ln' for ElementaryFunctionQ added
#Nasser 03/24/2017 corrected the check for complex result
#Nasser 10/27/2017 check for leafsize and do not call ExpnType()
#
# if leaf size is "too large". Set at 500,000
#Nasser 12/22/2019 Added debug flag, added 'dilog' to special functions
#
# see problem 156, file Apostol_Problems
#Nasser 4/07/2022 add second output which gives reason for the grade

GradeAntiderivative := proc(result,optimal)
local leaf_count_result,
      leaf_count_optimal,
      ExpnType_result,
      ExpnType_optimal,
      debug:=false;

  leaf_count_result:=leafcount(result);
  #do NOT call ExpnType() if leaf size is too large. Recursion problem
  if leaf_count_result > 500000 then
    return "B","result has leaf size over 500,000. Avoiding possible recursion issues";
  fi;

  leaf_count_optimal := leafcount(optimal);
  ExpnType_result := ExpnType(result);
  ExpnType_optimal := ExpnType(optimal);

```

```

    if debug then
        print("ExpnType_result",ExpnType_result," ExpnType_optimal=",ExpnType_optimal);
    fi;

# If result and optimal are mathematical expressions,
# GradeAntiderivative[result,optimal] returns
# "F" if the result fails to integrate an expression that
#   is integrable
# "C" if result involves higher level functions than necessary
# "B" if result is more than twice the size of the optimal
#   antiderivative
# "A" if result can be considered optimal

#This check below actually is not needed, since I only
#call this grading only for passed integrals. i.e. I check
#for "F" before calling this. But no harm of keeping it here.
#just in case.

if not type(result,freeof('int')) then
    return "F","Result contains unresolved integral";
fi;

if ExpnType_result<=ExpnType_optimal then
    if debug then
        print("ExpnType_result<=ExpnType_optimal");
    fi;
    if is_contains_complex(result) then
        if is_contains_complex(optimal) then
            if debug then
                print("both result and optimal complex");
            fi;
            if leaf_count_result<=2*leaf_count_optimal then
                return "A","";
            else
                return "B",cat("Both result and optimal contain complex but leaf count of r
                    convert(leaf_count_result,string)," vs. $2 (" ,
                    convert(leaf_count_optimal,string)," ) = ",convert(2*leaf_co

        end if
    else #result contains complex but optimal is not
        if debug then
            print("result contains complex but optimal is not");
        fi;
        return "C","Result contains complex when optimal does not.";
    fi;
else # result do not contain complex

```

```

    # this assumes optimal do not as well. No check is needed here.
    if debug then
        print("result do not contain complex, this assumes optimal do not as well")
    fi;
    if leaf_count_result<=2*leaf_count_optimal then
        if debug then
            print("leaf_count_result<=2*leaf_count_optimal");
        fi;
        return "A","";
    else
        if debug then
            print("leaf_count_result>2*leaf_count_optimal");
        fi;
        return "B",cat("Leaf count of result is larger than twice the leaf count of o
                        convert(leaf_count_result,string)," $ vs. $2(",
                        convert(leaf_count_optimal,string),")=",convert(2*leaf_cou

    fi;
    fi;
else #ExpnType(result) > ExpnType(optimal)
    if debug then
        print("ExpnType(result) > ExpnType(optimal)");
    fi;
    return "C",cat("Result contains higher order function than in optimal. Order ",
                  convert(ExpnType_result,string)," vs. order ",
                  convert(ExpnType_optimal,string),".");
fi;

end proc:

#
# is_contains_complex(result)
# takes expressions and returns true if it contains "I" else false
#
#Nasser 032417
is_contains_complex:= proc(expression)
    return (has(expression,I));
end proc:

# The following summarizes the type number assigned an expression
# based on the functions it involves
# 1 = rational function
# 2 = algebraic function
# 3 = elementary function
# 4 = special function
# 5 = hyperpergeometric function
# 6 = appell function
# 7 = rootsum function

```

```

# 8 = integrate function
# 9 = unknown function

ExpnType := proc(expn)
  if type(expn,'atomic') then
    1
  elif type(expn,'list') then
    apply(max,map(ExpnType,expn))
  elif type(expn,'sqrt') then
    if type(op(1,expn),'rational') then
      1
    else
      max(2,ExpnType(op(1,expn)))
    end if
  elif type(expn,'^^') then
    if type(op(2,expn),'integer') then
      ExpnType(op(1,expn))
    elif type(op(2,expn),'rational') then
      if type(op(1,expn),'rational') then
        1
      else
        max(2,ExpnType(op(1,expn)))
      end if
    else
      max(3,ExpnType(op(1,expn)),ExpnType(op(2,expn)))
    end if
  elif type(expn,'+`) or type(expn,'*`) then
    max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
  elif ElementaryFunctionQ(op(0,expn)) then
    max(3,ExpnType(op(1,expn)))
  elif SpecialFunctionQ(op(0,expn)) then
    max(4,apply(max,map(ExpnType,[op(expn)])))
  elif HypergeometricFunctionQ(op(0,expn)) then
    max(5,apply(max,map(ExpnType,[op(expn)])))
  elif AppellFunctionQ(op(0,expn)) then
    max(6,apply(max,map(ExpnType,[op(expn)])))
  elif op(0,expn)='int' then
    max(8,apply(max,map(ExpnType,[op(expn)]))) else
    9
  end if
end proc:

ElementaryFunctionQ := proc(func)
  member(func,[
    exp,log,ln,
    sin,cos,tan,cot,sec,csc,

```



```

    arcsin,arccos,arctan,arccot,arcsec,arccsc,
    sinh,cosh,tanh,coth,sech,csch,
    arcsinh,arccosh,arctanh,arccoth,arcsech,arccsch])
end proc:

SpecialFunctionQ := proc(func)
  member(func, [
    erf,erfc,erfi,
    FresnelS,FresnelC,
    Ei,Ei,Li,Si,Ci,Shi,Chi,
    GAMMA,lnGAMMA,Psi,Zeta,polylog,dilog,LambertW,
    EllipticF,EllipticE,EllipticPi])
end proc:

HypergeometricFunctionQ := proc(func)
  member(func, [Hypergeometric1F1,hypergeom,HypergeometricPFQ])
end proc:

AppellFunctionQ := proc(func)
  member(func, [AppellF1])
end proc:

# u is a sum or product.  rest(u) returns all but the
# first term or factor of u.
rest := proc(u) local v;
  if nops(u)=2 then
    op(2,u)
  else
    apply(op(0,u),op(2..nops(u),u))
  end if
end proc:

#leafcount(u) returns the number of nodes in u.
#Nasser 3/23/17 Replaced by build-in leafCount from package in Maple
leafcount := proc(u)
  MmaTranslator[Mma][LeafCount](u);
end proc:

```

### 4.2.3 Sympy grading function

```

#Dec 24, 2019. Nasser M. Abbasi:
#      Port of original Maple grading function by
#      Albert Rich to use with Sympy/Python
#Dec 27, 2019 Nasser. Added `RootSum`. See problem 177, Timofeev file
#      added 'exp_polar'
from sympy import *

def leaf_count(expr):
    #sympy do not have leaf count function. This is approximation
    return round(1.7*count_ops(expr))

def is_sqrt(expr):
    if isinstance(expr,Pow):
        if expr.args[1] == Rational(1,2):
            return True
        else:
            return False
    else:
        return False

def is_elementary_function(func):
    return func in [exp,log,ln,sin,cos,tan,cot,sec,csc,
        asin,acos,atan,acot,asec,acsc,sinh,cosh,tanh,coth,sech,csch,
        asinh,acosh,atanh,acoth,asech,acsch
    ]

def is_special_function(func):
    return func in [ erf,erfc,erfi,
        fresnelc,fresnelc,Ei,Ei,Li,Si,Ci,Shi,Chi,
        gamma,loggamma,digamma,zeta,polylog,LambertW,
        elliptic_f,elliptic_e,elliptic_pi,exp_polar
    ]

def is_hypergeometric_function(func):
    return func in [hyper]

def is_appell_function(func):
    return func in [appellf1]

def is_atom(expn):
    try:
        if expn.isAtom or isinstance(expn,int) or isinstance(expn,float):
            return True
        else:
            return False

```

```

except AttributeError as error:
    return False

def expnType(expn):
    debug=False
    if debug:
        print("expn=",expn,"type(expn)=",type(expn))

    if is_atom(expn):
        return 1
    elif isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
            return 1
        else:
            return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
    elif isinstance(expn,Pow): #type(expn,'^')
        if isinstance(expn.args[1],Integer): #type(op(2,expn),'integer')
            return expnType(expn.args[0]) #ExpnType(op(1,expn))
        elif isinstance(expn.args[1],Rational): #type(op(2,expn),'rational')
            if isinstance(expn.args[0],Rational): #type(op(1,expn),'rational')
                return 1
            else:
                return max(2,expnType(expn.args[0])) #max(2,ExpnType(op(1,expn)))
        else:
            return max(3,expnType(expn.args[0]),expnType(expn.args[1])) #max(3,ExpnType(op(1,expn)),ExpnT
    elif isinstance(expn,Add) or isinstance(expn,Mul): #type(expn,'+') or type(expn,'*')
        m1 = expnType(expn.args[0])
        m2 = expnType(list(expn.args[1:]))
        return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
    elif is_elementary_function(expn.func): #ElementaryFunctionQ(op(0,expn))
        return max(3,expnType(expn.args[0])) #max(3,ExpnType(op(1,expn)))
    elif is_special_function(expn.func): #SpecialFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(4,m1) #max(4,apply(max,map(ExpnType,[op(expn)])))
    elif is_hypergeometric_function(expn.func): #HypergeometricFunctionQ(op(0,expn))
        m1 = max(map(expnType, list(expn.args)))
        return max(5,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif is_appell_function(expn.func):
        m1 = max(map(expnType, list(expn.args)))
        return max(6,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
    elif isinstance(expn,RootSum):
        m1 = max(map(expnType, list(expn.args))) #Apply[Max,Append[Map[ExpnType,Apply[List,expn]],7]],
        return max(7,m1)
    elif str(expn).find("Integral") != -1:

```

```

    m1 = max(map(expnType, list(expn.args)))
    return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

#main function
def grade_antiderivative(result,optimal):

    #print ("Enter grade_antiderivative for sagemath")
    #print("Enter grade_antiderivative, result=",result," optimal=",optimal)

    leaf_count_result = leaf_count(result)
    leaf_count_optimal = leaf_count(optimal)

    #print("leaf_count_result=",leaf_count_result)
    #print("leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

    if str(result).find("Integral") != -1:
        grade = "F"
        grade_annotation = ""
    else:
        if expnType_result <= expnType_optimal:
            if result.has(I):
                if optimal.has(I): #both result and optimal complex
                    if leaf_count_result <= 2*leaf_count_optimal:
                        grade = "A"
                        grade_annotation = ""
                    else:
                        grade = "B"
                        grade_annotation = "Both result and optimal contain complex but leaf count of result is larger"
                else: #result contains complex but optimal is not
                    grade = "C"
                    grade_annotation = "Result contains complex when optimal does not."
            else: # result do not contain complex, this assumes optimal do not as well
                if leaf_count_result <= 2*leaf_count_optimal:
                    grade = "A"
                    grade_annotation = ""
                else:
                    grade = "B"
                    grade_annotation = "Leaf count of result is larger than twice the leaf count of optimal. "+str(leaf_count_result)
            else:
                grade = "C"
                grade_annotation = "Result contains higher order function than in optimal. Order "+str(ExpnType_result)

```

```
#print("Before returning. grade=",grade, " grade_annotation=",grade_annotation)

return grade, grade_annotation
```

#### 4.2.4 SageMath grading function

```
#Dec 24, 2019. Nasser: Ported original Maple grading function by
#      Albert Rich to use with Sagemath. This is used to
#      grade Fracas, Giac and Maxima results.
#Dec 24, 2019. Nasser: Added 'exp_integral_e' and 'sng', 'sin_integral'
#      'arctan2', 'floor', 'abs', 'log_integral'
#June 4, 2022 Made default grade_annotation "none" instead of "" due
#      issue later when reading the file.
#July 14, 2022. Added ellipticF. This is until they fix sagemath, then remove it.

from sage.all import *
from sage.symbolic.operators import add_vararg, mul_vararg

debug=False;

def tree_size(expr):
    r"""
    Return the tree size of this expression.
    """
    #print("Enter tree_size, expr is ",expr)

    if expr not in SR:
        # deal with lists, tuples, vectors
        return 1 + sum(tree_size(a) for a in expr)
    expr = SR(expr)
    x, aa = expr.operator(), expr.operands()
    if x is None:
        return 1
    else:
        return 1 + sum(tree_size(a) for a in aa)

def is_sqrt(expr):
    if expr.operator() == operator.pow: #instance(expr,Pow):
        if expr.operands()[1]==1/2: #expr.args[1] == Rational(1,2):
            if debug: print ("expr is sqrt")
            return True
        else:
            return False
    else:
        return False
```

```

def is_elementary_function(func):
    #debug=False
    m = func.name() in ['exp','log','ln',
        'sin','cos','tan','cot','sec','csc',
        'arcsin','arccos','arctan','arccot','arcsec','arccsc',
        'sinh','cosh','tanh','coth','sech','csch',
        'arcsinh','arccosh','arctanh','arcoth','arcsech','arccsch','sgn',
        'arctan2','floor','abs'
    ]
    if debug:
        if m:
            print ("func ", func , " is elementary_function")
        else:
            print ("func ", func , " is NOT elementary_function")

    return m

def is_special_function(func):
    #debug=False
    if debug:
        print ("type(func)=", type(func))

    m= func.name() in ['erf','erfc','erfi','fresnel_sin','fresnel_cos','Ei',
        'Ei','Li','Si','sin_integral','Ci','cos_integral','Shi','sinh_integral',
        'Chi','cosh_integral','gamma','log_gamma','psi,zeta',
        'polylog','lambert_w','elliptic_f','elliptic_e','ellipticF',
        'elliptic_pi','exp_integral_e','log_integral']

    if debug:
        print ("m=",m)
        if m:
            print ("func ", func , " is special_function")
        else:
            print ("func ", func , " is NOT special_function")

    return m

def is_hypergeometric_function(func):
    return func.name() in ['hypergeometric','hypergeometric_M','hypergeometric_U']

def is_appell_function(func):
    return func.name() in ['hypergeometric'] #[appellf1] can't find this in sagemath

```

```

def is_atom(expn):

    #debug=False
    if debug:
        print ("Enter is_atom, expn=",expn)

    if not hasattr(expn, 'parent'):
        return False

    #thanks to answer at https://ask.sagemath.org/question/49179/what-is-sagemath-equivalent-to-atomic-try:
    if expn.parent() is SR:
        return expn.operator() is None
    if expn.parent() in (ZZ, QQ, AA, QQbar):
        return expn in expn.parent() # Should always return True
    if hasattr(expn.parent(), "base_ring") and hasattr(expn.parent(), "gens"):
        return expn in expn.parent().base_ring() or expn in expn.parent().gens()

    return False

except AttributeError as error:
    print("Exception,AttributeError in is_atom")
    print ("caught exception" , type(error).__name__ )
    return False

def expnType(expn):

    if debug:
        print (">>>>>Enter expnType, expn=", expn)
        print (">>>>>is_atom(expn)=", is_atom(expn))

    if is_atom(expn):
        return 1
    elif type(expn)==list: #isinstance(expn,list):
        return max(map(expnType, expn)) #apply(max,map(ExpnType,expn))
    elif is_sqrt(expn):
        if type(expn.operands()[0])==Rational: #type(isinstance(expn.args[0],Rational):
            return 1
        else:
            return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.args[0]))
    elif expn.operator() == operator.pow: #isinstance(expn,Pow)
        if type(expn.operands()[1])==Integer: #isinstance(expn.args[1],Integer)
            return expnType(expn.operands()[0]) #expnType(expn.args[0])
        elif type(expn.operands()[1])==Rational: #isinstance(expn.args[1],Rational)
            if type(expn.operands()[0])==Rational: #isinstance(expn.args[0],Rational)

```

```

    return 1
  else:
    return max(2,expnType(expn.operands()[0])) #max(2,expnType(expn.args[0]))
  else:
    return max(3,expnType(expn.operands()[0]),expnType(expn.operands()[1])) #max(3,expnType(expn.op
elif expn.operator() == add_vararg or expn.operator() == mul_vararg: #isinstance(expn,Add) or instan
    m1 = expnType(expn.operands()[0]) #expnType(expn.args[0])
    m2 = expnType(expn.operands()[1:]) #expnType(list(expn.args[1:]))
    return max(m1,m2) #max(ExpnType(op(1,expn)),max(ExpnType(rest(expn))))
elif is_elementary_function(expn.operator()): #is_elementary_function(expn.func)
    return max(3,expnType(expn.operands()[0]))
elif is_special_function(expn.operator()): #is_special_function(expn.func)
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(4,m1) #max(4,m1)
elif is_hypergeometric_function(expn.operator()): #is_hypergeometric_function(expn.func)
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(5,m1) #max(5,m1)
elif is_appell_function(expn.operator()):
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(6,m1) #max(6,m1)
elif str(expn).find("Integral") != -1: #this will never happen, since it
    #is checked before calling the grading function that is passed.
    #but kept it here.
    m1 = max(map(expnType, expn.operands())) #max(map(expnType, list(expn.args)))
    return max(8,m1) #max(5,apply(max,map(ExpnType,[op(expn)])))
else:
    return 9

#main function
def grade_antiderivative(result,optimal):

    if debug:
        print ("Enter grade_antiderivative for sagemath")
        print("Enter grade_antiderivative, result=",result)
        print("Enter grade_antiderivative, optimal=",optimal)
        print("type(anti)=",type(result))
        print("type(optimal)=",type(optimal))

    leaf_count_result = tree_size(result) #leaf_count(result)
    leaf_count_optimal = tree_size(optimal) #leaf_count(optimal)

    #if debug: print ("leaf_count_result=", leaf_count_result, "leaf_count_optimal=",leaf_count_optimal)

    expnType_result = expnType(result)
    expnType_optimal = expnType(optimal)

```



```

if debug: print ("expnType_result=", expnType_result, "expnType_optimal=",expnType_optimal)

if expnType_result <= expnType_optimal:
    if result.has(I):
        if optimal.has(I): #both result and optimal complex
            if leaf_count_result <= 2*leaf_count_optimal:
                grade = "A"
                grade_annotation = "none"
            else:
                grade = "B"
                grade_annotation = "Both result and optimal contain complex but leaf count of result is larger t
        else: #result contains complex but optimal is not
            grade = "C"
            grade_annotation = "Result contains complex when optimal does not."
    else: # result do not contain complex, this assumes optimal do not as well
        if leaf_count_result <= 2*leaf_count_optimal:
            grade = "A"
            grade_annotation = "none"
        else:
            grade = "B"
            grade_annotation = "Leaf count of result is larger than twice the leaf count of optimal. "+str(leaf_
else:
    grade = "C"
    grade_annotation = "Result contains higher order function than in optimal. Order "+str(expnType_resu

print("Before returning. grade=",grade, " grade_annotation=",grade_annotation)

return grade, grade_annotation

```